Edges and orientations

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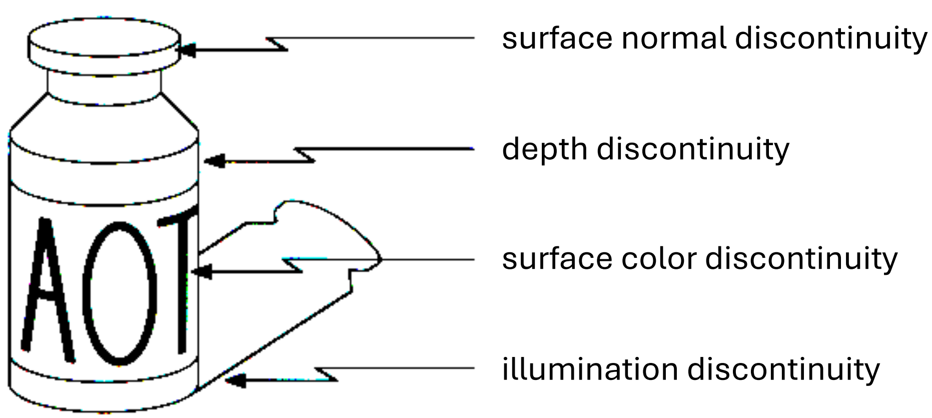
Edge detection

Winter in Kraków photographed by Marcin Ryczek

Edge detection

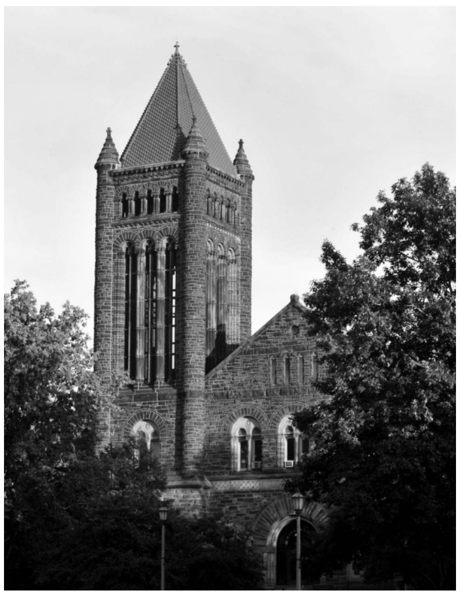
- **Goal:** Identify sudden changes (discontinuities) in an image
- Intuitively, edges carry most of the semantic and shape information from the image



Sources: D. Lowe and S. Seitz

Edge detection

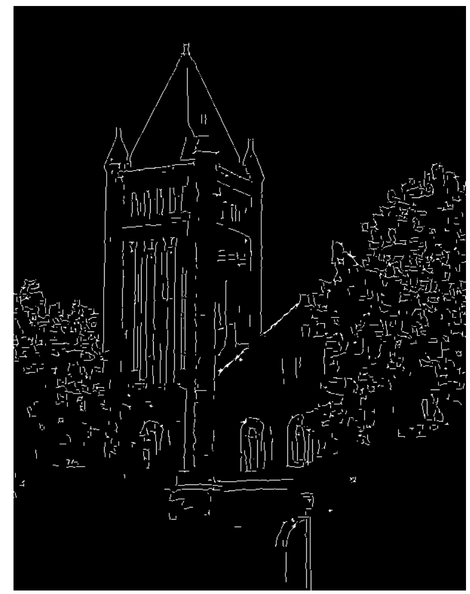
Input photo



Ideal: artist's line drawing

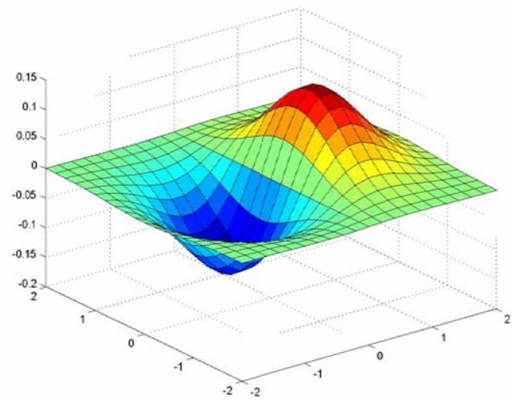
Image source

Reality

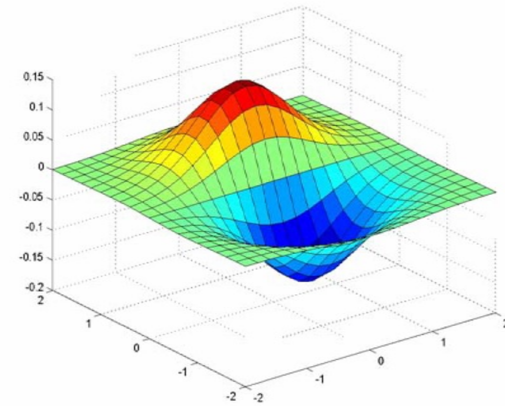


Source: S. Gupta

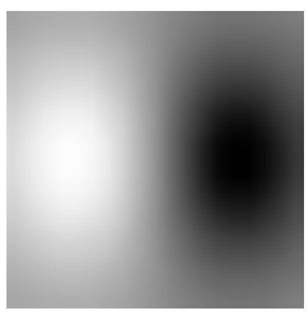
2D Derivative of Gaussian (d.o.g. or dog) filters

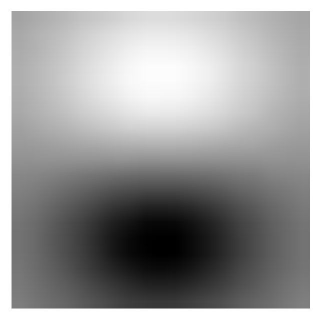


x-direction



y-direction

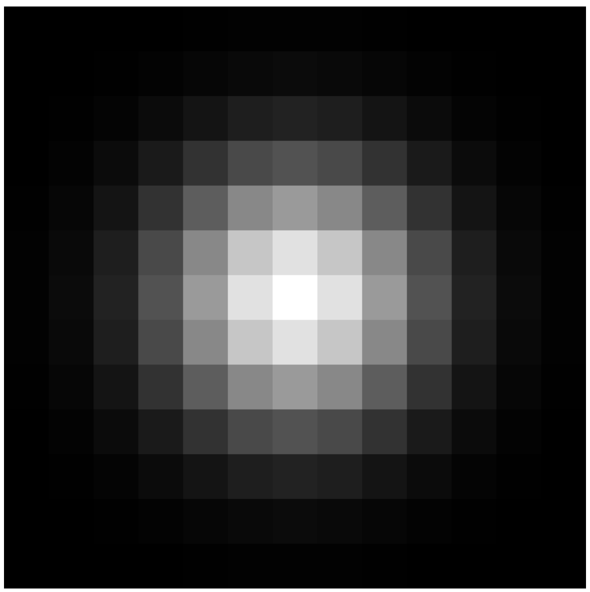




Separability of the Gaussian filter

$$\frac{1}{2\pi\sigma^2}\exp\left(-\frac{x^2+y^2}{2\sigma^2}\right) =$$

$$\frac{1}{\sqrt{2\pi}\sigma}\exp\left(-\frac{x^2}{2\sigma^2}\right) \quad \frac{1}{\sqrt{2\pi}\sigma}\exp\left(-\frac{y^2}{2\sigma^2}\right)$$



=

*

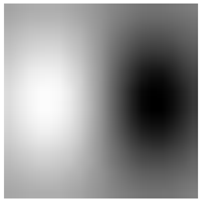
Note: matrix multiplication (outer product) and full convolution are the same in this special case

Adapted from [D. Fouhey and J. Johnson]

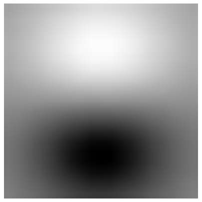
2D Derivative of Gaussian filters

- (Unnormalized) Gaussian derivatives:

$$\frac{\partial g}{\partial x} \propto -x \exp\left(-\frac{x^2}{2\sigma^2}\right) \exp\left(-\frac{y^2}{2\sigma^2}\right)$$



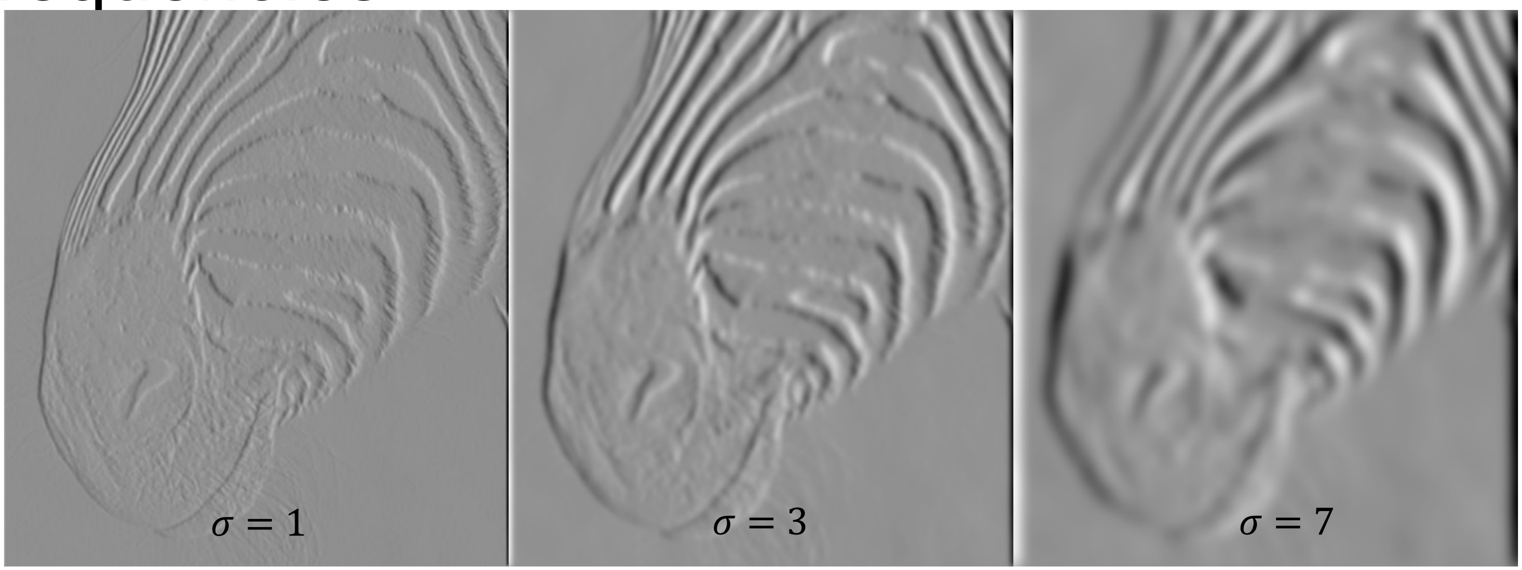
$$\frac{\partial g}{\partial y} \propto -y \exp\left(-\frac{y^2}{2\sigma^2}\right) \exp\left(-\frac{x^2}{2\sigma^2}\right)$$



- These are products of a 1D Gaussian in one direction and 1D derivative of Gaussian in the other direction!

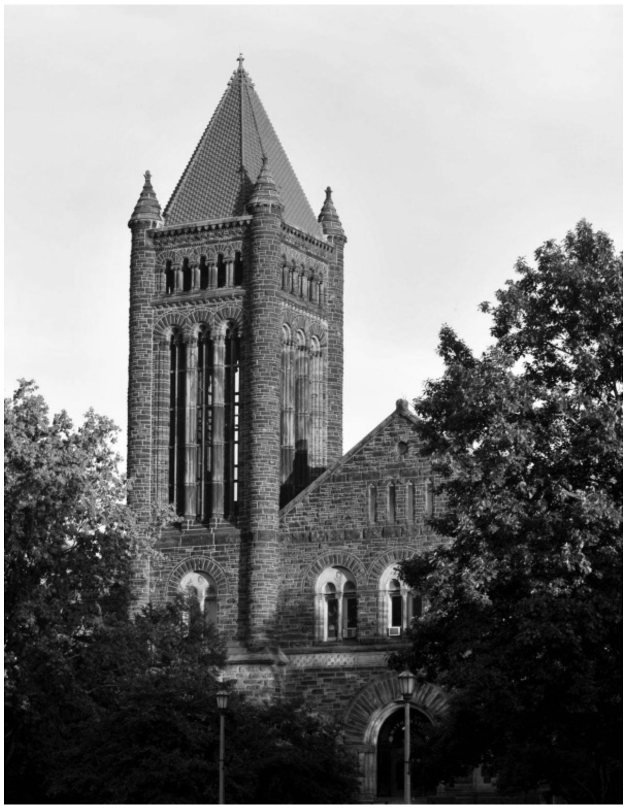
Derivative of Gaussian: Scale

- Using Gaussian derivatives with different values of σ finds structures at different scales or frequencies

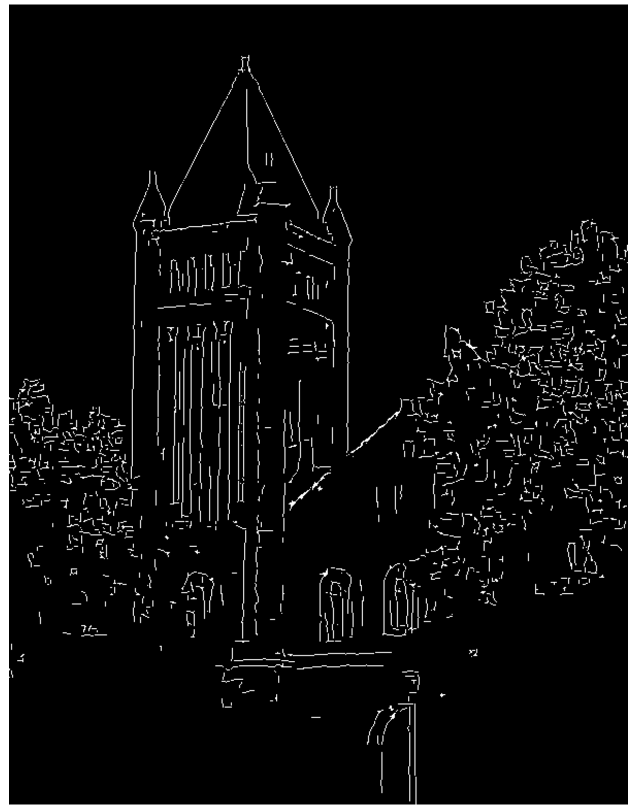


Source: D. Forsyth

Building an edge detector



original image

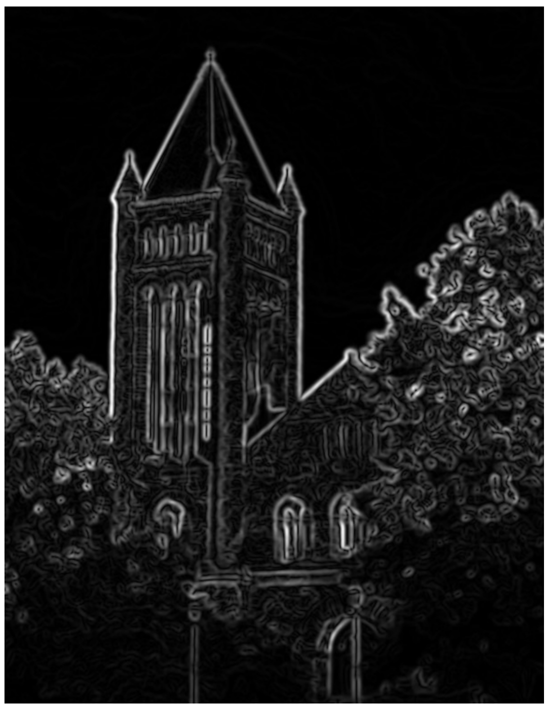


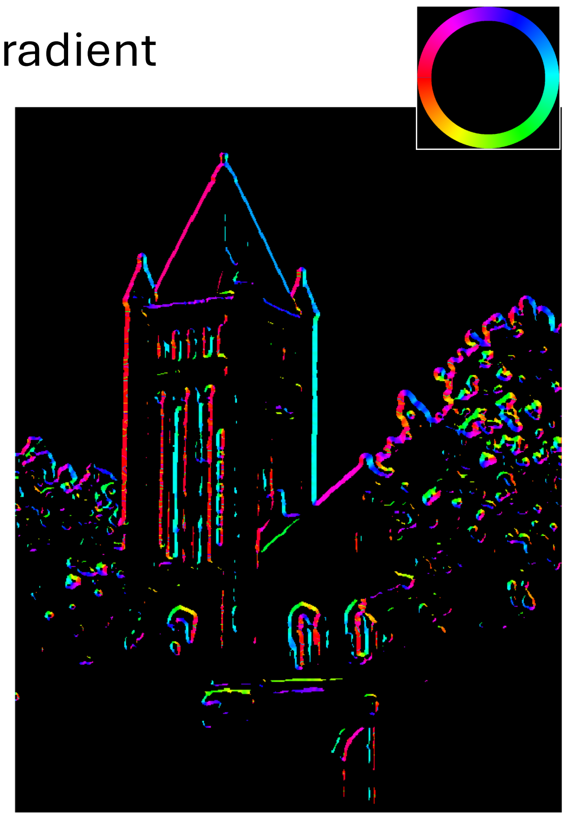
final output

J. Canny, A Computational Approach To Edge Detection, IEEE Trans. PAMI, 8:679-714, 1986

Building an edge detector

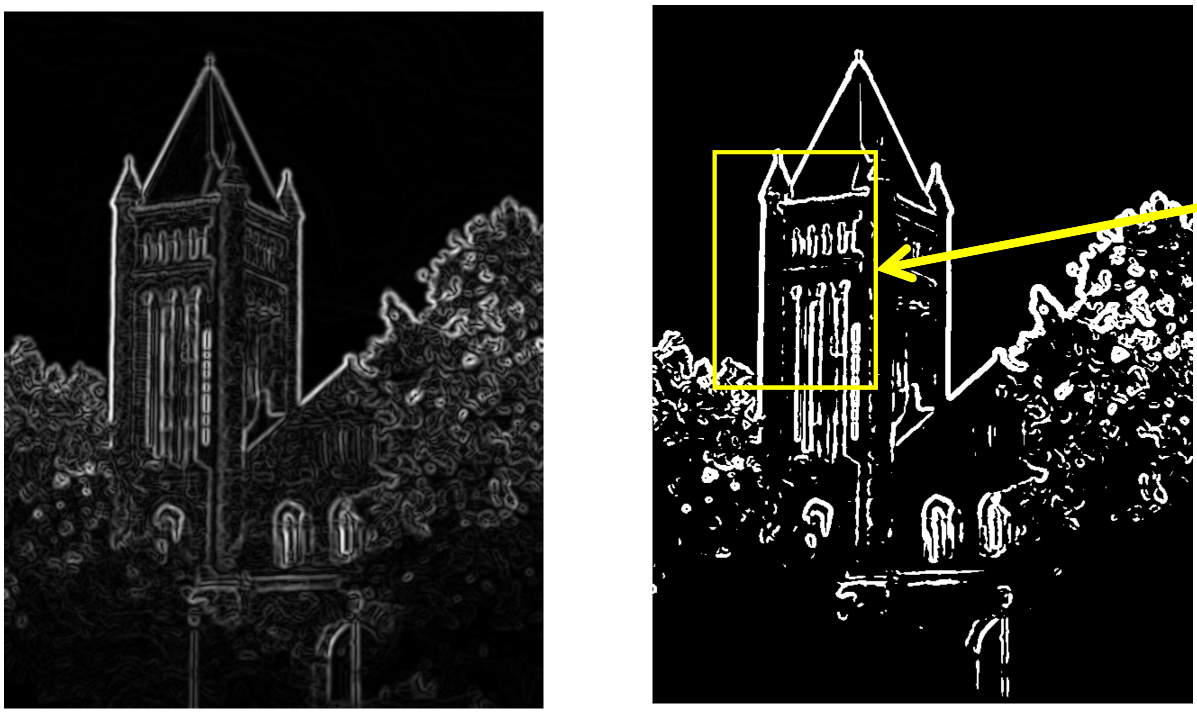
1. Compute x and y derivative images
2. Find magnitude and orientation of the gradient





Source: S. Gupta

Building an edge detector

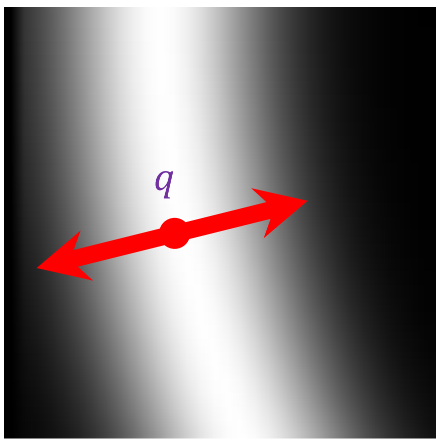


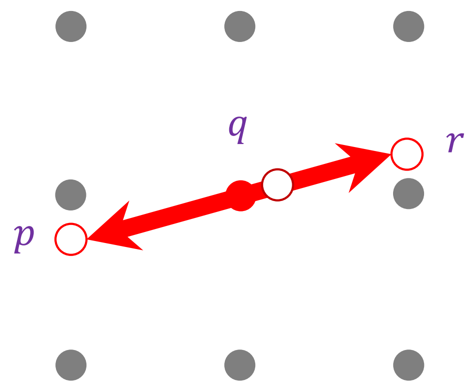
We get thick edge curves

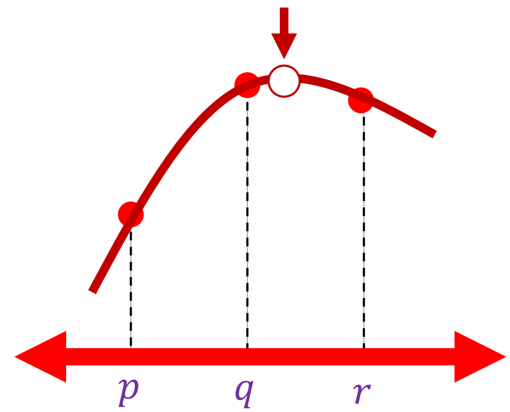
Thresholding the gradient magnitude

Source: S. Gupta

Non-maximum suppression







1D image “slice” normal to the edge

- For each location q above threshold, check that the gradient magnitude is higher than at adjacent points p and r along the direction of the gradient
  - Need to interpolate to get the gradient magnitude values at p and r
  - Can even use nonlinear interpolation to get sub-pixel edge localization!

Non-maximum suppression

NMS

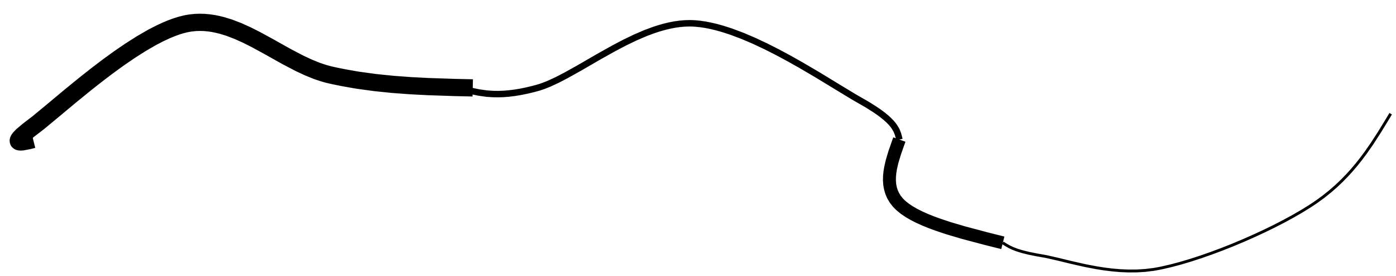
NMS > threshold

Another problem: pixels along this edge didn't survive the thresholding

Source: S. Gupta

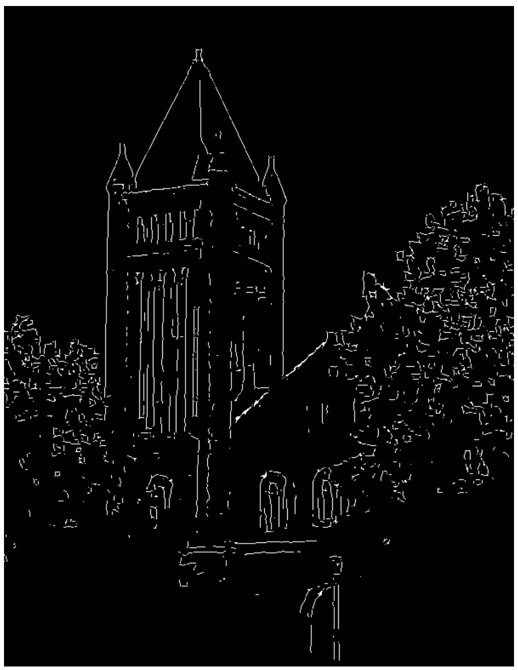
Hysteresis thresholding

- Use a high threshold to start edge curves, and a low threshold to continue them

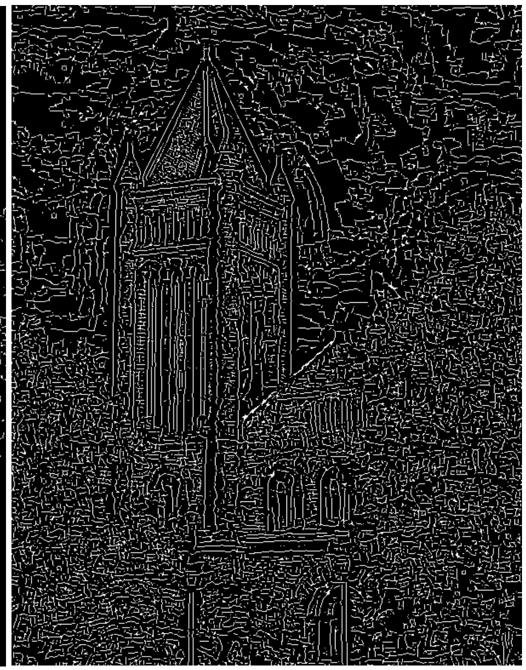


Source: Steve Seitz

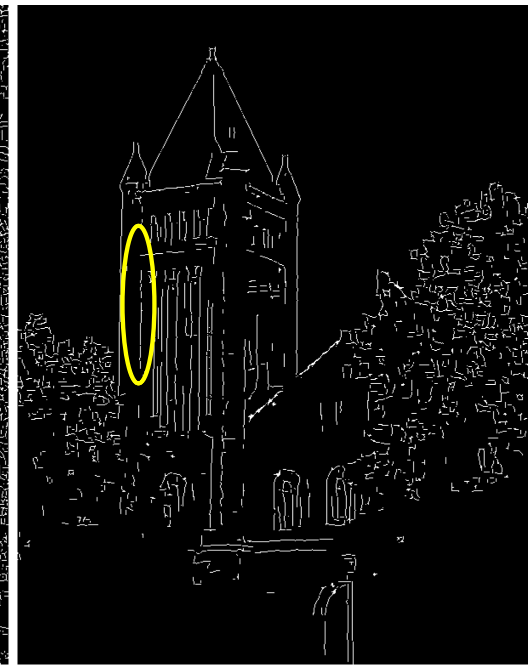
Hysteresis thresholding



high threshold
(strong edges)



low threshold
(weak edges)



hysteresis threshold

Source: S. Gupta

Recap: Canny edge detector

1. Compute x and y derivative images
2. Find magnitude and orientation of the gradient
3. Non-maximum suppression:
   - Thin wide “ridges” down to single pixel width
4. Linking and thresholding (hysteresis):
   - Define two thresholds: low and high
   - Use the high threshold to start edge curves and the low threshold to continue them

J. Canny, A Computational Approach To Edge Detection, IEEE Trans. PAMI, 8:679-714, 1986.

Image gradients vs. meaningful contours

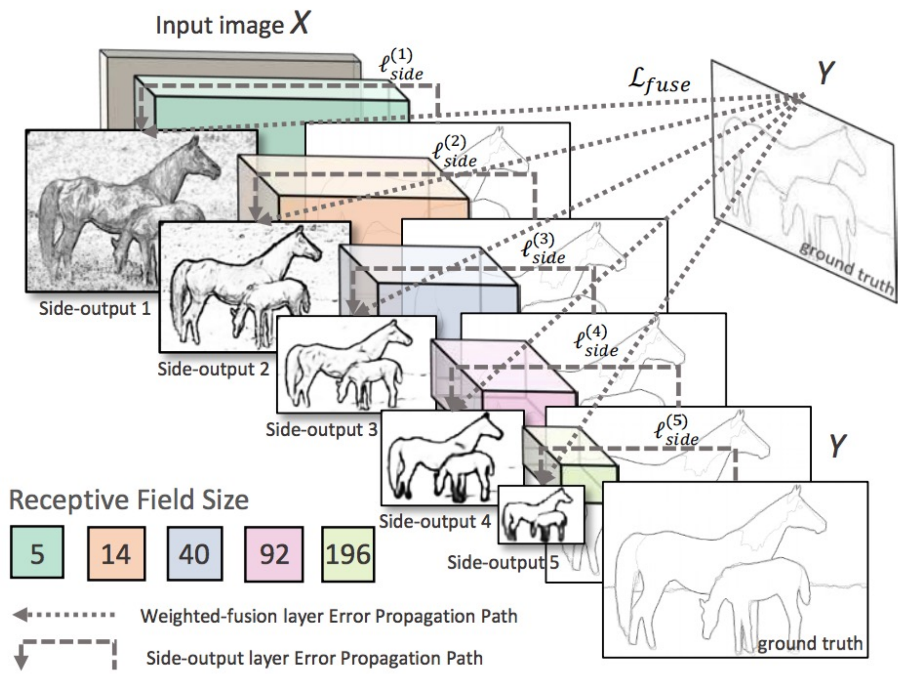
Image

Human segmentation

Gradient magnitude

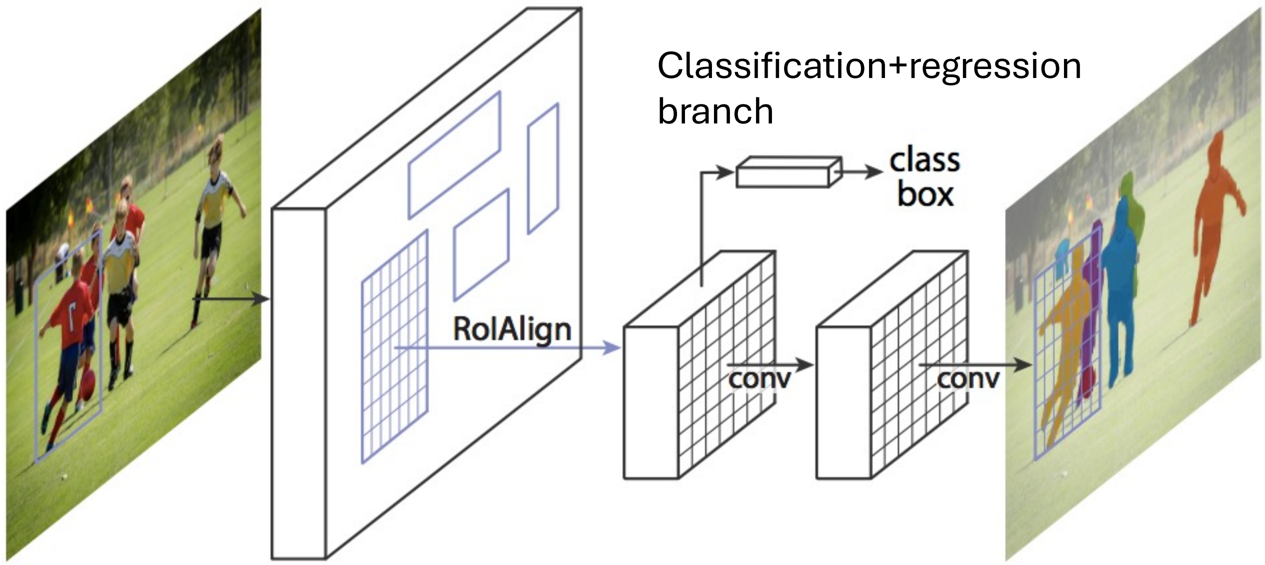
D. Martin, C. Fowlkes, D. Tal, and J. Malik. [A Database of Human Segmented Natural Images and its Application to Evaluating Segmentation Algorithms and Measuring Ecological Statistics](). ICCV 2001

Data-driven edge detection



S. Xie and Z. Tu, Holistically-nested edge detection, ICCV 2015

Most successful approach in practice: Top-down segmentation



Mask branch: output binary segmentation for each instance

K. He, G. Gkioxari, P. Dollar, and R. Girshick, [Mask R-CNN](), ICCV 2017 (Best Paper Award)

Problem:

- Scaling the image scales gradient magnitude

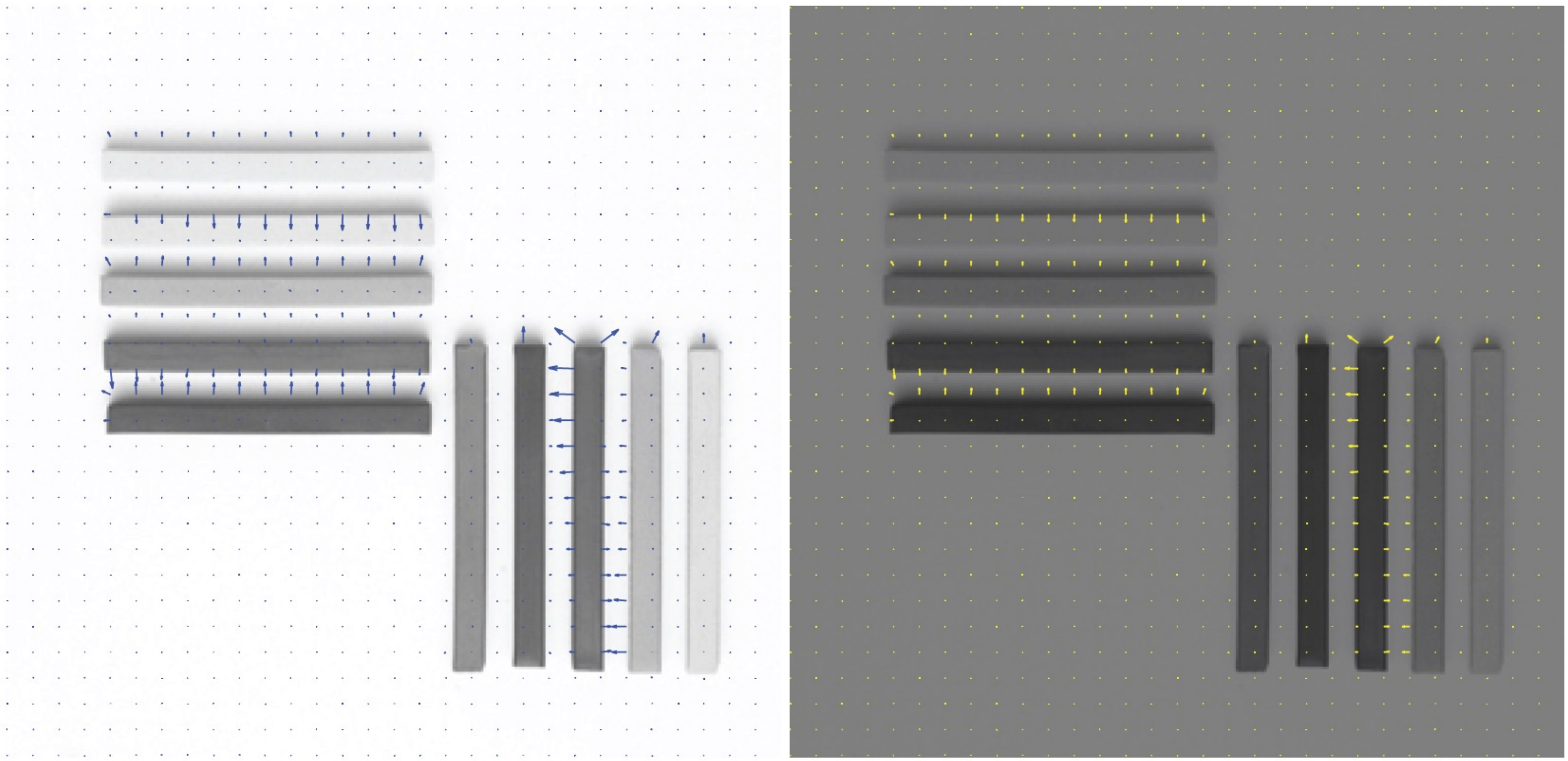
$$f \rightarrow kf \text{ implies } \sqrt{\frac{\partial f}{\partial x}^2 + \frac{\partial f}{\partial y}^2} \rightarrow k\sqrt{\frac{\partial f}{\partial x}^2 + \frac{\partial f}{\partial y}^2}$$

- Which causes problems with thresholds, etc
  - - image gets darker, some edges disappear
  - - image gets lighter, some edges appear
- Hysteresis helps, but doesn't cure

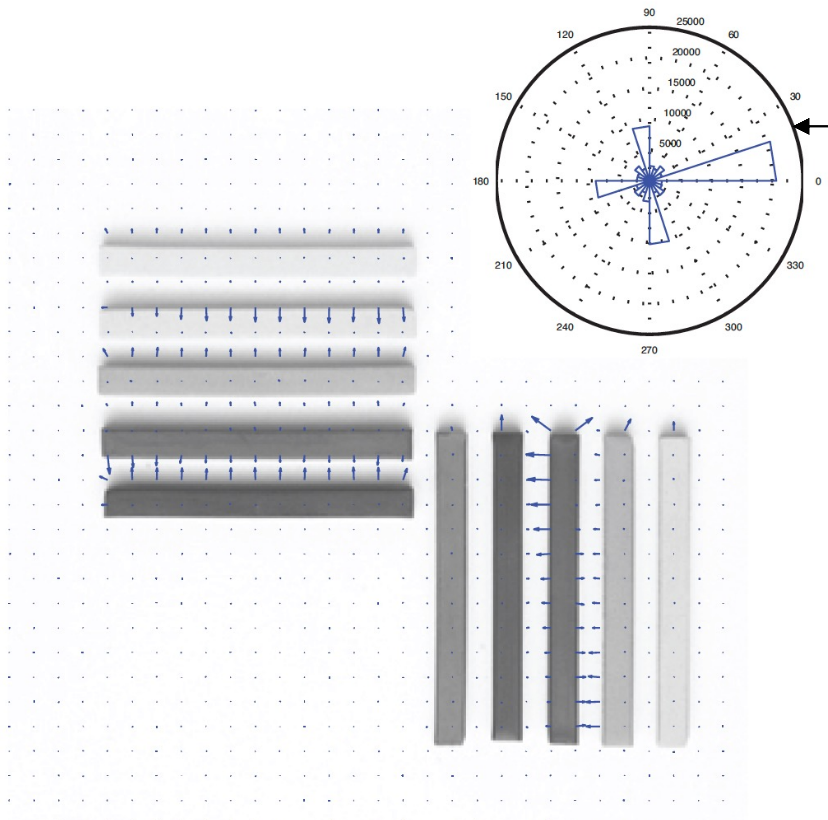
Orientations don't change with illumination

$$f \to kf \text{ implies } \left(\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}\right) \to k\left(\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}\right)$$

- Q: build a representation out of orientations?

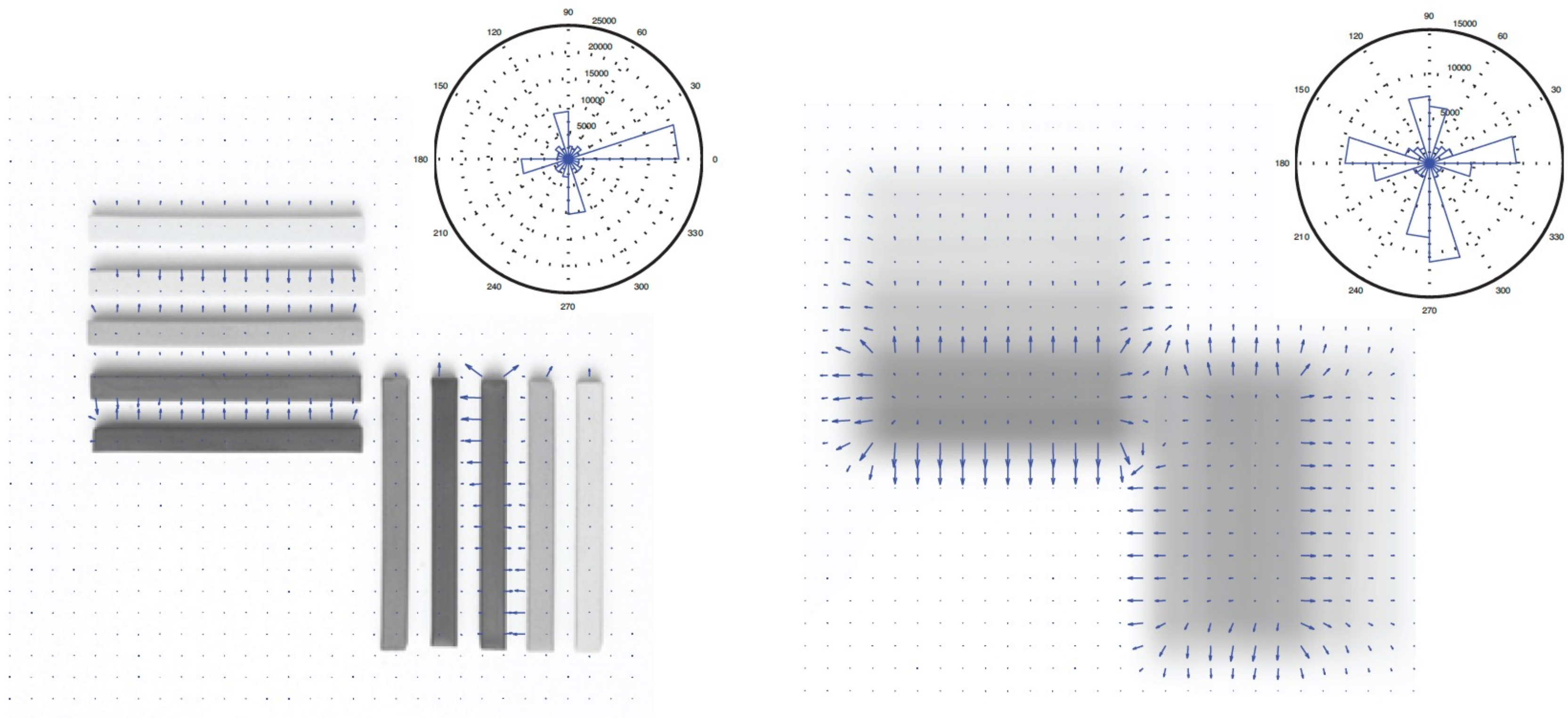


Orientation histograms

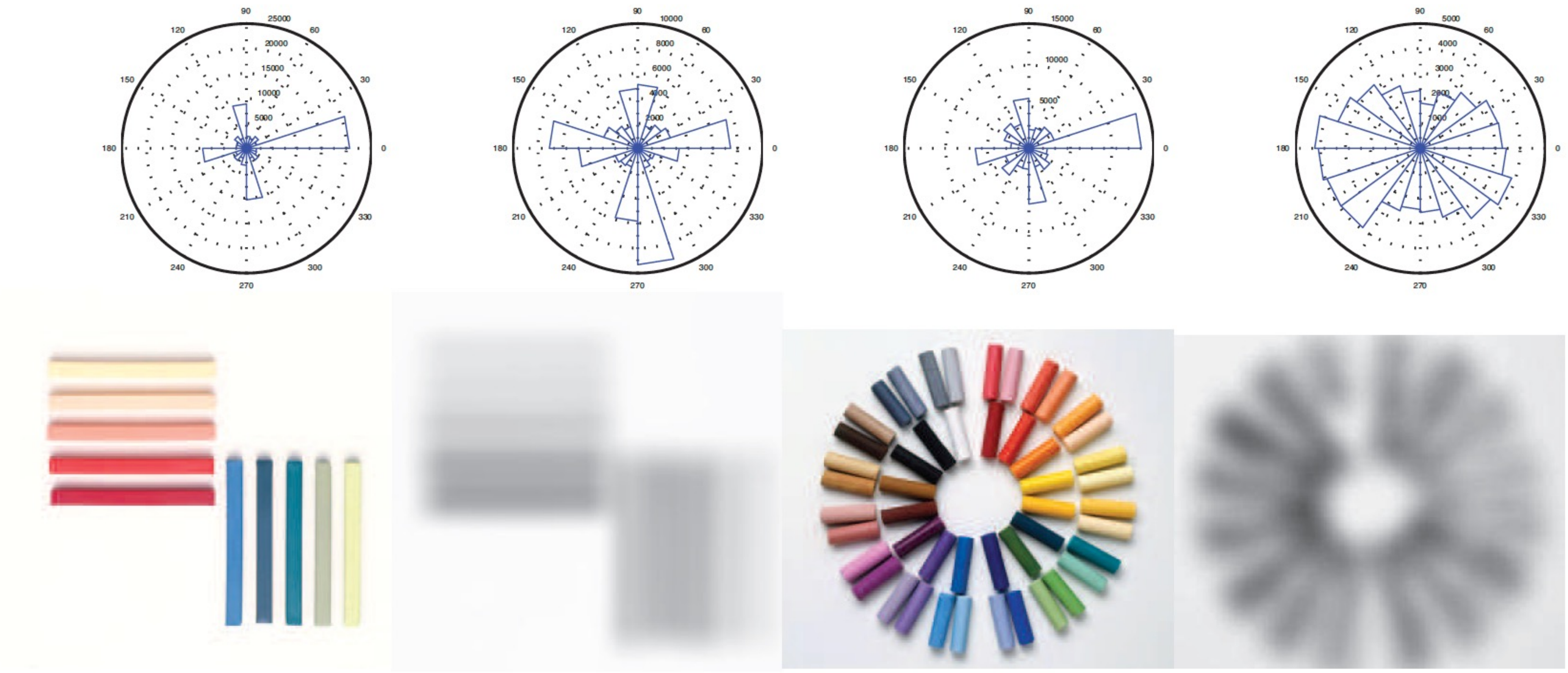


Rose plot, which shows number of vectors at each range of angles

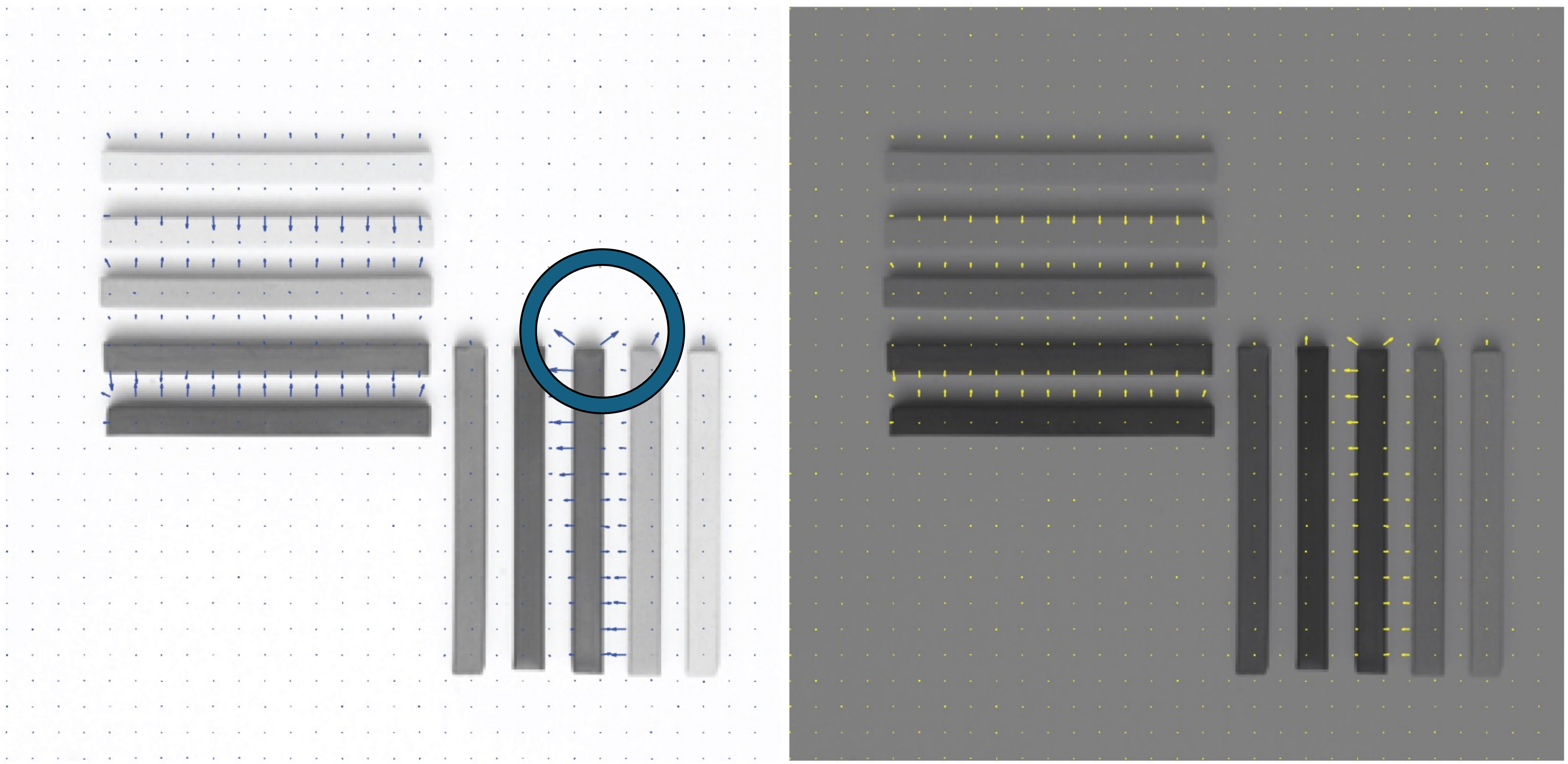
Orientation histogram depends on scale



Different patterns have different orientation histograms



Notice something important...



Think about this...

8.1. Why do edge detectors look for a local maximum of the gradient magnitude?
8.2. Why is hysteresis helpful for edge detection?