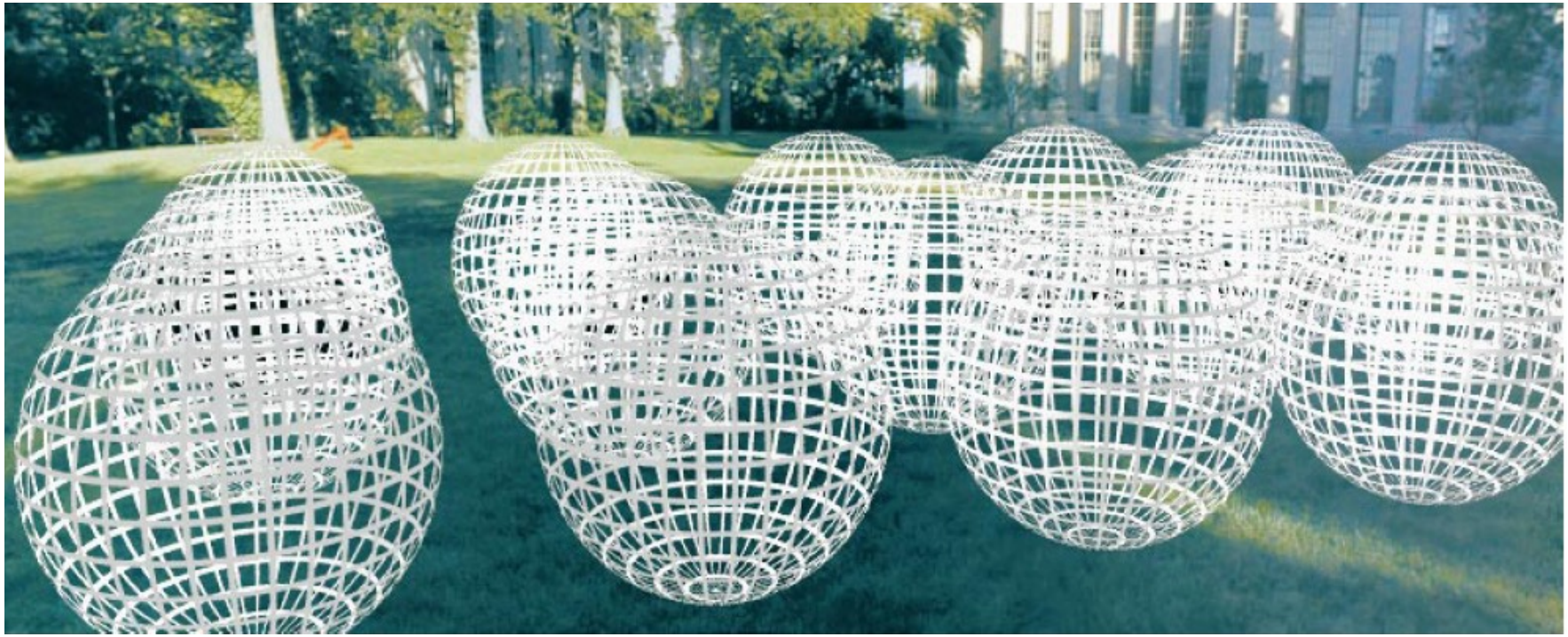
Modeling the plenoptic function



Adopted from: CS194: Intro to Comp. Vision, and Comp. Photo
Alexei Efros & Angjoo Kanazawa, UC Berkeley, Fall 2021

Outline

- The plenoptic function
- Two-plane light fields
- Plenoptic camera
- Neural radiance fields (NeRFs)

Representing 3D

- Multiview stereo: create a textured 3D model from the images, use traditional graphics to render
  - 3D models have many applications
    - Compute length, area, volume, etc. etc.
    - Render

But all we want to do is render – why not aim for representation that is purely intended for rendering?

A light field:

color of light travelling in any direction at any point

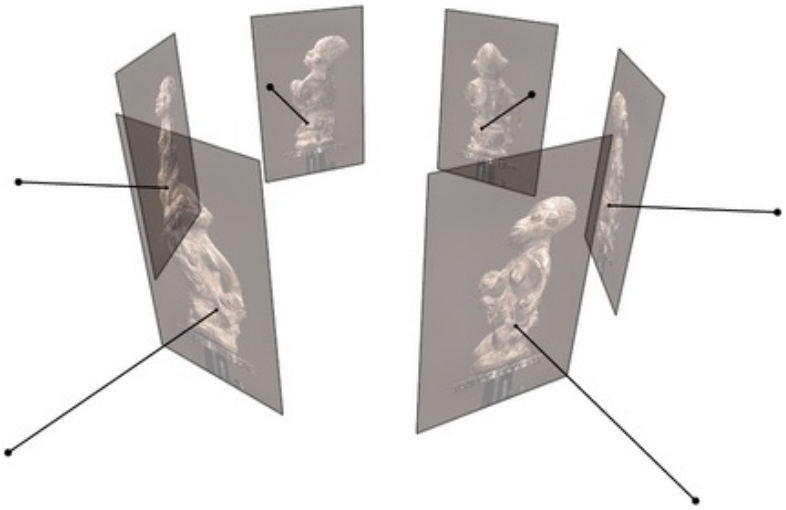


Figure source: C. Hernandez, N. Snavely

The light field, or plenoptic function

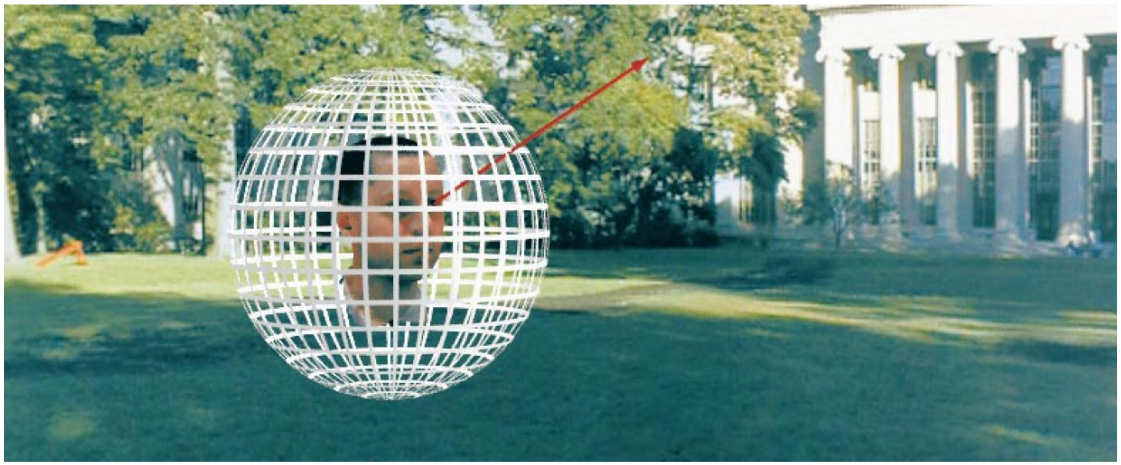


Figure by Leonard McMillan

Q: What is the set of all things that we can ever see?

A: The *plenoptic function*

E. Adelson and J. Bergen. The plenoptic function and the elements of early vision. Computational models of visual processing, MIT Press, 1991

The light field, or plenoptic function

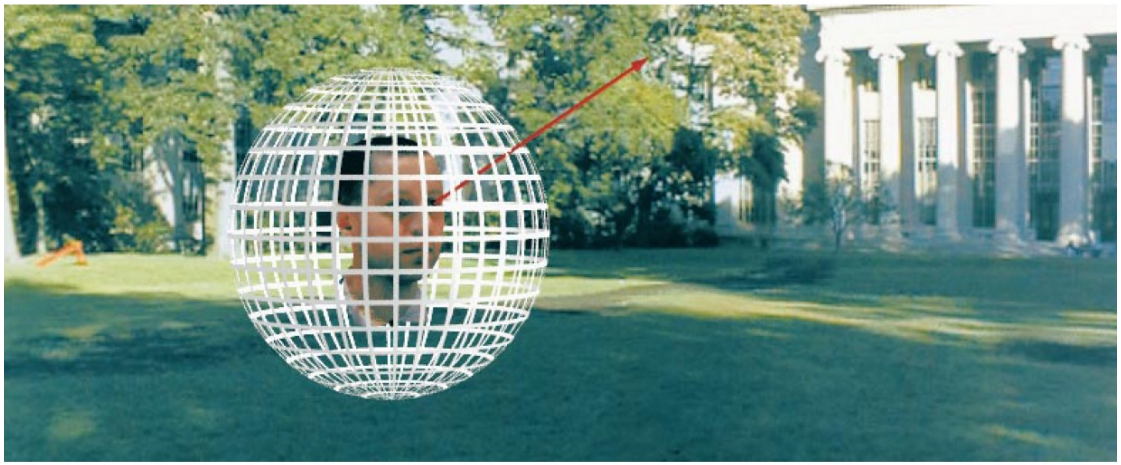


Figure by Leonard McMillan

Q: What is the set of all things that we can ever see?

A: The *plenoptic function*

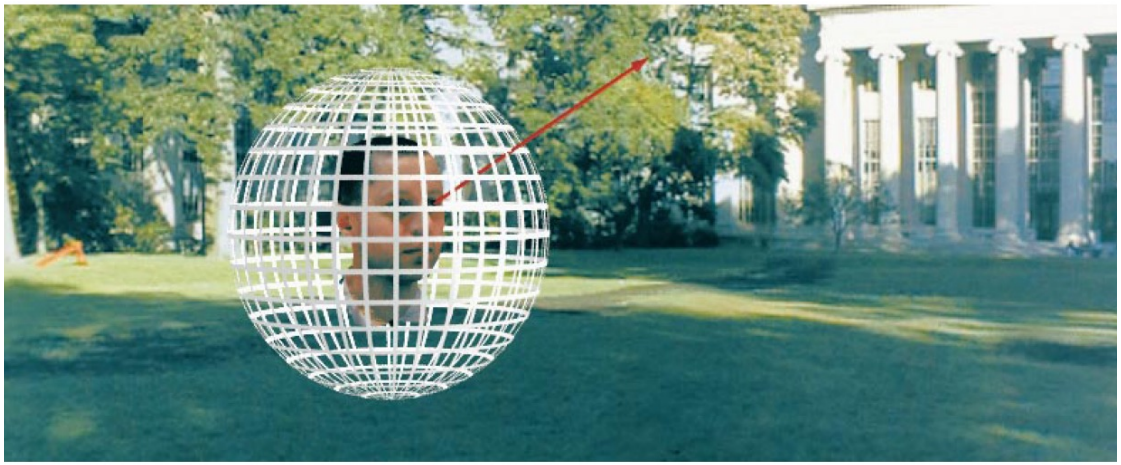
Let's start with a stationary person and try to parameterize <u>everything</u> that they can see…

Grayscale snapshot

$L(\theta, \phi)$

- Intensity of light
  - Seen from a single view point
  - At a single time
  - Averaged over the wavelengths of the visible spectrum

Color snapshot

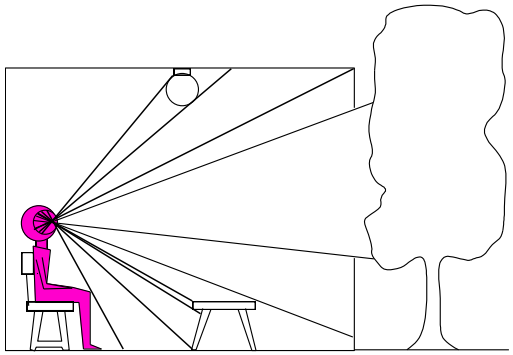


$L(\theta, \phi, \lambda)$

- Intensity of light
  - Seen from a single view point
  - At a single time
  - As a function of wavelength

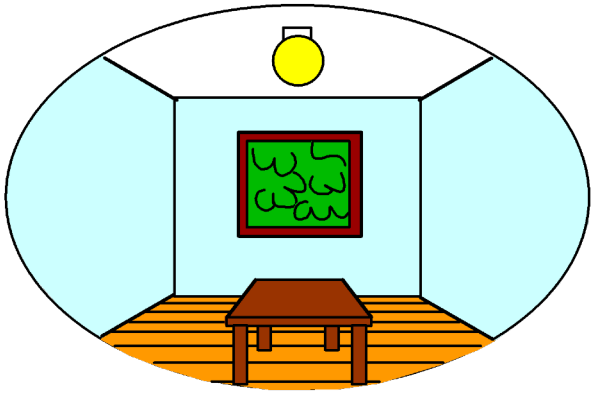
Modeling the light field

3D world



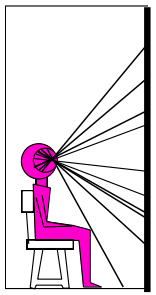
Point of observation

2D image



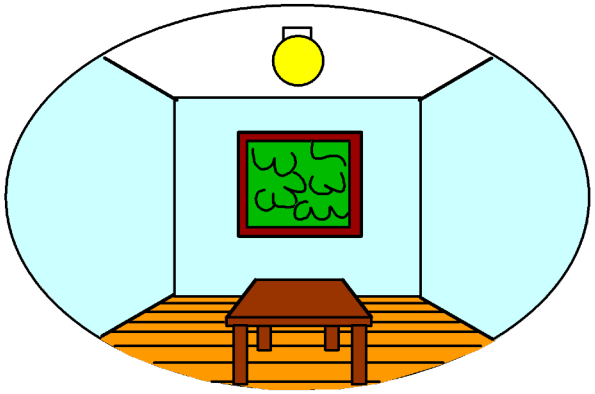
Modeling the light field

3D world

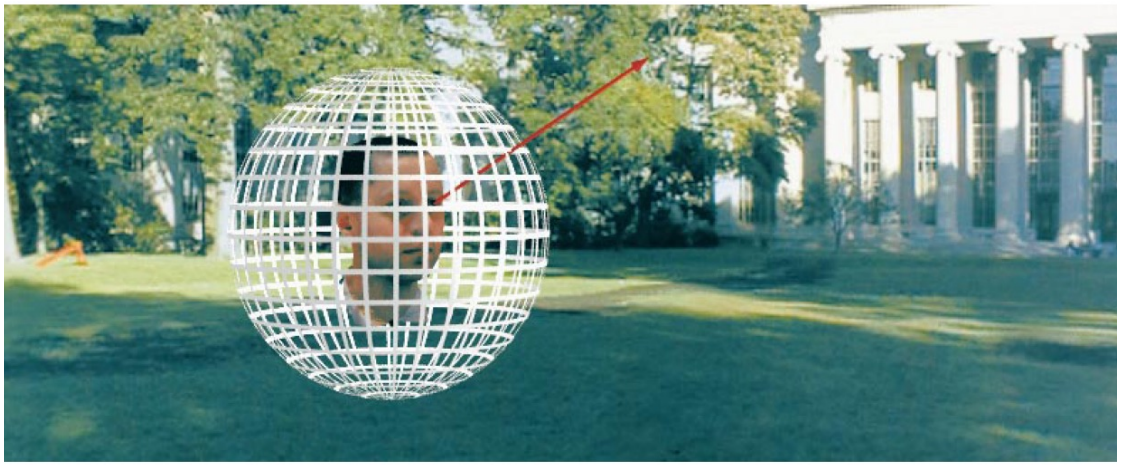


Painted
backdrop

2D image



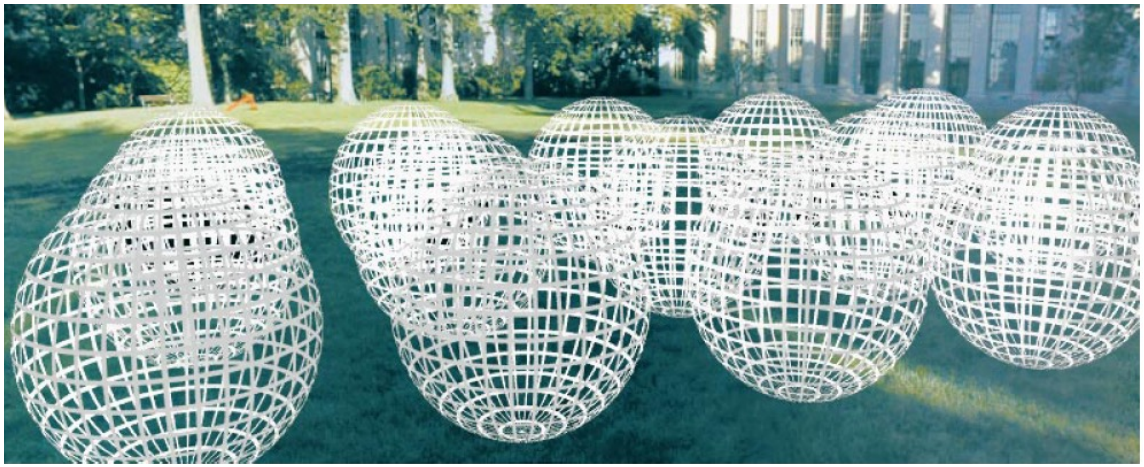
A movie



$$L(\theta, \phi, \lambda, t)$$

- Intensity of light
  - Seen from a single view point
  - Over time
  - As a function of wavelength

Holographic movie



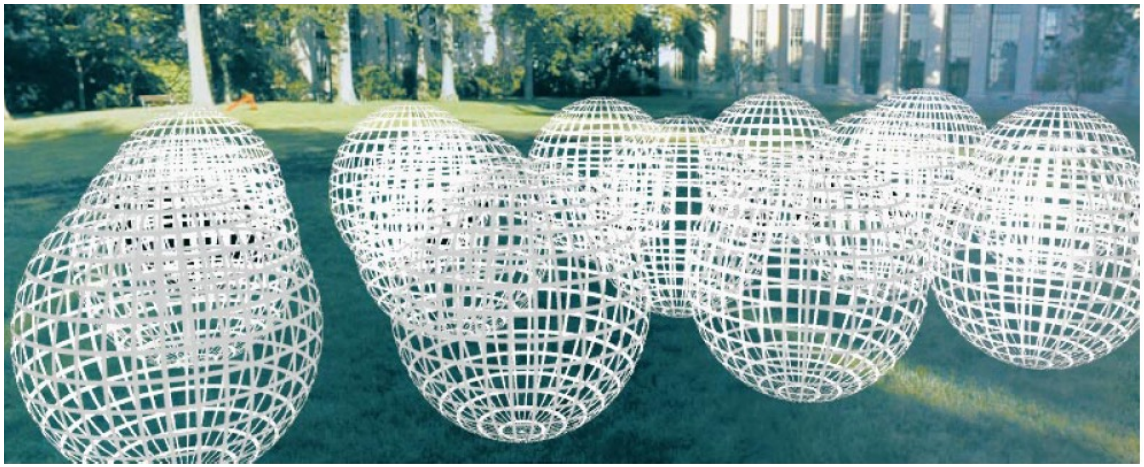
$$L(\theta, \phi, \lambda, t, x, y, z)$$

- Intensity of light
  - Seen from ANY viewpoint
  - Over time
  - As a function of wavelength

Light field modeling: Outline

- The plenoptic function
- Two-plane light fields
- Plenoptic camera
- Neural radiance fields (NeRFs)

The plenoptic function



$$L(\theta, \phi, \lambda, t, x, y, z)$$

- Can reconstruct every possible view, at every moment, from every position, at every wavelength
- Contains every photograph, every movie, everything that anyone has ever seen! it completely captures our visual reality!
- Not bad for a function…

The plenoptic function - careful!

- This is a function whose domain is nasty
  - all maximal directed line segments (lines) in free space
  - the domain can get very complicated
    - easy when there aren't any objects
    - otherwise, much harder
  - domain is sometimes called a visibility complex

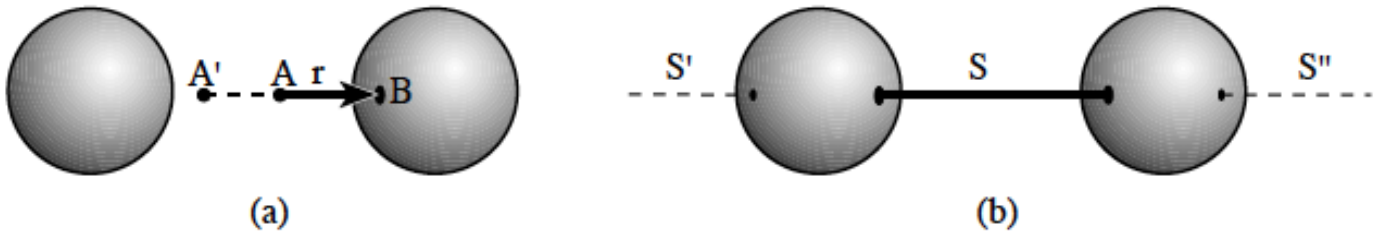
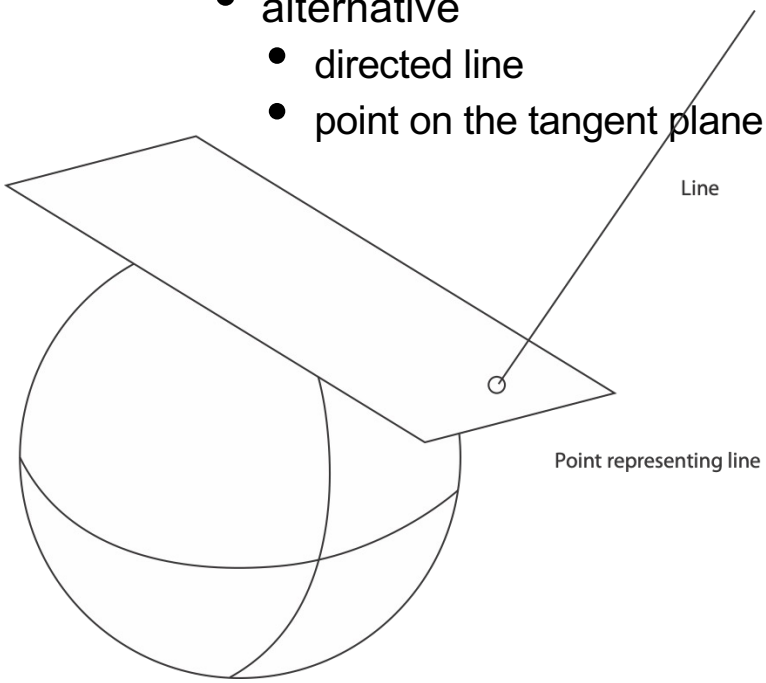


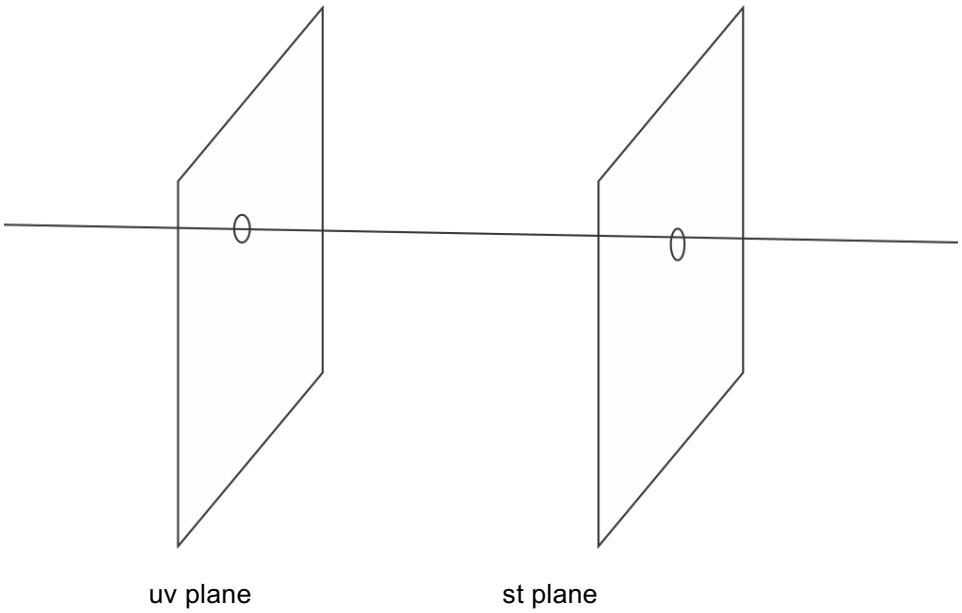
Fig. 1. Maximal free segment. (a) All the rays collinear to r whose origin is between the two spheres "see" point B. (b) These rays are grouped into a *maximal free segment* S. Two other maximal free segments S' and S'' are collinear to S.

Durand et al 02

Lines in 3D (if it's empty!)

- Space of lines is 4 dimensional
  - can specify a line by:
    - where it intersects each of two planes
      - some missing lines, some details
  - alternative
    - directed line
    - point on the tangent plane of sphere





Lines in 3D with object can be nasty

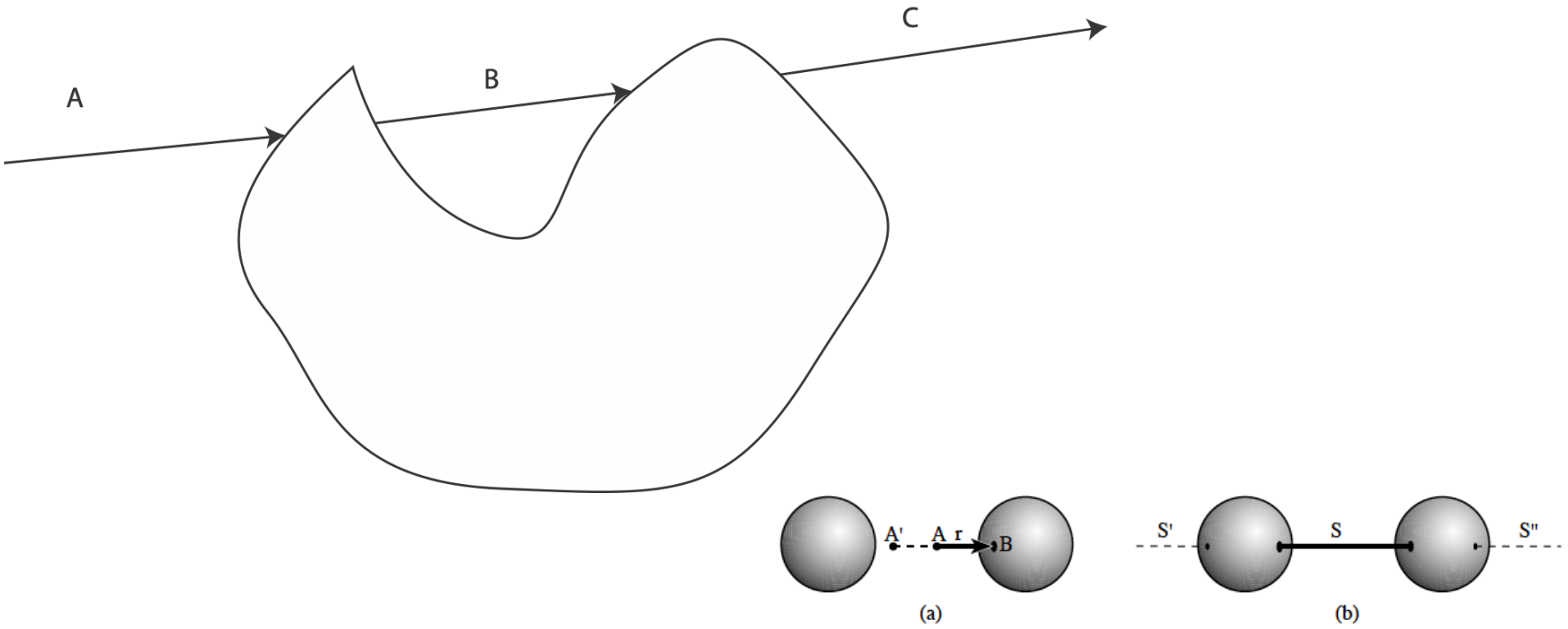
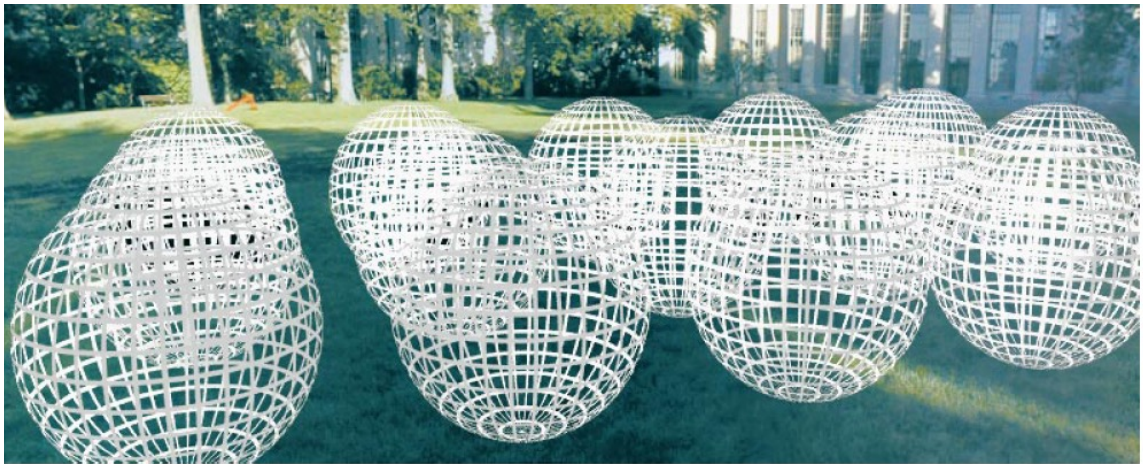


Fig. 1. Maximal free segment. (a) All the rays collinear to r whose origin is between the two spheres "see" point B. (b) These rays are grouped into a *maximal free segment* S. Two other maximal free segments S' and S'' are collinear to S.

Durand et al 02

The plenoptic function: More practical version



$$L(\theta, \phi, x, y, z) = (r, g, b)$$

- Other simplifications/variants are possible, as we will see

Modeling the plenoptic function

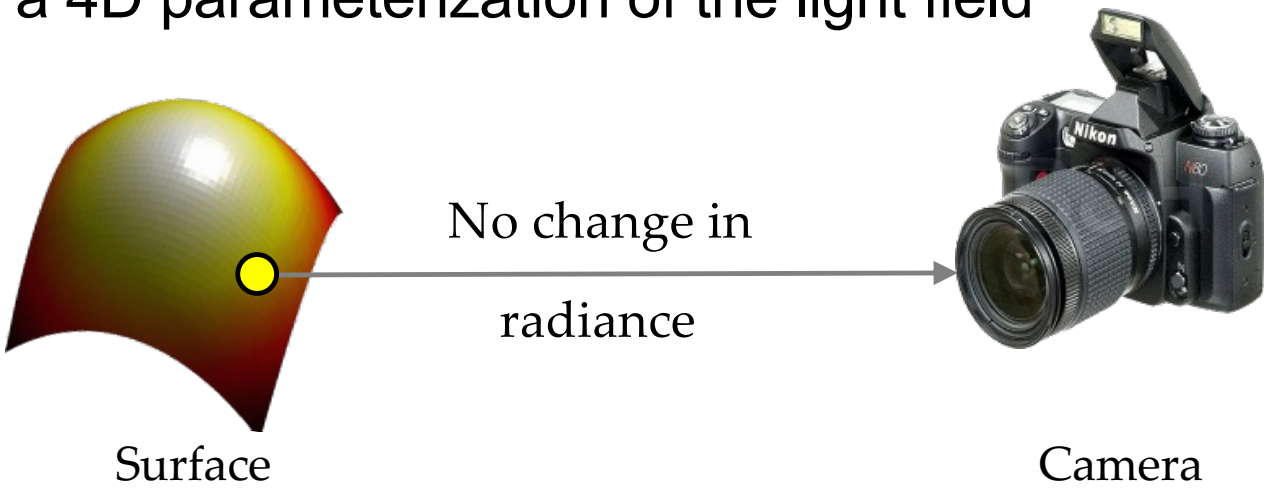
- Capture
  - Create a special camera setup to capture a slice of the plenoptic function
  - Combine captured rays for novel view synthesis, defocus, and other effects
- Optimization
  - Given a set of multi-view calibrated images, optimize a parametric representation of the plenoptic function of the scene

Outline

- The plenoptic function
- Two-plane light fields

Two-plane light fields

- Key idea: assuming light is constant along rays, we can create a 4D parameterization of the light field



If there is no occlusion or fog

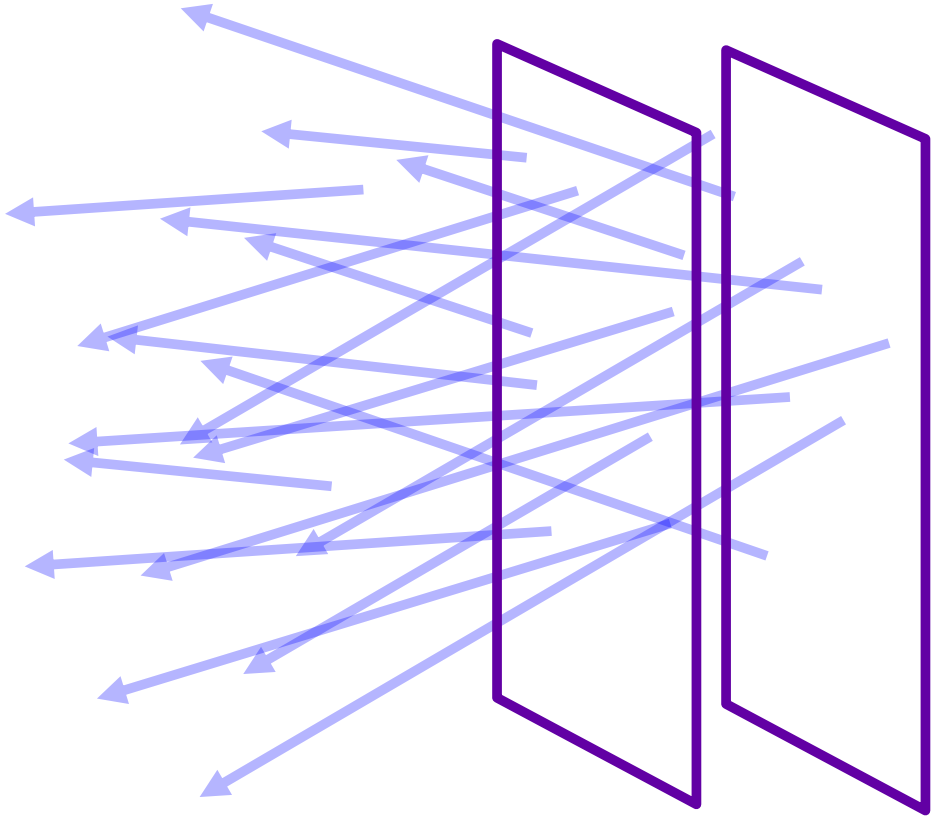
S. Gortler, R. Grzeszczuk, S. Szeliski, M. Cohen. The Lumigraph. Proceedings of the 23rd Annual Conference on Computer Graphics and Interactive Techniques, 1996

M. Levoy and P. Hanrahan. Light field rendering. SIGGRAPH 1996

Two-plane light fields

- Two-plane parameterization:

Observer

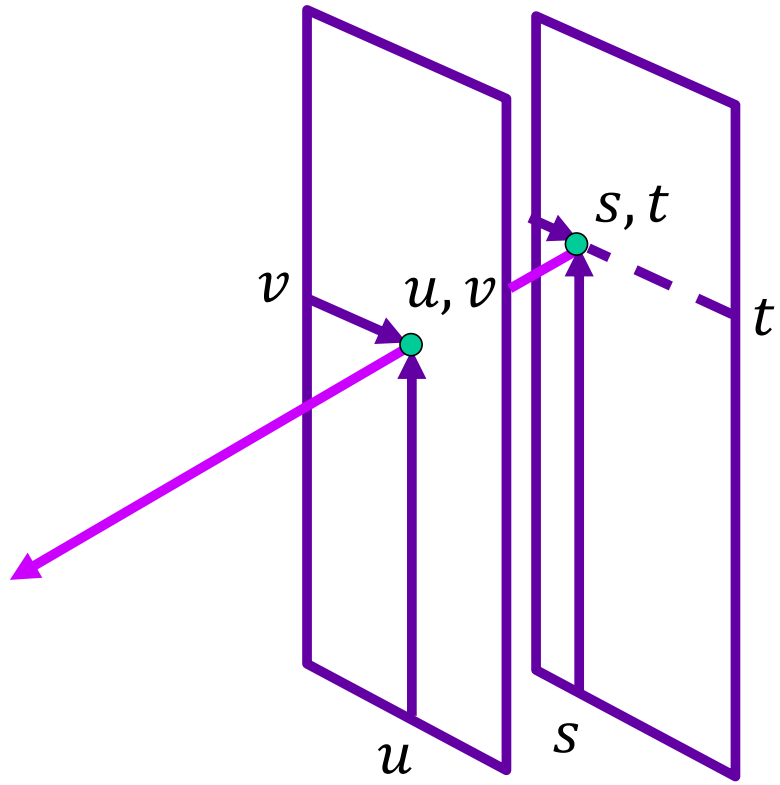


Scene

Two-plane light fields

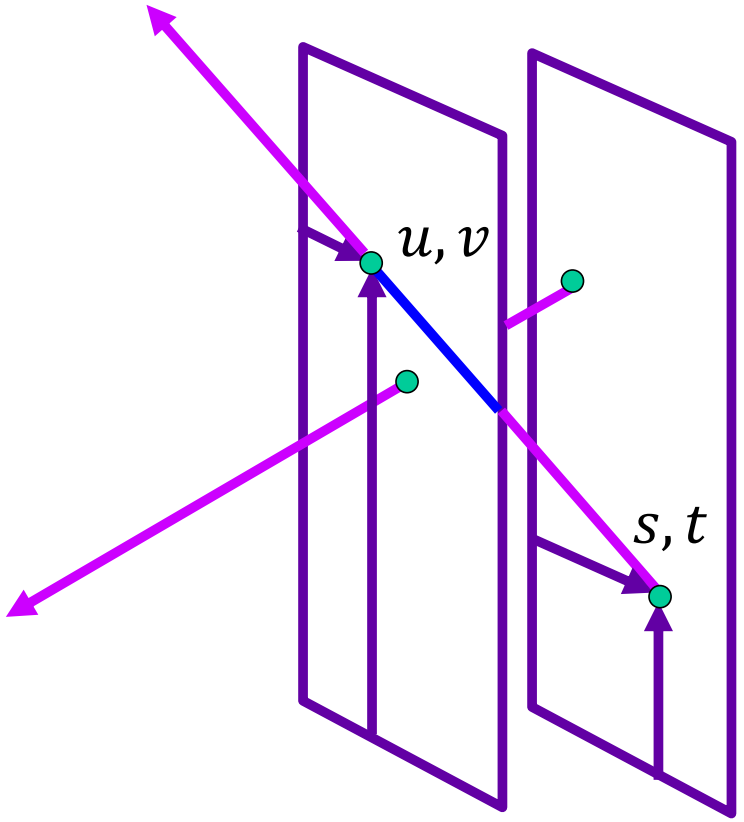
- Two-plane parameterization:

$$L(s,t,u,v) = (r,g,b)$$



Two-plane light fields

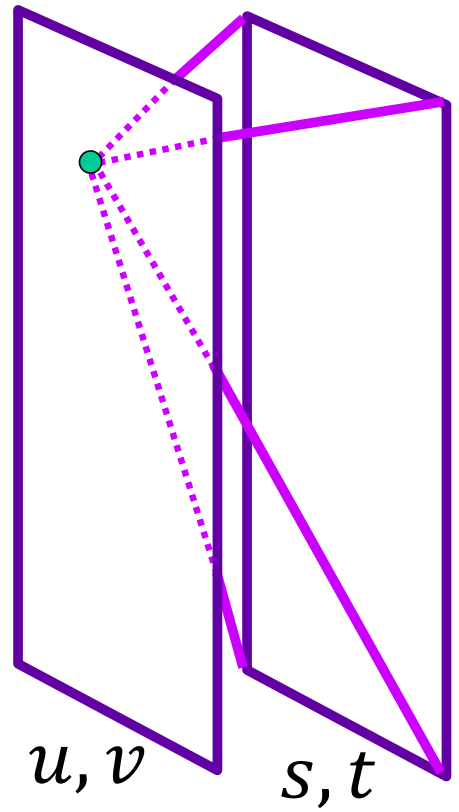
- Two-plane parameterization:



$L(s,t,u,v) = (r,g,b)$

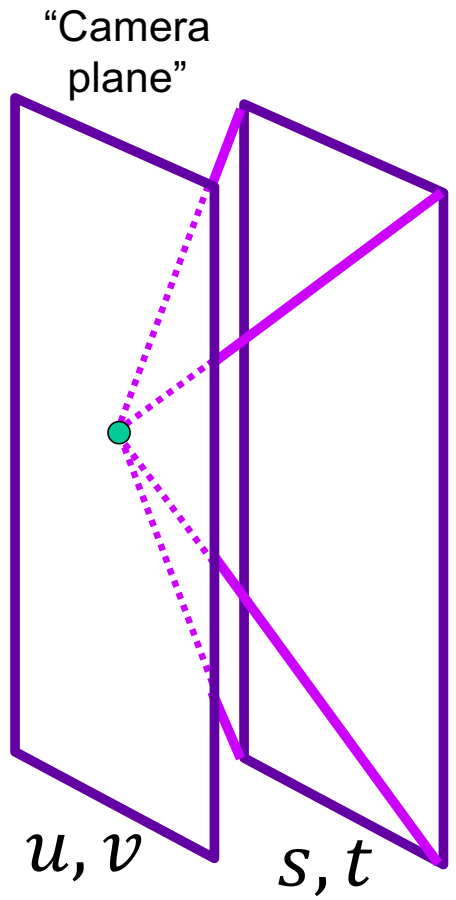
Two-plane light fields

- What do we get if we hold u, v constant and let s, t vary?
- An image!



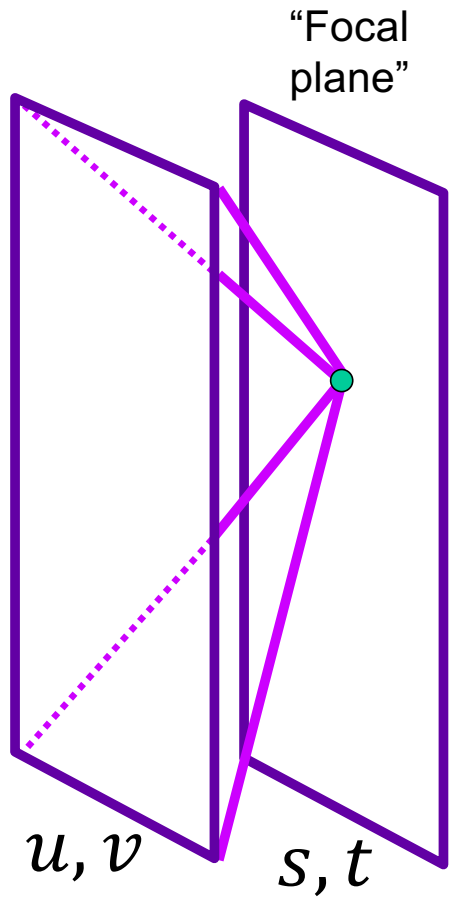
Two-plane light fields

- What do we get if we hold u, v constant and let s, t vary?
- An image!



Two-plane light fields

- What do we get if we hold s, t constant and let u, v vary?
- A set of rays leaving a point in the scene in a bundle of directions towards the image plane



Light field visualization

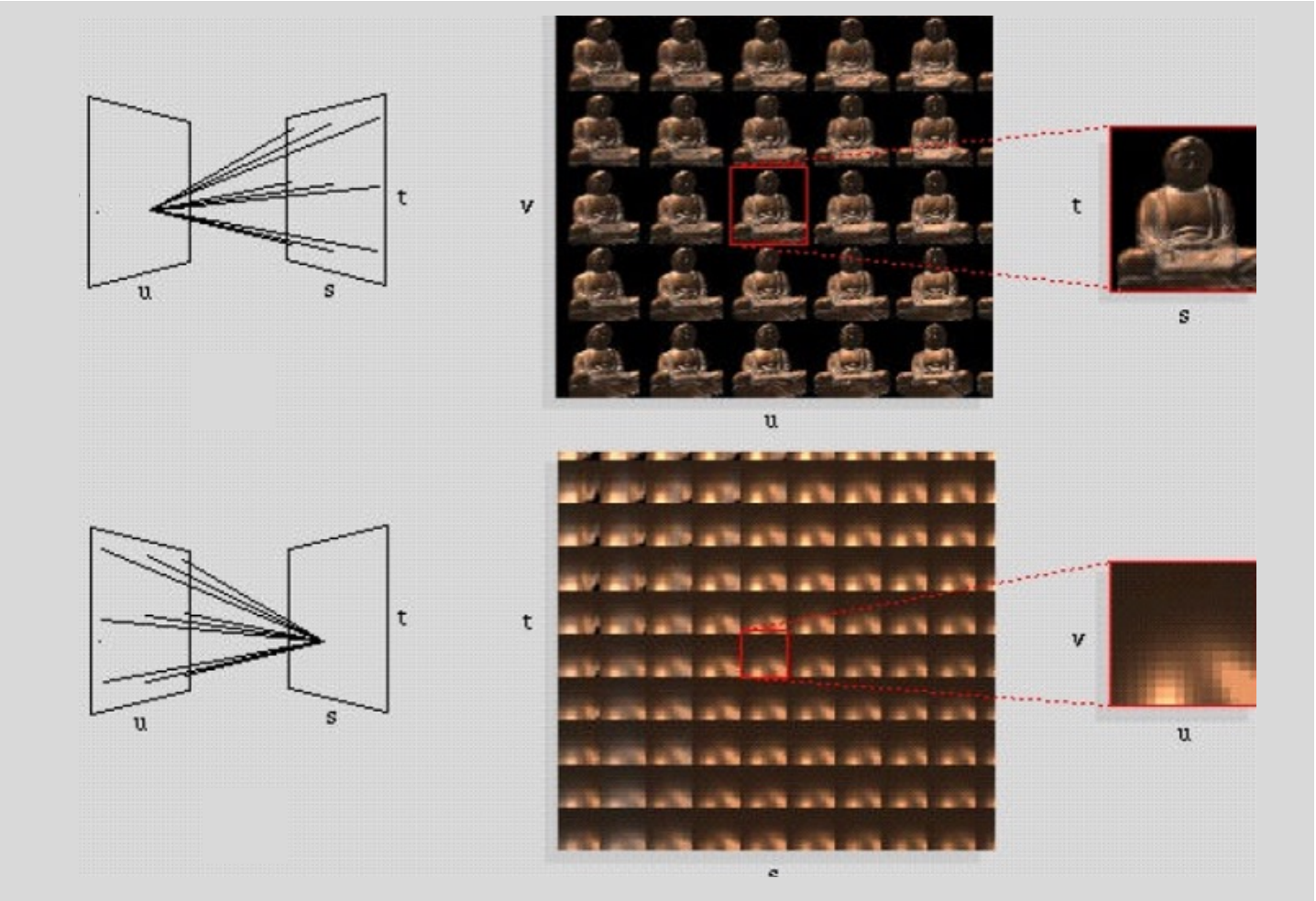
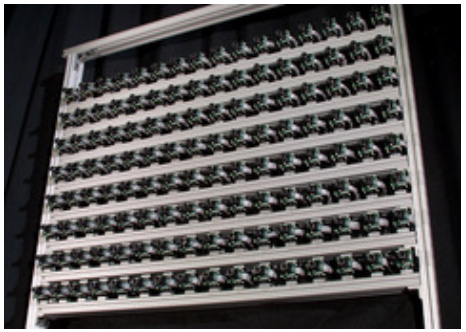
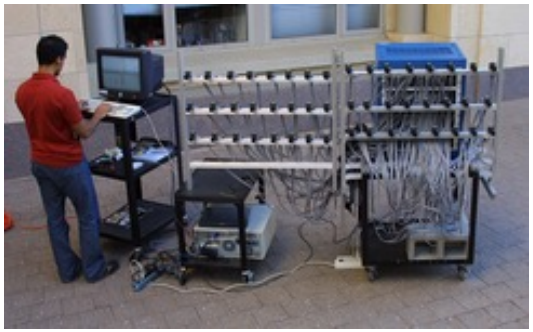


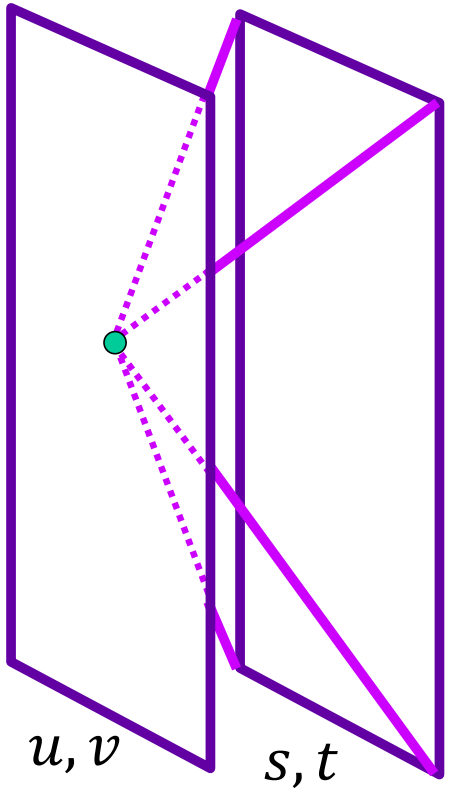
Figure source: M. Levoy and P. Hanrahan

Light field capture

- Idea 1: move camera carefully over u, v plane

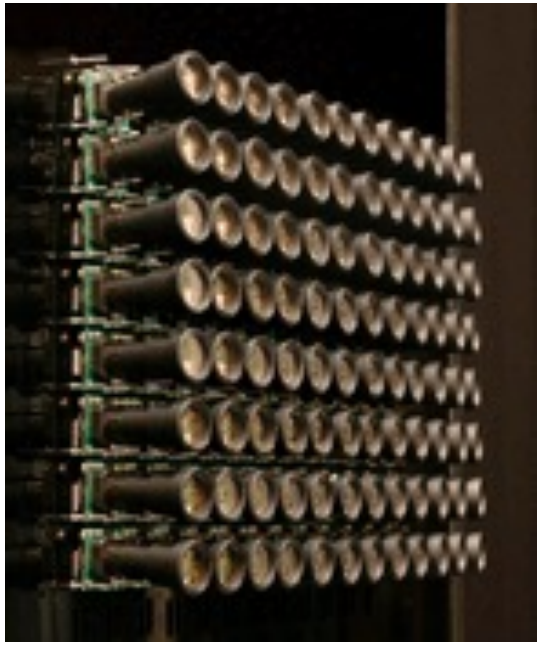


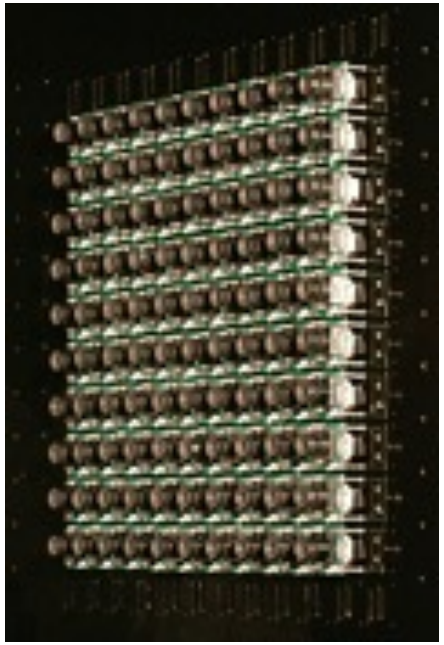




Stanford multi-camera array

- 640 × 480 pixels × 30 fps × 128 cameras
- Synchronized timing
- Continuous streaming
- Flexible arrangement

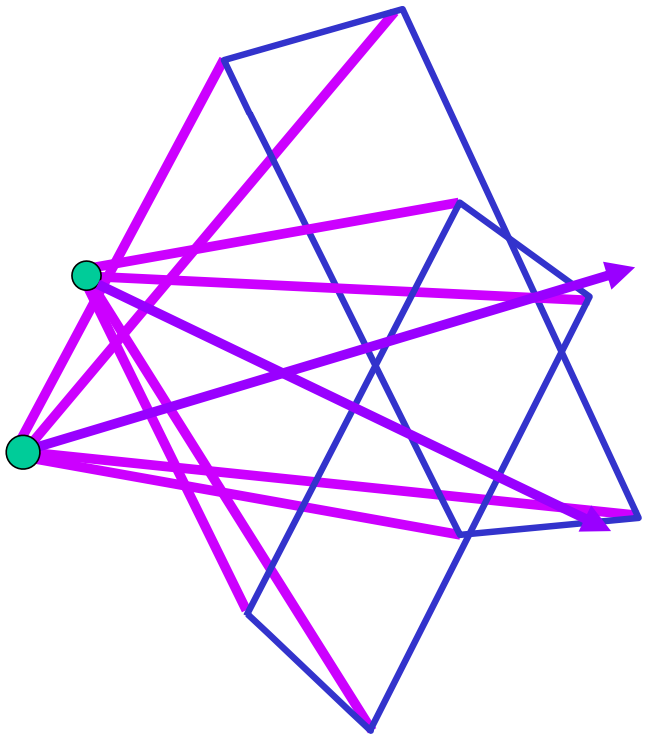




http://graphics.stanford.edu/projects/array/

Light field capture

- Idea 2: move camera anywhere, use rebinning or resampling



Light field capture

- Idea 2: move camera anywhere, use rebinning or resampling

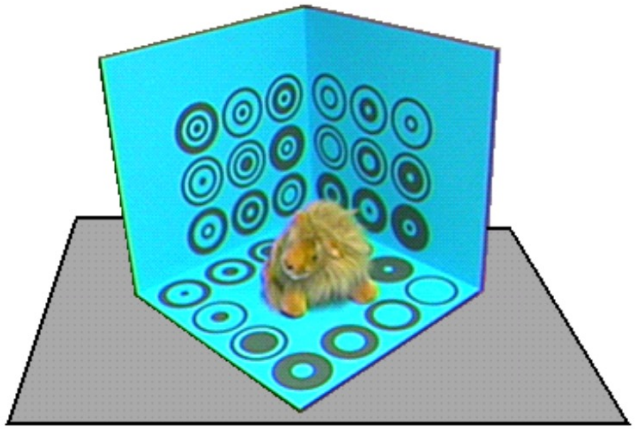
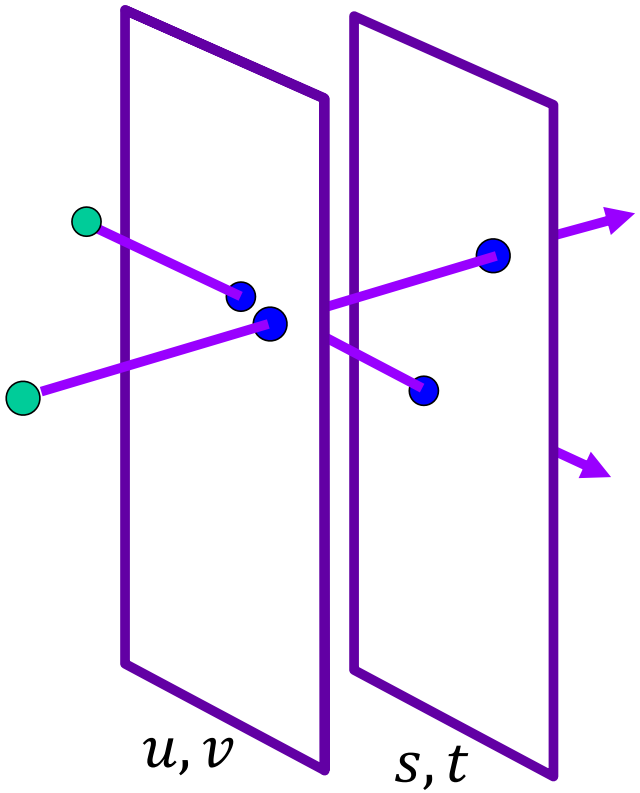


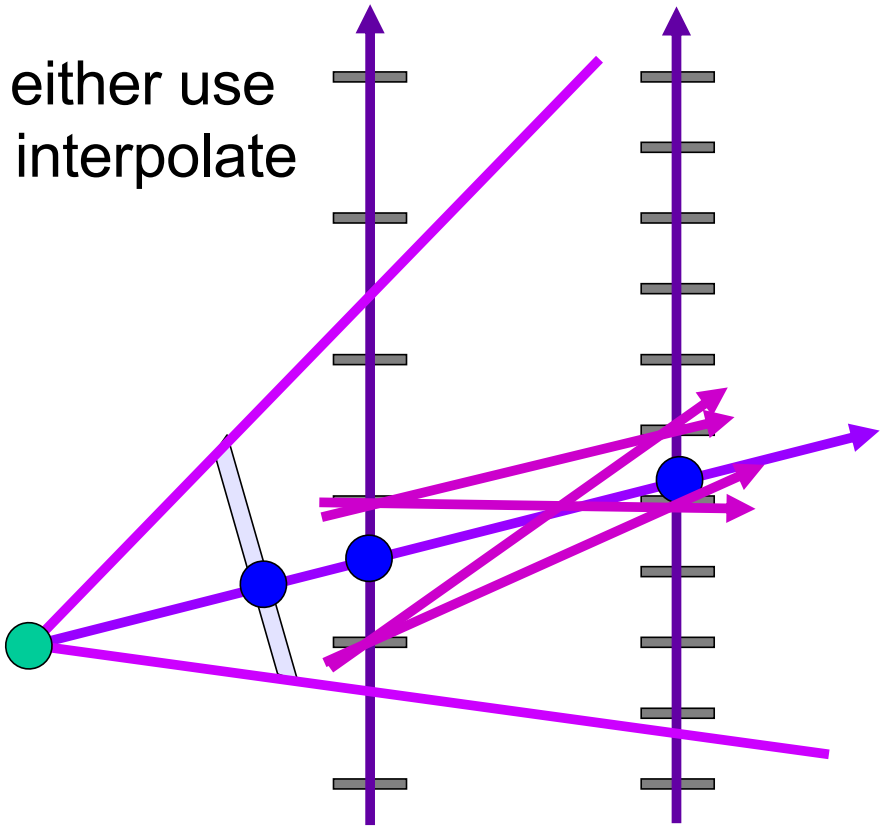
Figure 10: The capture stage

Figure source: S. Gortler et al.



Novel view synthesis

- For each output pixel, determine s, t, u, v, then either use closest discrete RGB or interpolate several nearby values



Slide by Rick Szeliski and Michael Cohen

Features of a light field

In principle, you can

- view object from any direction
- simulate lens effects
    - change depth of field
    - change focal plane
    - simulate odd lenses

Renderings aren’t that great …

Some issues with this story…

Direction of the line

Sampling

Size of the representation

Getting close

Another way to get a light field

Predict from a single image

Fairly obviously, there are limits to how well this can work!

Srinivasan et al, 2017

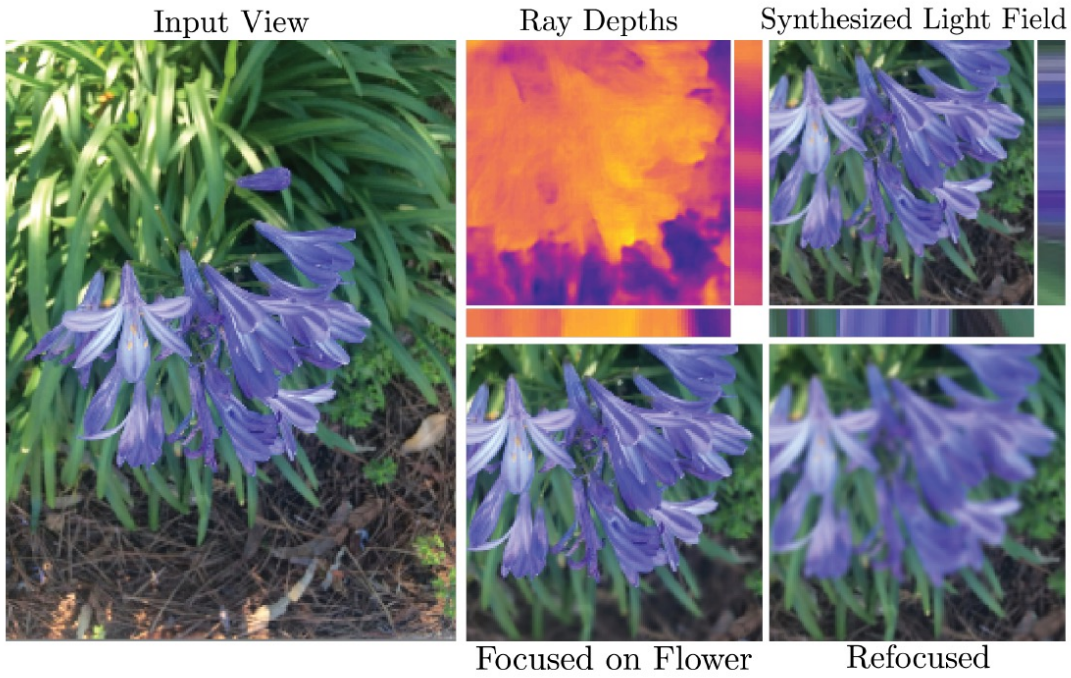


Figure 10. Our pipeline applied to cell phone photographs. We demonstrate that our network can generalize to synthesize light fields from pictures taken with an iPhone 5s. We synthesize realistic depth variations and occlusions, as shown in the epipolar slices. Furthermore, we can synthetically increase the iPhone aperture size and refocus the full-aperture image.

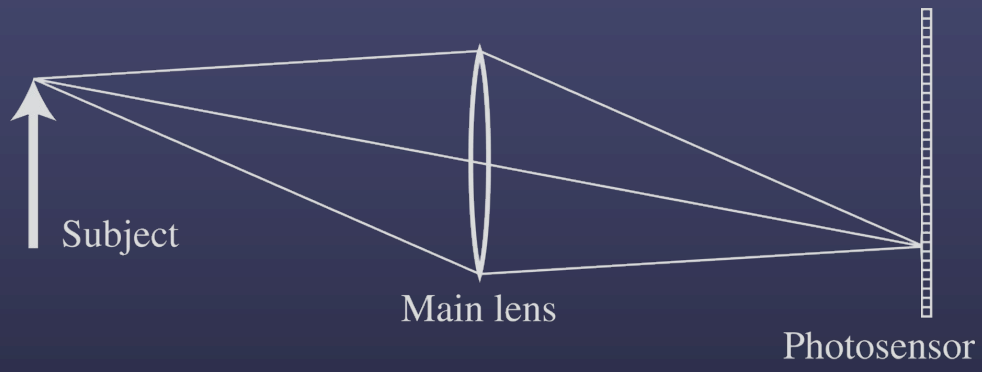
Outline

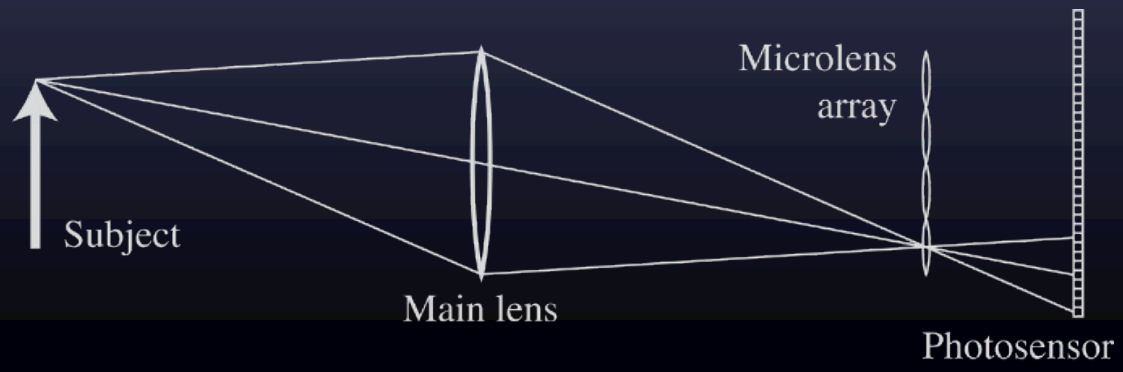
- The plenoptic function
- Two-plane light fields
- Plenoptic camera

Plenoptic camera

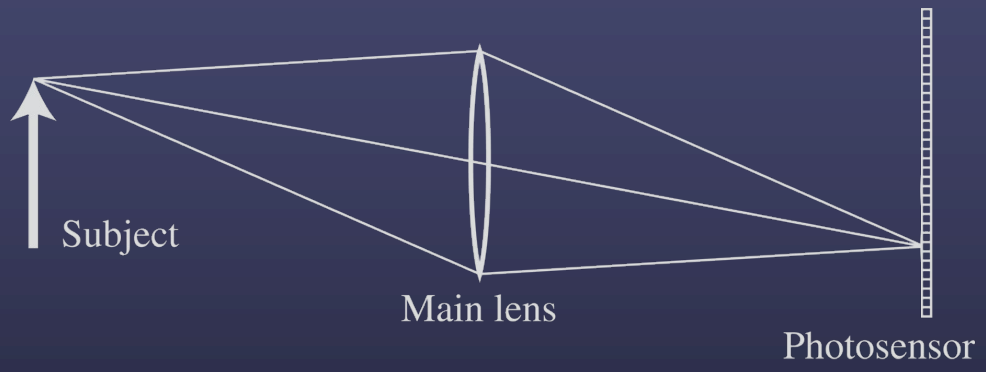
R. Ng et al. Light Field Photography with a Hand-held Plenoptic Camera. 2005

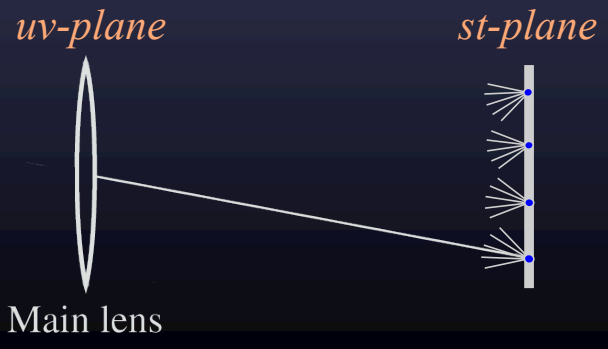
Conventional vs. light field camera





Conventional vs. light field camera

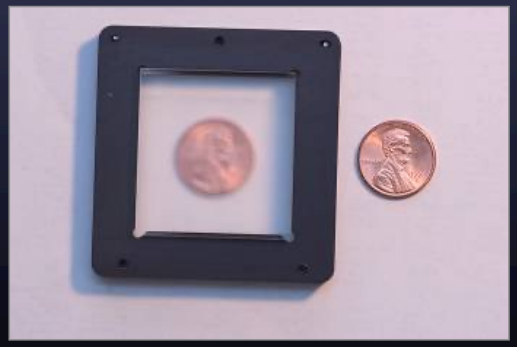




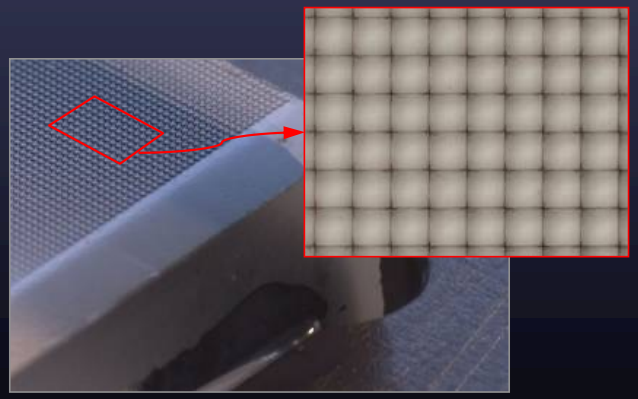
Prototype camera

Contax medium format camera

Kodak 16-megapixel sensor



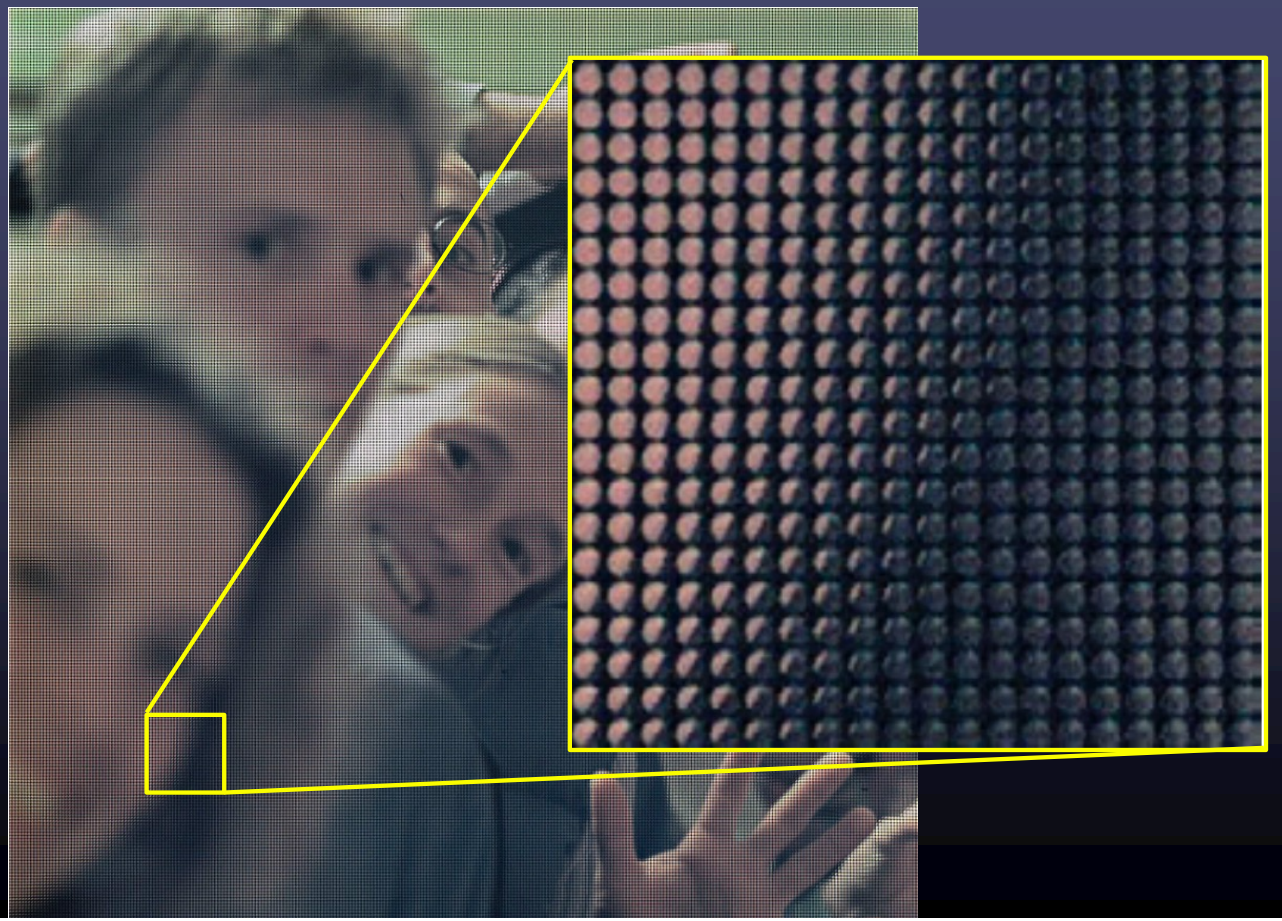
Adaptive Optics microlens array



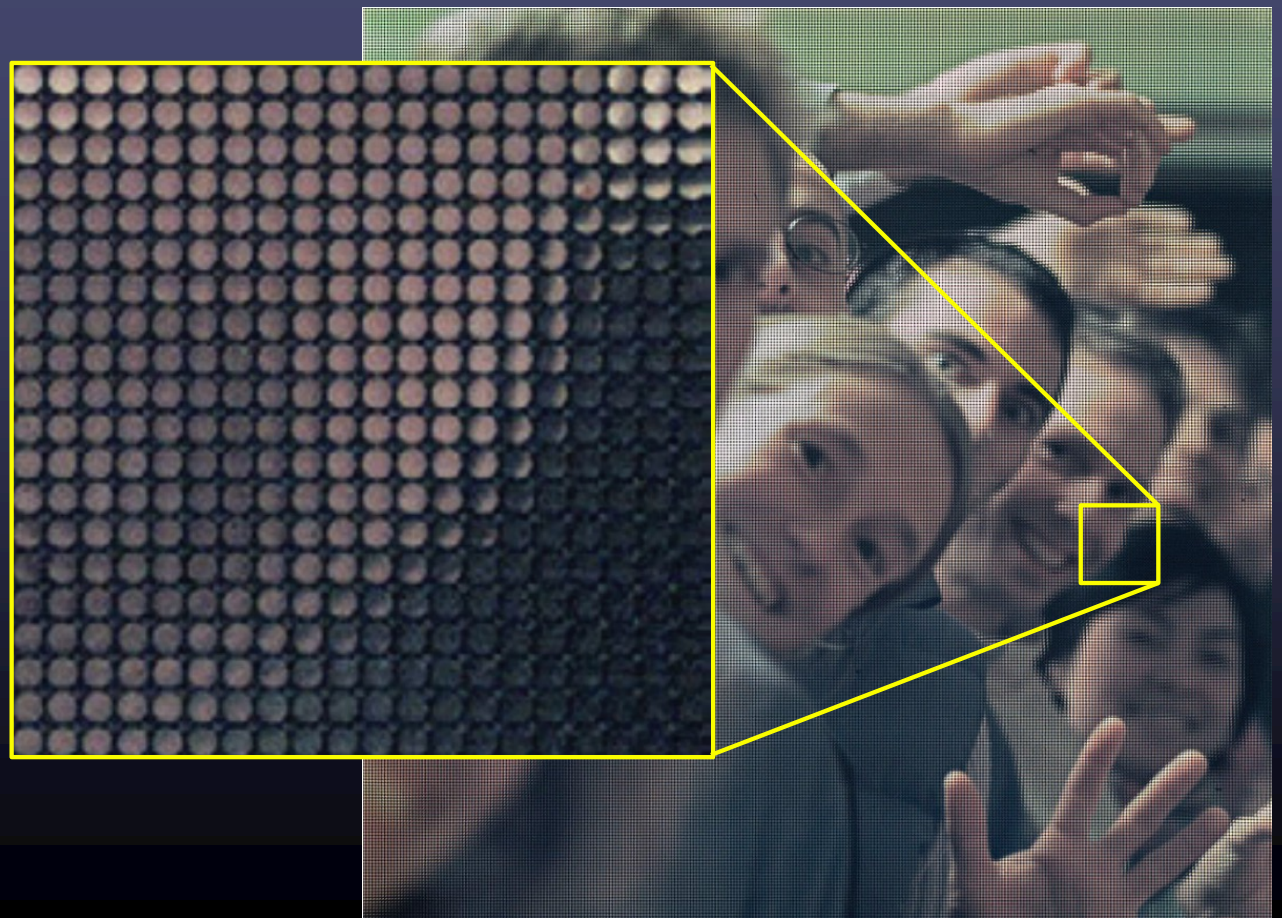
125µ square-sided microlenses

4000 × 4000 pixels /
292 × 292 lenses =
14 × 14 pixels per lens

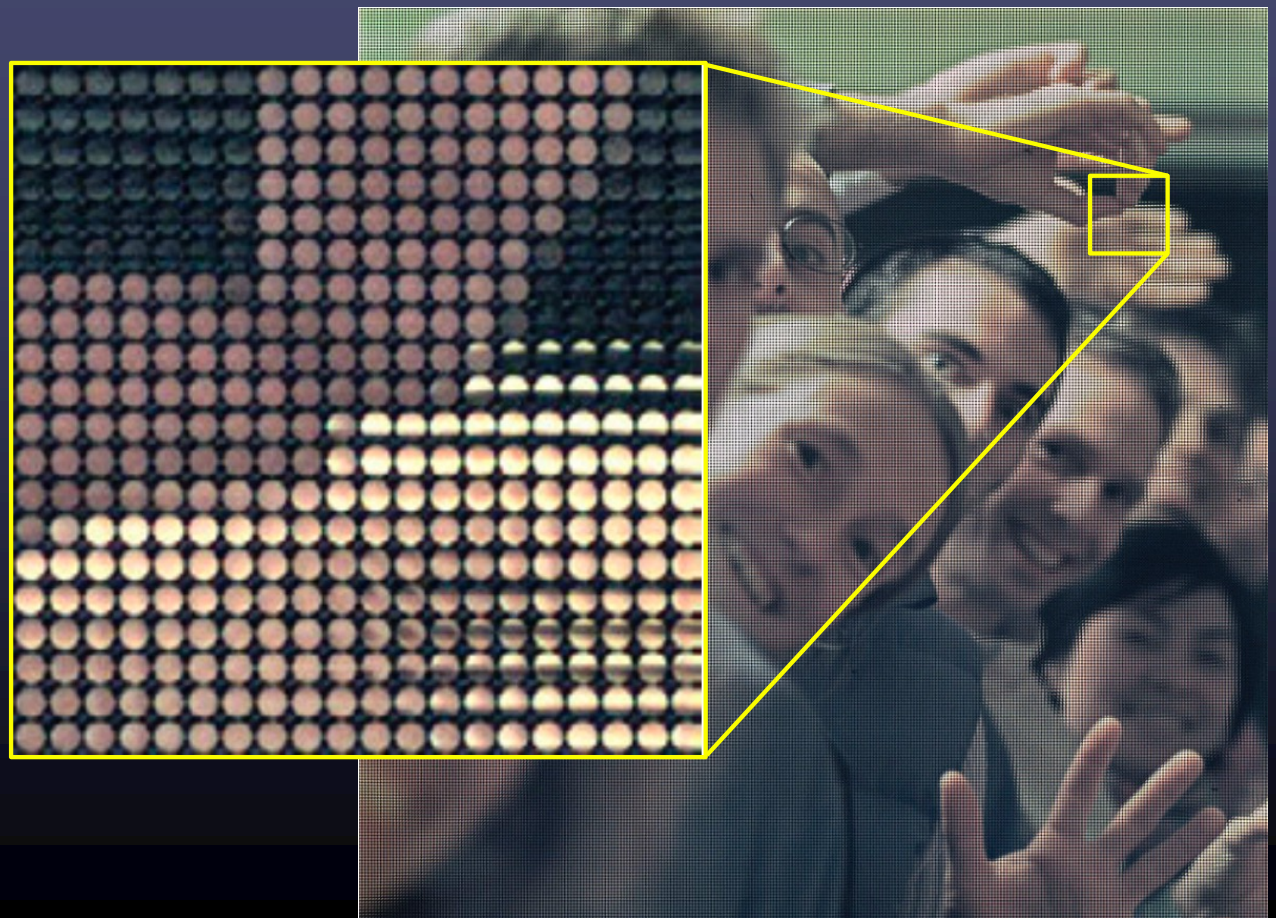
Captured light field



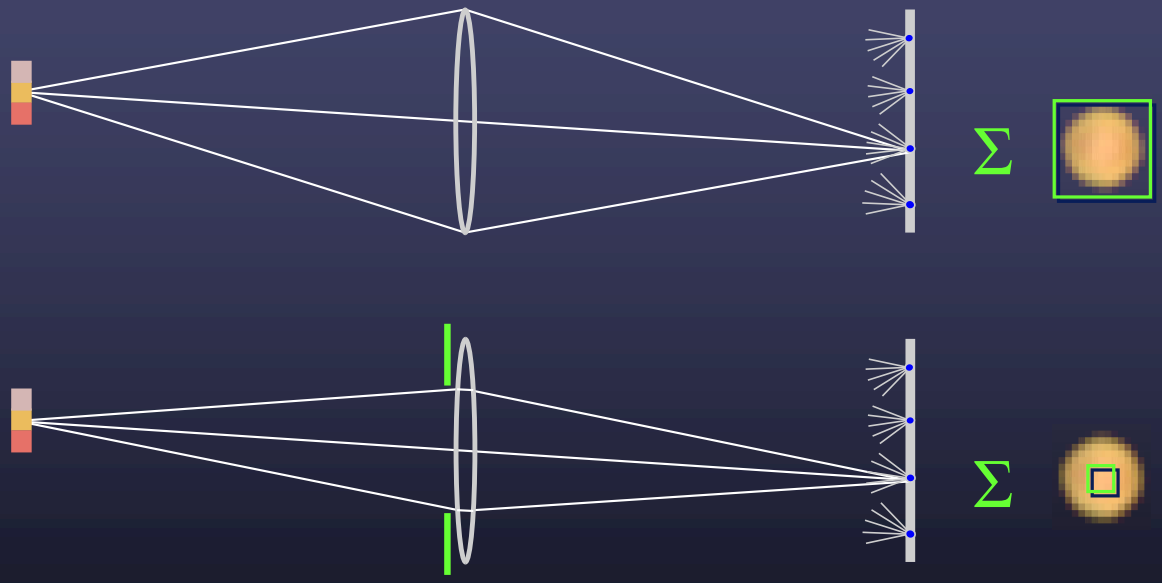
Captured light field



Captured light field

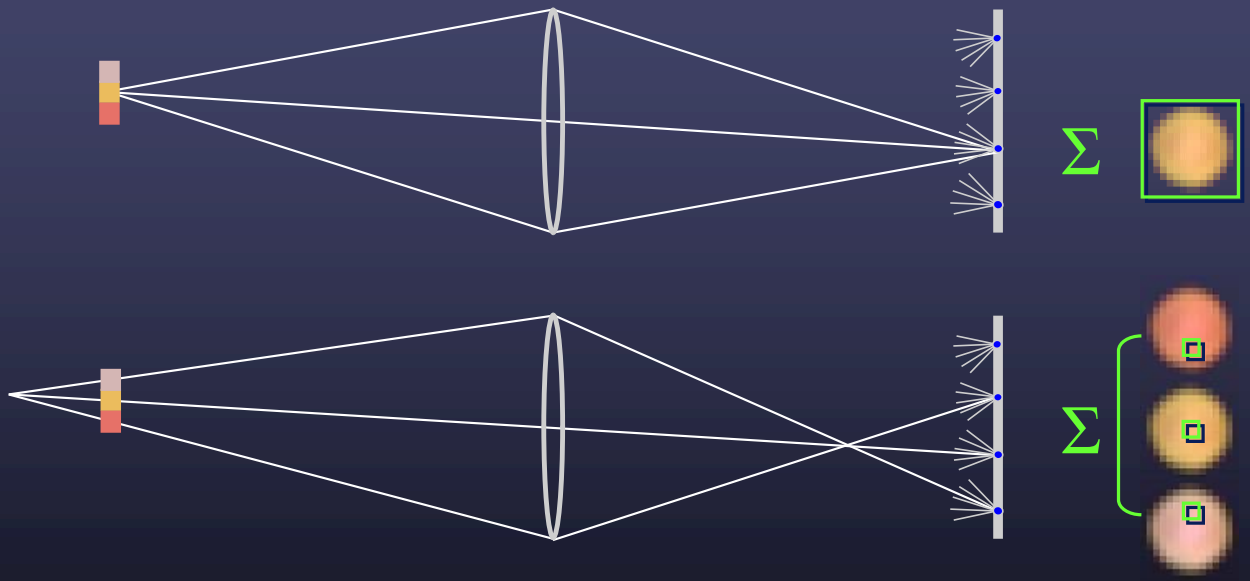


Digitally stopping down (reducing the aperture)



- stopping down = summing only the central portion of each microlens

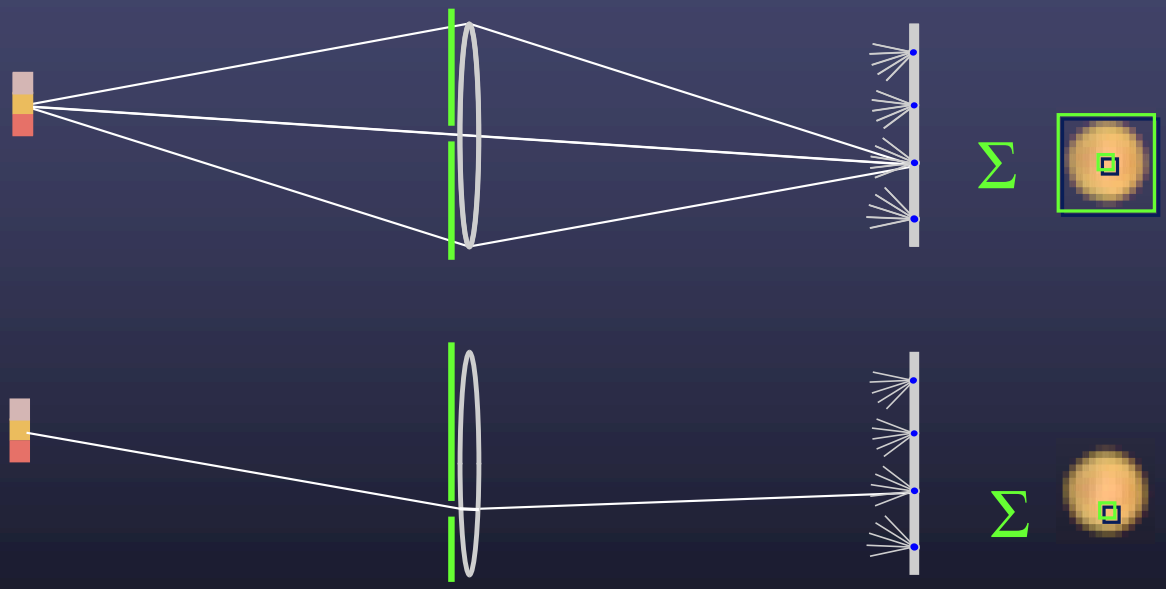
Digital refocusing



- refocusing = summing windows extracted from several microlenses

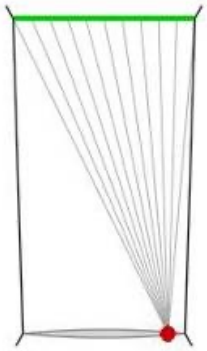
Digital refocusing

Digitally moving the observer

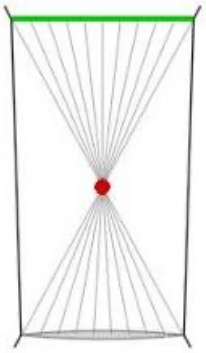


- moving the observer = moving the window we extract from the microlenses

Digitally moving the observer



Digitally moving the observer



Lytro (RIP)

https://en.wikipedia.org/wiki/Lytro

What happened to Lytro?

Outline

- The plenoptic function
- Two-plane light fields
- Plenoptic camera
- Neural radiance fields (NeRFs)

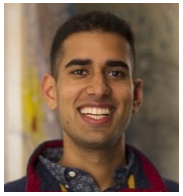
NeRF: Representing Scenes as Neural Radiance Fields for View Synthesis

ECCV 2020 (best paper honorable mention)

Ben Mildenhall*

UC Berkeley

Pratul Srinivasan*



UC Berkeley

Google

Matt Tancik*

UC Berkeley

Jon Barron

Google Research

Google

Ravi Ramamoorthi

UC San Diego

UC San Diego

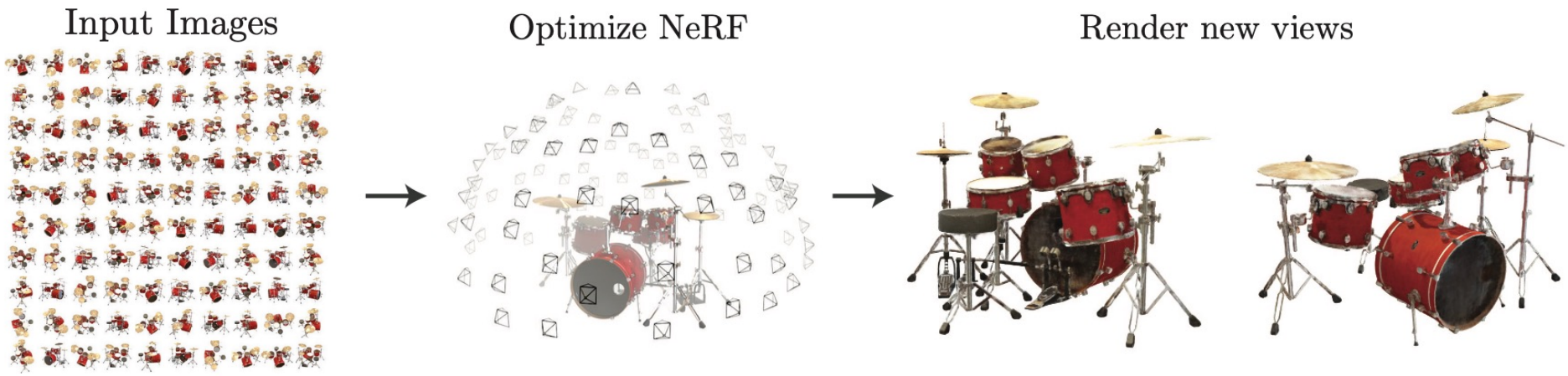
Ren Ng

UC Berkeley

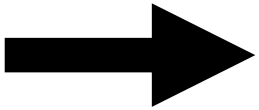
https://www.matthewtancik.com/nerf

NeRF: Representing Scenes as Neural Radiance Fields for View Synthesis

ECCV 2020 (best paper honorable mention)



Train a neural network to represent the plenoptic function



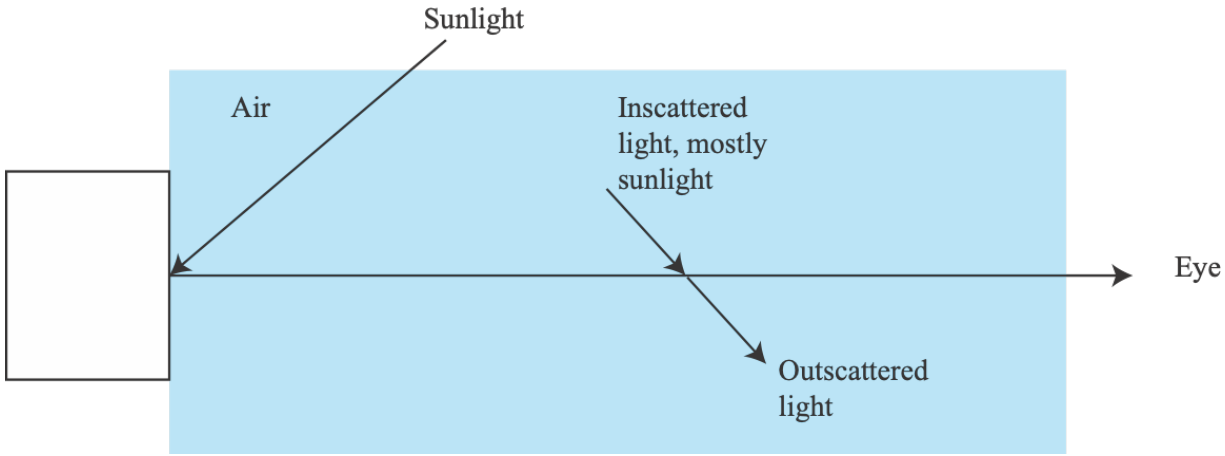
Inputs: sparsely sampled images of scene

Outputs: *new* views of same scene

tancik.com/nerf

Slide credit: Jon Barron

Scattering


Sunlight
Air
Inscattered
light, mostly
sunlight
Eye
Outscattered
light

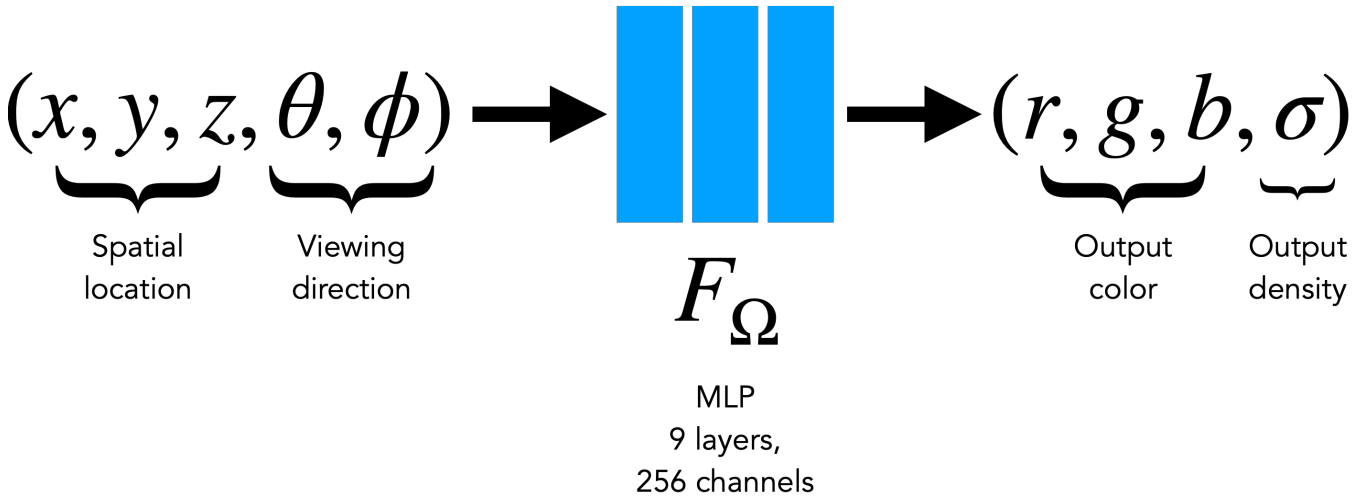
Key idea

- Represent an object as a field of scatterers
  - Adjust the scattering properties
    - so that object produces images that look like training images

- Crucial strengths
  - Very good smoothing of the plenoptic function
  - You don't have to get correspondences right
  - You don't have to work with meshes, etc.

- Difficulty
  - You have to do nasty integrals

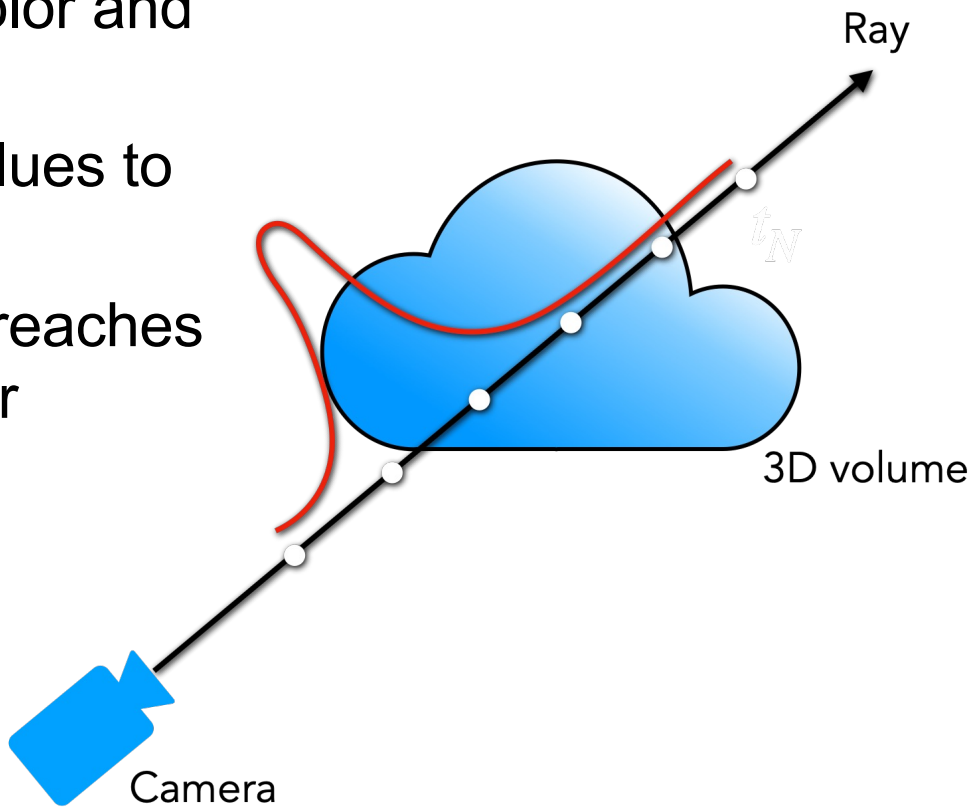
Neural radiance field



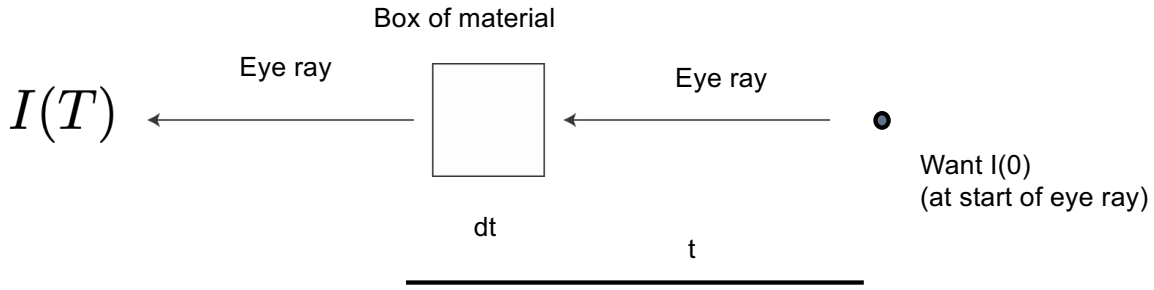
Volumetric “fog” model: Every 5D input gets mapped to **Color** and **Density**

NeRF rendering

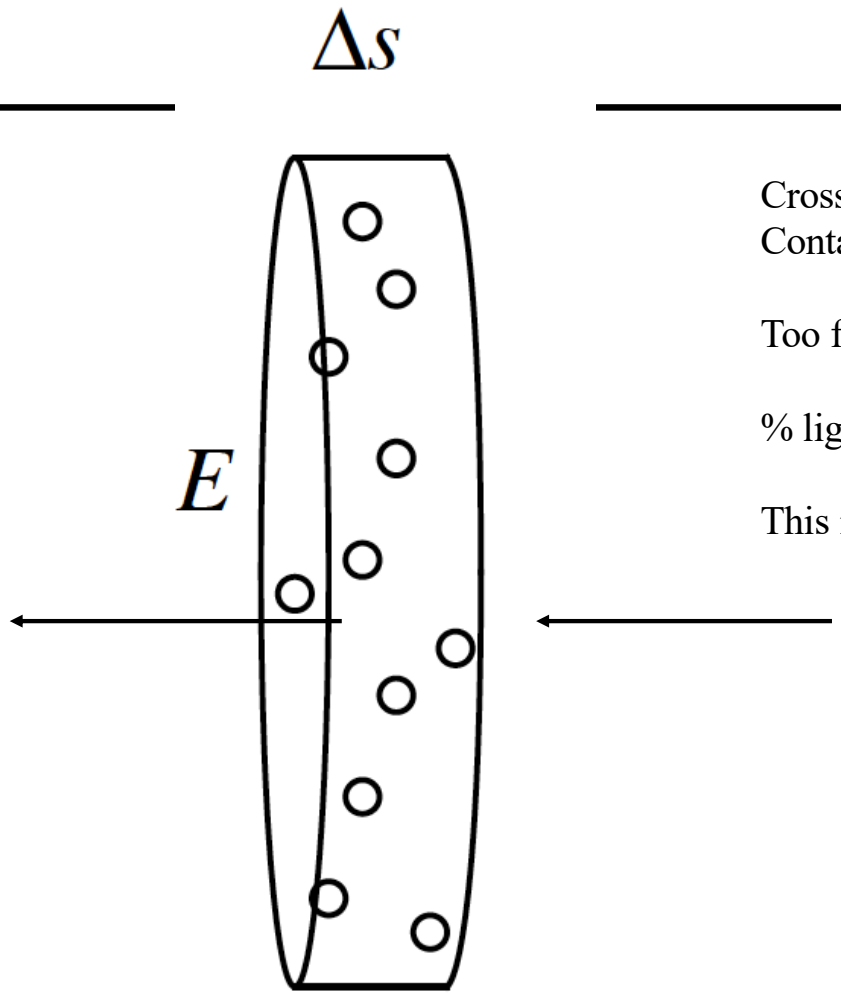
- At every point you know color and density: (c_i, σ_i)
- Need to integrate these values to render a pixel
- Idea: sum how much light reaches each point * visibility * color



Simplest scattering model: Absorption



- Ignore in-scattering
  - only account for forward scattering
- Assume there is a source at t=T
  - of intensity I(T)
  - what do we see at t=0?



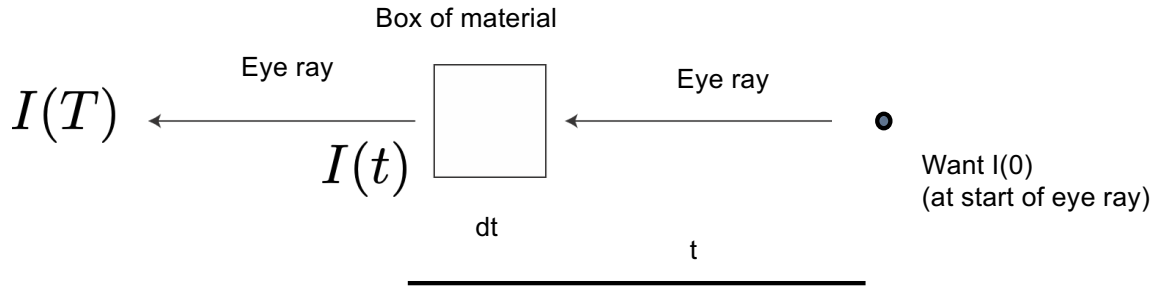
Cross sectional area of "slab" is E
Contains particles, radius r, density rho

Too few to overlap when projected

% light absorbed = (area of projected particles)/(area of slab)

This is:

$$\frac{(\rho E \Delta s)\pi r^2}{E} = \sigma(s)\Delta s$$



$$I(t-\delta t) = I(t) - \sigma(t)I(t)\delta(t)$$

Extinction coefficient

$$\frac{dI}{dt} = \sigma(t)I(t)$$

$$\frac{d\log I}{dt} = \sigma(t)$$

$$I(T) = I(0)e^{\int_0^T \sigma(t)dt}$$

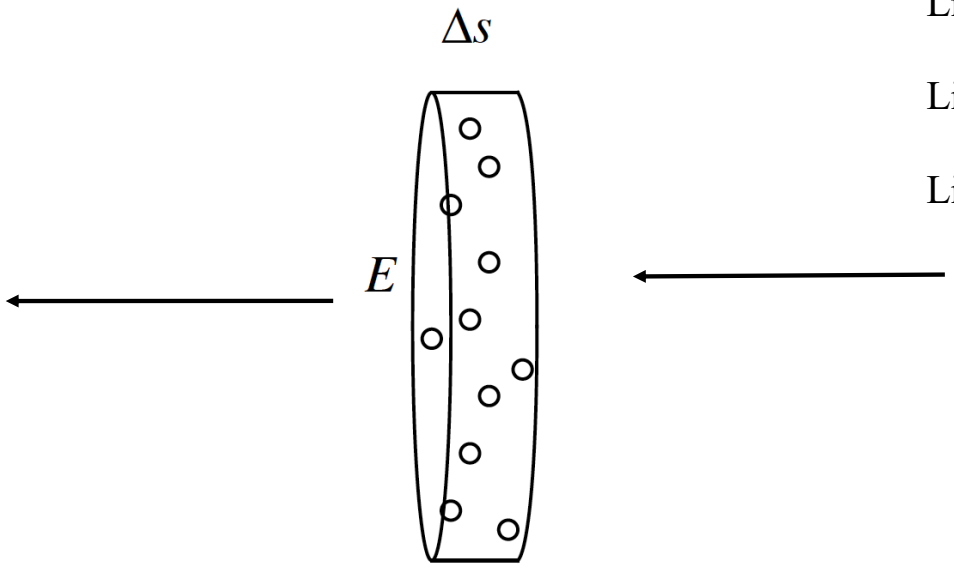
$$I(0) = I(T)e^{-\int_0^T \sigma(t)dt}$$

Eye is at 0

Intensity at T

More interesting scattering model

- Intensity is “created along the ray”
  - by (say) airlight
  - Model - the particles glow with intensity C(x)



Cross sectional area of “slab” is E
Contains particles, radius r, density rho

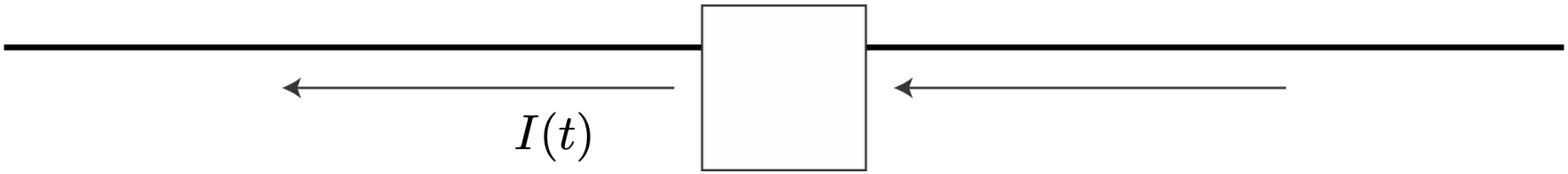
Too few to overlap when projected

Light out = Light in - Light absorbed+Light generated

Light generated: C x (area fraction of proj. particles)

Light generated is

$$C(\mathbf{x}(s))\frac{(\rho E \Delta s)\pi r^2}{E} = C(\mathbf{x}(s))\sigma(s)\Delta s$$



$$I(t-\delta t) = I(t) - \sigma(t)I(t)\delta t + \mathbf{c}(\mathbf{x}(t))\sigma(t)\delta t$$

Absorption

Generation

$$I(0) = \int_0^T \mathbf{c}(\mathbf{x}(s))\sigma(s)e^{-\int_0^s \sigma(u)du} ds$$

$$I(0) = \int_0^T \underbrace{\mathbf{c}(\mathbf{x}(s))\sigma(s)}_{\text{Made at s}} \underbrace{e^{-\int_0^s \sigma(u)du}}_{\substack{\text{Absorbed in transit} \\ \text{from s to 0}}} ds$$

Accumulate along ray

Intensity we see at eye:

Choose this to get pictures right:

$$I(0) = \int_0^T \mathbf{c}(\mathbf{x}(s))\sigma(s)e^{-\int_0^s \sigma(u)du} ds$$

Made at s

Absorbed in transit from s to 0

Accumulate along ray

How to render a pixel: Volume rendering

Given: a ray $\mathbf{r}(i) = \vec{o} + i\vec{d}$ At every point you know: (c_i, σ_i)

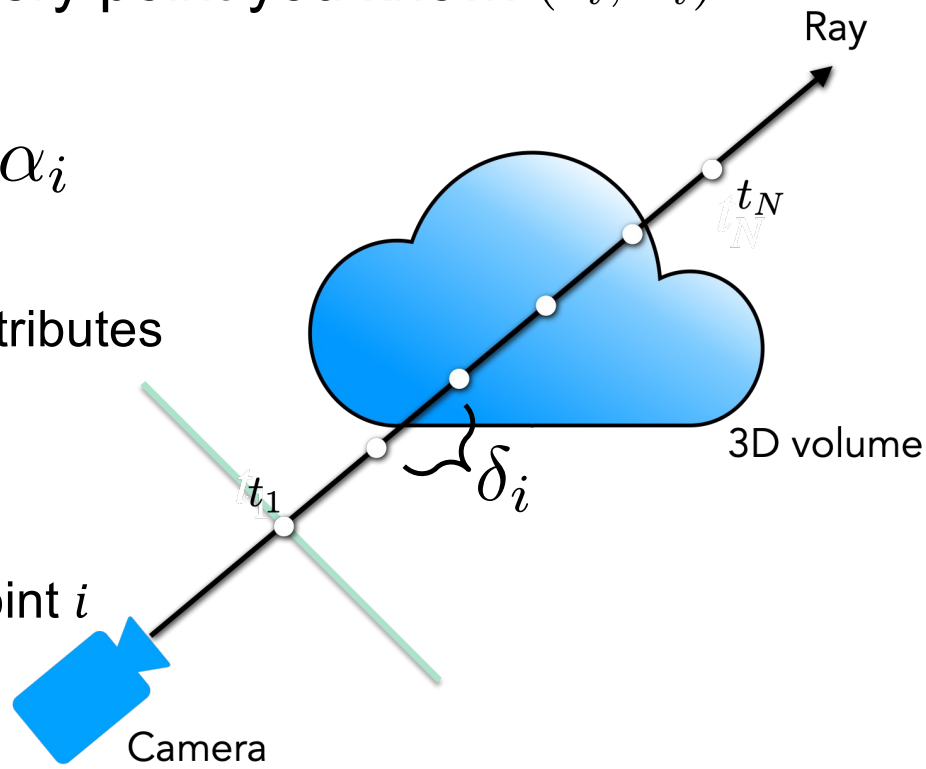
$$C(\mathbf{r}) \approx \sum_{i}^{N} w_i c_i \qquad w_i = T_i \alpha_i$$

Alpha: How much light a ray segment contributes

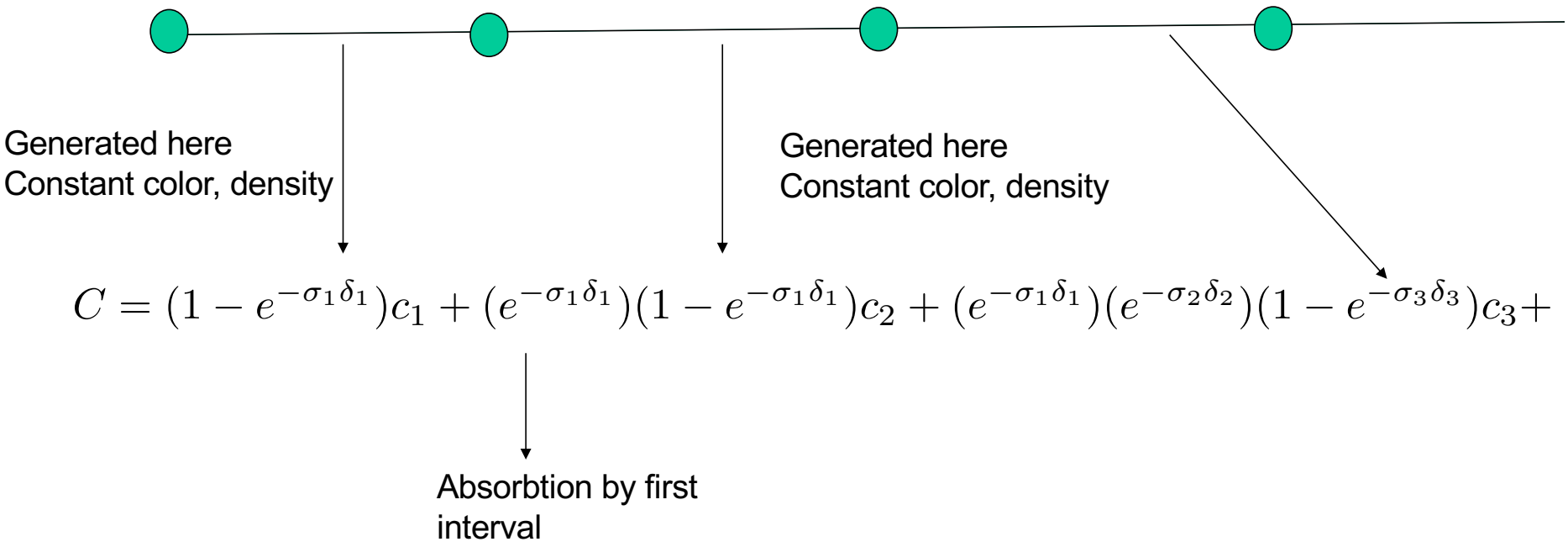
$$\alpha_i = 1 - \exp(-\sigma_i \delta_i)$$

Transmittance: how much light reaches point i

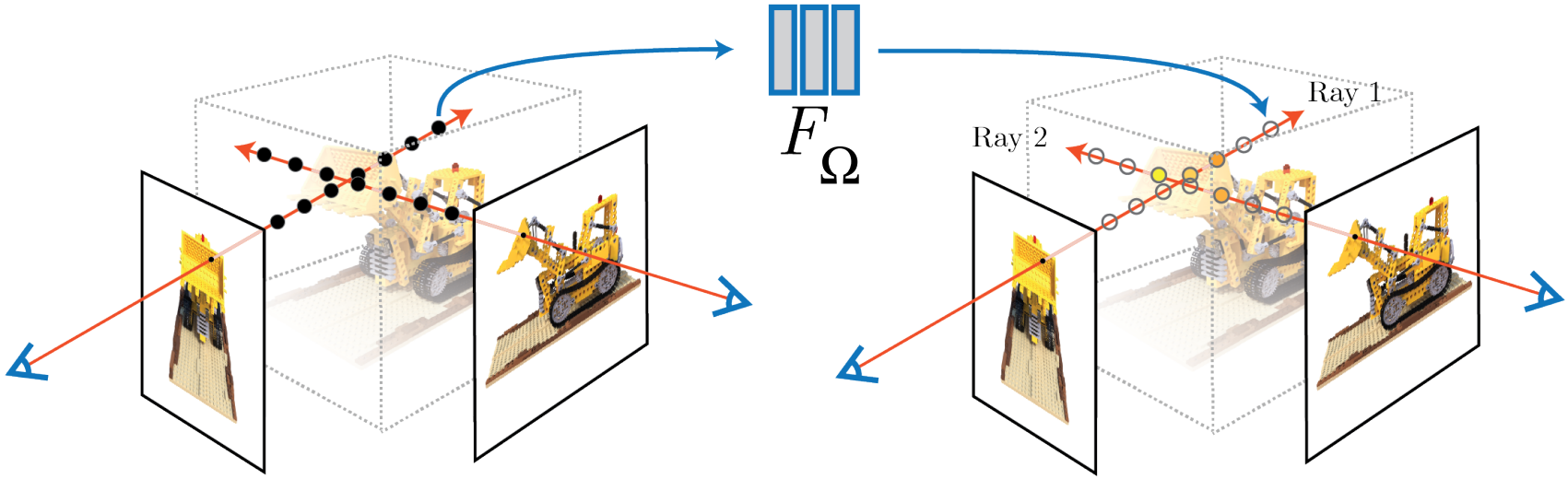
$$T_i = \prod_{j=1}^{i-1} (1 - \alpha_j)$$



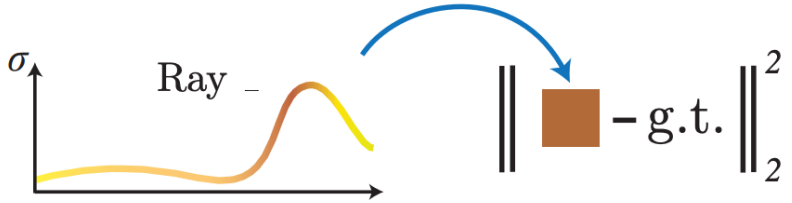
Expand to get



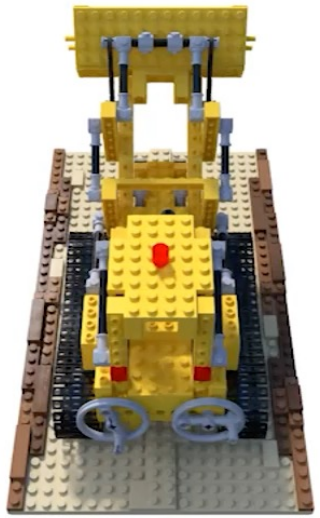
Training: Optimization with reconstruction loss



$$\min_{\Omega} \sum_{i} \|\text{render}^{(i)}(F_\Omega) - I_{\text{gt}}^{(i)}\|^2$$



Example results



Viewpoint-dependent effects

Viewpoint-dependent effects

Rendering expected depth

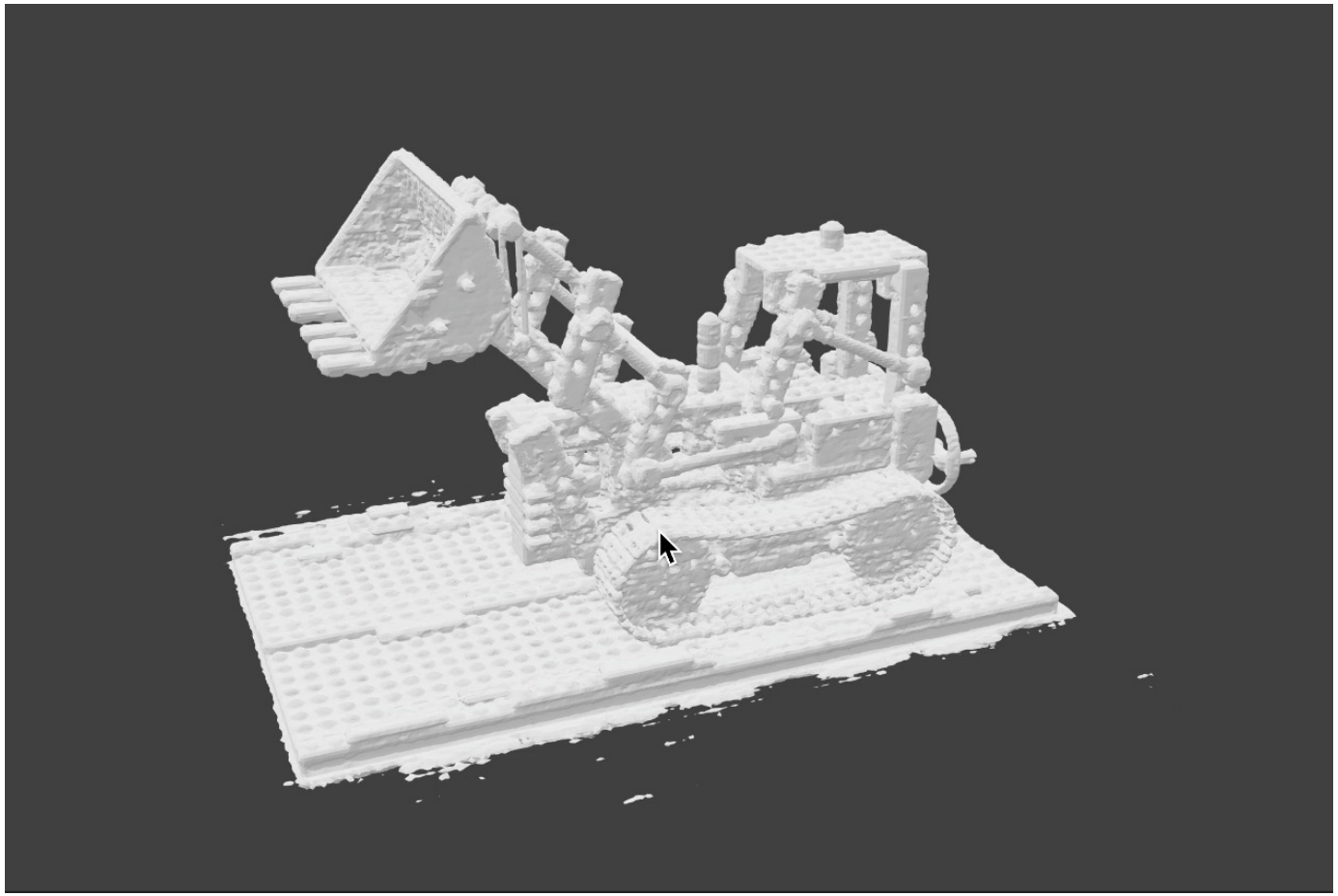
$$d(\mathbf{r}) \approx \sum_{i}^{N} T_i \alpha_i z_i$$

Because it models the entire plenoptic function you can insert objects with proper occlusion effects (in contrast to lightfields)

ClimateNERF
Li et al 2023

Neat feature: because rendering is based on scattering, you can apply all sorts of new scattering effects

Extract surface on high density regions



NeRF limitations

- Expensive / slow to train and render
  - Not any more – massive changes in representation and rendering practices
- Sensitive to sampling strategy
- Does not generalize between scenes
- Sensitive to pose accuracy
- Assumes static scene
- Assumes static lighting and camera focus
- Not a mesh

NeRF explosion

Awesome Neural Radiance Fields

A curated list of awesome neural radiance fields papers, inspired by awesome-computer-vision.

How to Pull Request?

If you are interested in adding papers, feel free to submit a pull request following the instruction here.

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Survey

- Neural Volume Rendering: NeRF And Beyond, Dellaert and Yen-Chen, Arxiv 2020 | blog | github

Papers

- NeRF: Representing Scenes as Neural Radiance Fields for View Synthesis, Mildenhall et al., ECCV 2020 | github | bibtex
- NeRF++: Analyzing and Improving Neural Radiance Fields, Zhang et al., Arxiv 2020 | github | bibtex
- DeRF: Decomposed Radiance Fields, Rebain et al. Arxiv 2020 | bibtex
- NeRD: Neural Reflectance Decomposition from Image Collections, Boss et al., Arxiv 2020 | github | bibtex
- NeRF--: Neural Radiance Fields Without Known Camera Parameters, Wang et al., Arxiv 2021 | github | bibtex

Faster Inference

- Neural Sparse Voxel Fields, Liu et al., NeurIPS 2020 | github | bibtex
- AutoInt: Automatic Integration for Fast Neural Volume Rendering, Lindell et al., Arxiv 2020 | bibtex

Unconstrained Images

- NeRF in the Wild: Neural Radiance Fields for Unconstrained Photo Collections, Martin-Brualla et al., Arxiv 2020 | bibtex

Deformable

- Deformable Neural Radiance Fields, Park et al., Arxiv 2020 | github | bibtex
- D-NeRF: Neural Radiance Fields for Dynamic Scenes, Pumarola et al., Arxiv 2020 | bibtex
- Dynamic Neural Radiance Fields for Monocular 4D Facial Avatar Reconstruction, Gafni et al., Arxiv 2020 | bibtex
- Non-Rigid Neural Radiance Fields: Reconstruction and Novel View Synthesis of a Deforming Scene from Monocular Video, Tretschk et al., Arxiv 2020 | github | bibtex

Video

- Neural Scene Flow Fields for Space-Time View Synthesis of Dynamic Scenes, Li et al., Arxiv 2020 | bibtex
- Space-time Neural Irradiance Fields for Free-Viewpoint Video, Xian et al., Arxiv 2020 | bibtex
- Neural Radiance Flow for 4D View Synthesis and Video Processing, Du et al., Arxiv 2020 | bibtex
- Neural Body: Implicit Neural Representations with Structured Latent Codes for Novel View Synthesis of Dynamic Humans, Peng et al., Arxiv 2020 | bibtex

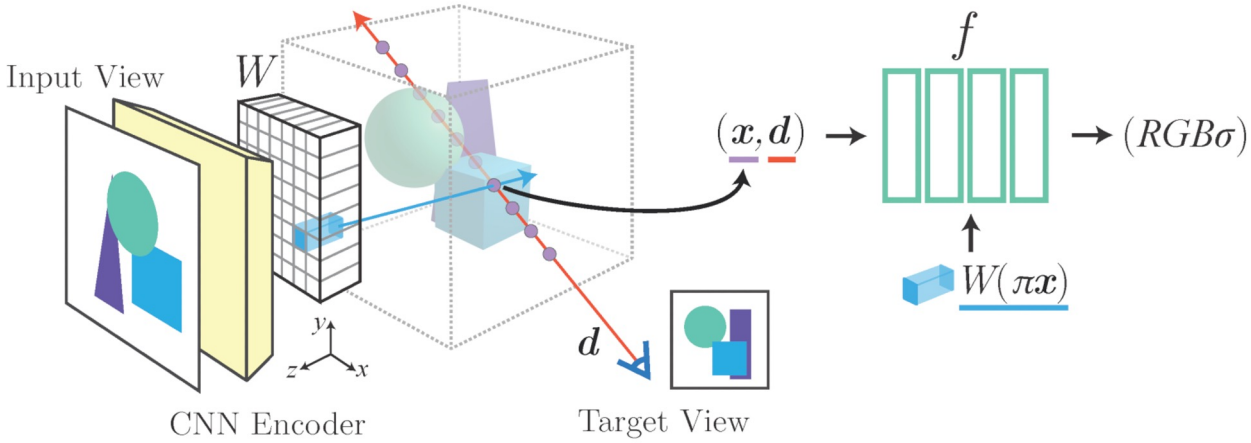
Generalization

- GRAF: Generative Radiance Fields for 3D-Aware Image Synthesis, Schwarz et al., NeurIPS 2020 | github | bibtex
- GRF: Learning a General Radiance Field for 3D Scene Representation and Rendering, Trevithick and

https://github.com/yenchenlin/awesome-NeRF

NeRF generalizations

- PixelNeRF [Yu et al. CVPR'21]
- IBRNet [Wang et al. CVPR'21]
- MVSNeRF [Yao et al. ICCV'21]
- NerfingMVS [Wei et al. ICCV'21]
- NeRFormer [Reizenstein et al. ICCV'21]
- GRF [Trevithick et al. ICCV'21]
- …



PixelNeRF [Yu et al. CVPR'21]

NeRF in the wild

R. Martin-Brualla et al. NeRF in the Wild. CVPR 2021

PixelNeRF

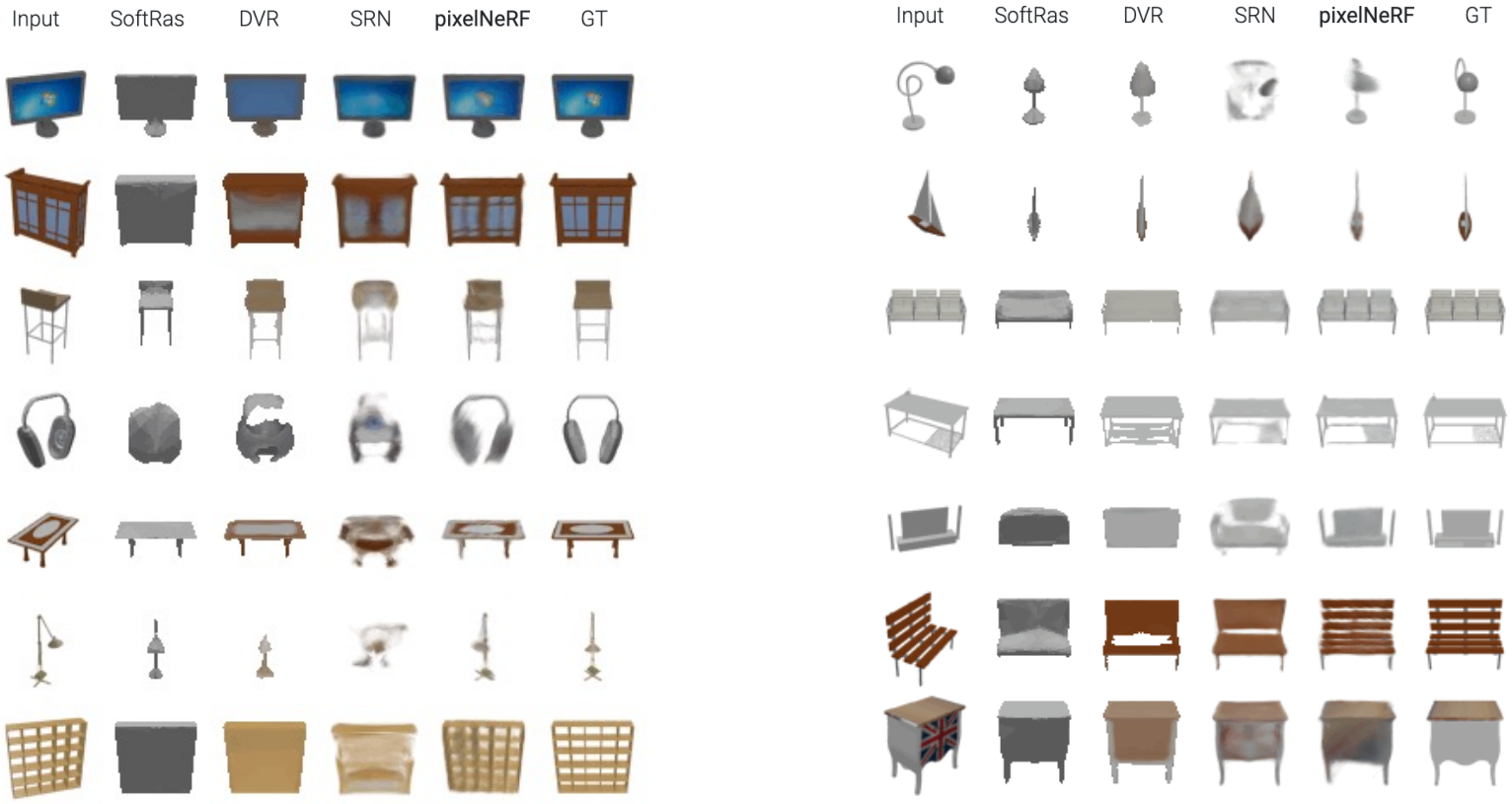
Three input views

PixelNeRF

3-view NeRF

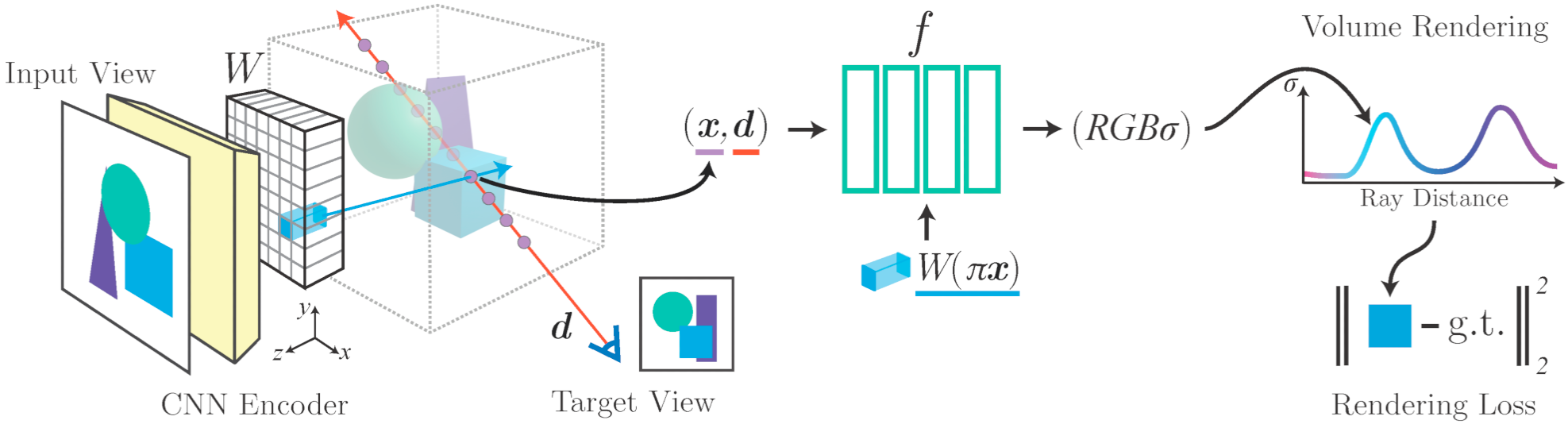
A. Yu et al. PixelNeRF: Neural Radiance Fields from One or Few Images. CVPR 2021

PixelNeRF



A. Yu et al. [PixelNeRF: Neural Radiance Fields from One or Few Images](). CVPR 2021

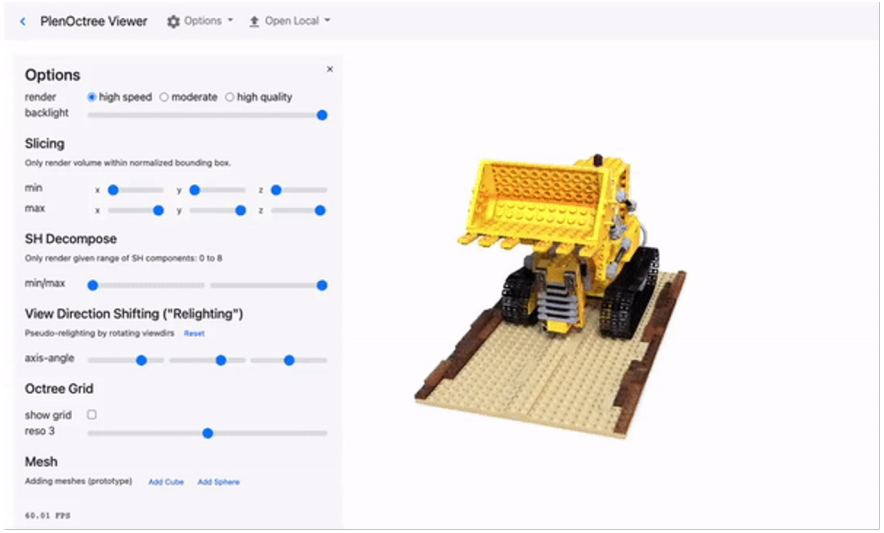
PixelNeRF



A. Yu et al. PixelNeRF: Neural Radiance Fields from One or Few Images. CVPR 2021

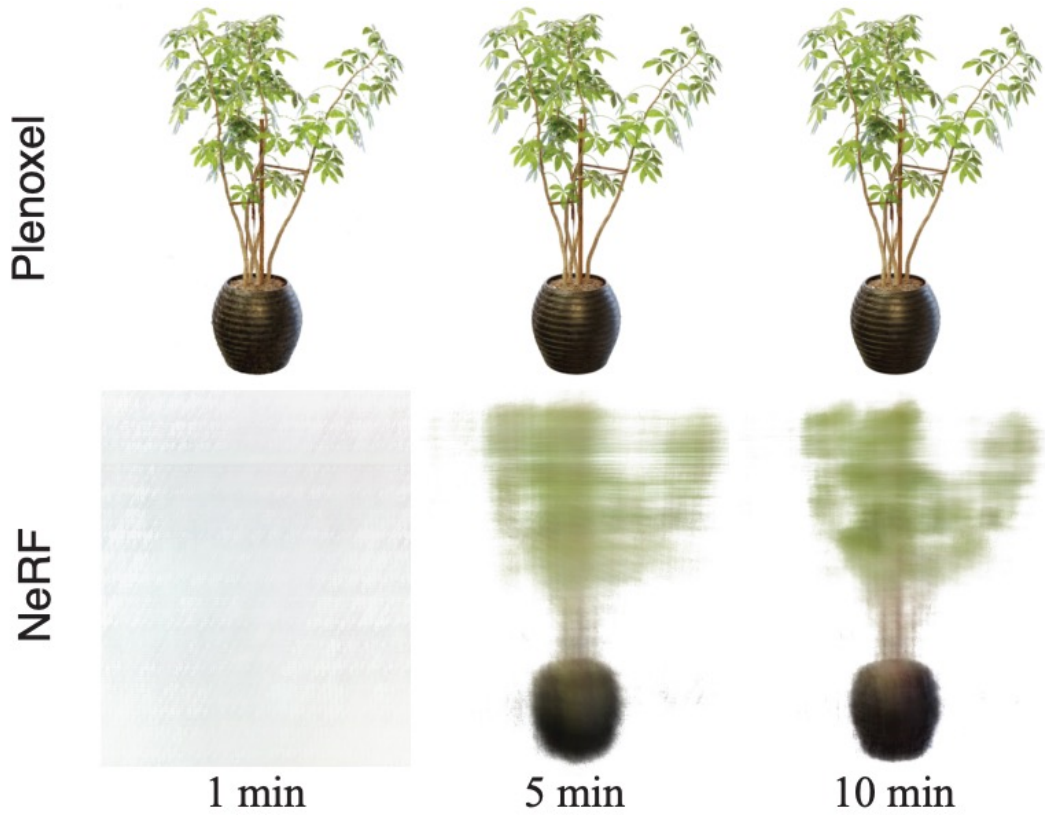
Fast Inference

- PlenOctrees [Yu et al. ICCV'21]
- SNeRG [Hedman et al. ICCV'21]
- FastNeRF [Garbin et al. ICCV'21]
- KiloNeRF [Reiser et al. ICCV'21]
- AutoInt [Lindell et al. CVPR'21]
- …



PlenOctrees [Yu et al. ICCV'21]

Plenoxels



S. Fridovich-Kiel et al. Plenoxels: Radiance Fields without Neural Networks. CVPR 2022

Plenoxels

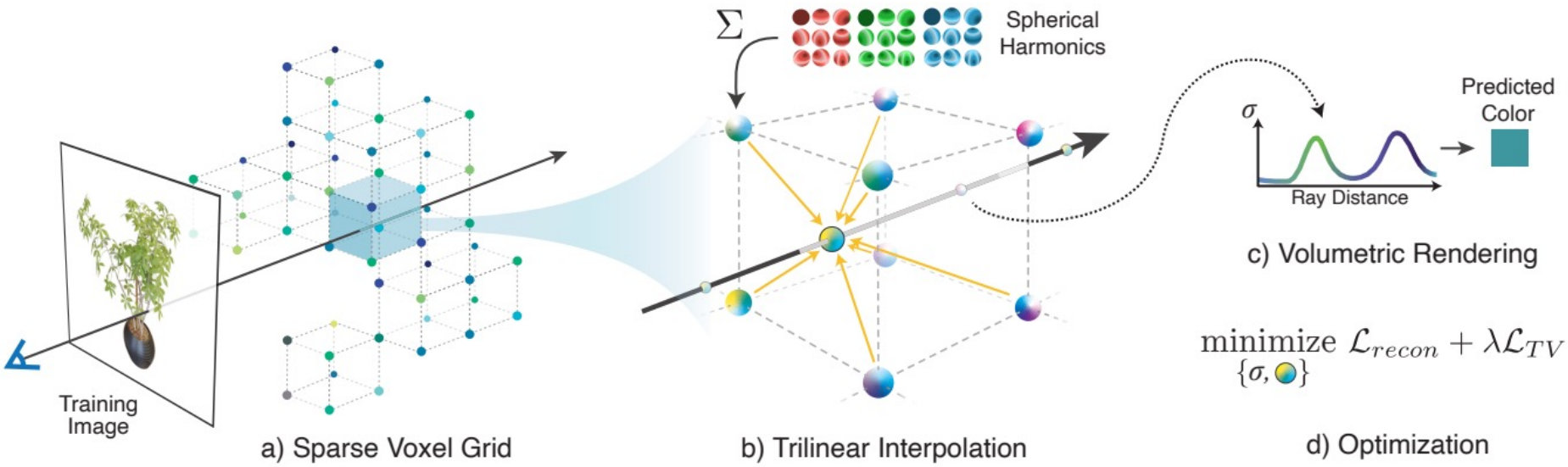


Figure 2. **Overview of our sparse Plenoxel model.** Given a set of images of an object or scene, we reconstruct a (a) sparse voxel ("Plenoxel") grid with density and spherical harmonic coefficients at each voxel. To render a ray, we (b) compute the color and opacity of each sample point via trilinear interpolation of the neighboring voxel coefficients. We integrate the color and opacity of these samples using (c) differentiable volume rendering, following the recent success of NeRF [26]. The voxel coefficients can then be (d) optimized using the standard MSE reconstruction loss relative to the training images, along with a total variation regularizer.

S. Fridovich-Kiel et al. Plenoxels: Radiance Fields without Neural Networks. CVPR 2022

Pose Estimation

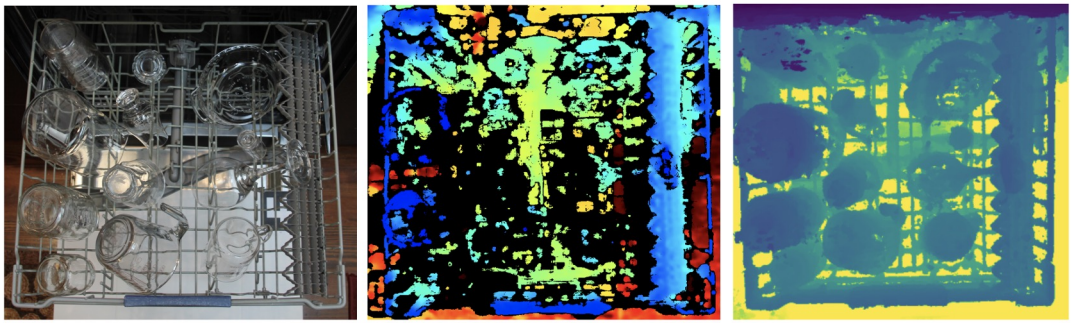
- GNeRF [Meng et al. ICCV ‘21]
- BARF [Lin et al. ICCV ‘21]
- NeRF– [Wang et al. arXiv ‘21]
- SC-NeRF [Jeong et al. ICCV ’21]
- iNeRF [Yen-Chen et al. IROS ‘21]

Input video.

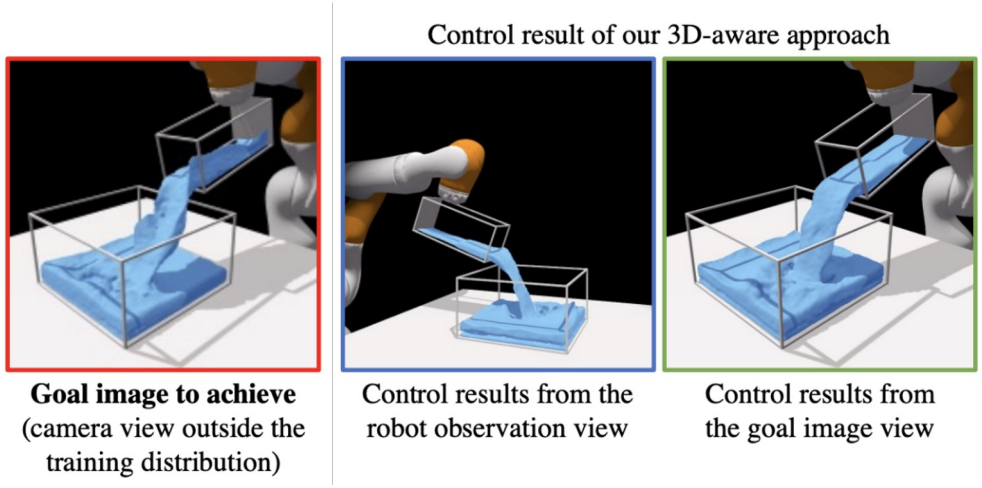
Predicted pose & image.

iNeRF [Yen-Chen et al. IROS ‘21]

Robotics / Simulation



NeRF-GTO: Using a Neural Radiance Field to Grasp Transparent Objects [Ichnowski et al. CoRL ‘21]



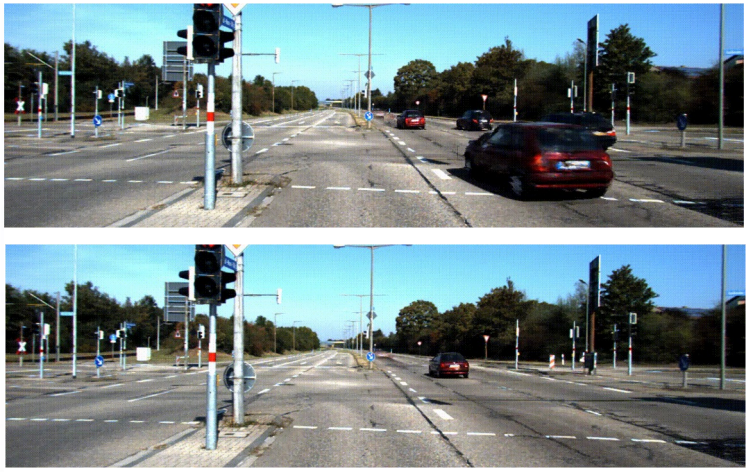
3D Neural Scene Representations for Visuomotor Control [Li et al. Corl ‘21]

Others: iMAP[Sucar ICCV’21]

Object Decomposition

ST-NeRF [Zhang et al. SISGRAPH ‘21]

Yang et al.



Neural Scene Graphs [Ost et al. CVPR ‘21]

Others: OSF [Guo et al.], uORF [Yu et al.]

Neural RGB-D surface reconstruction

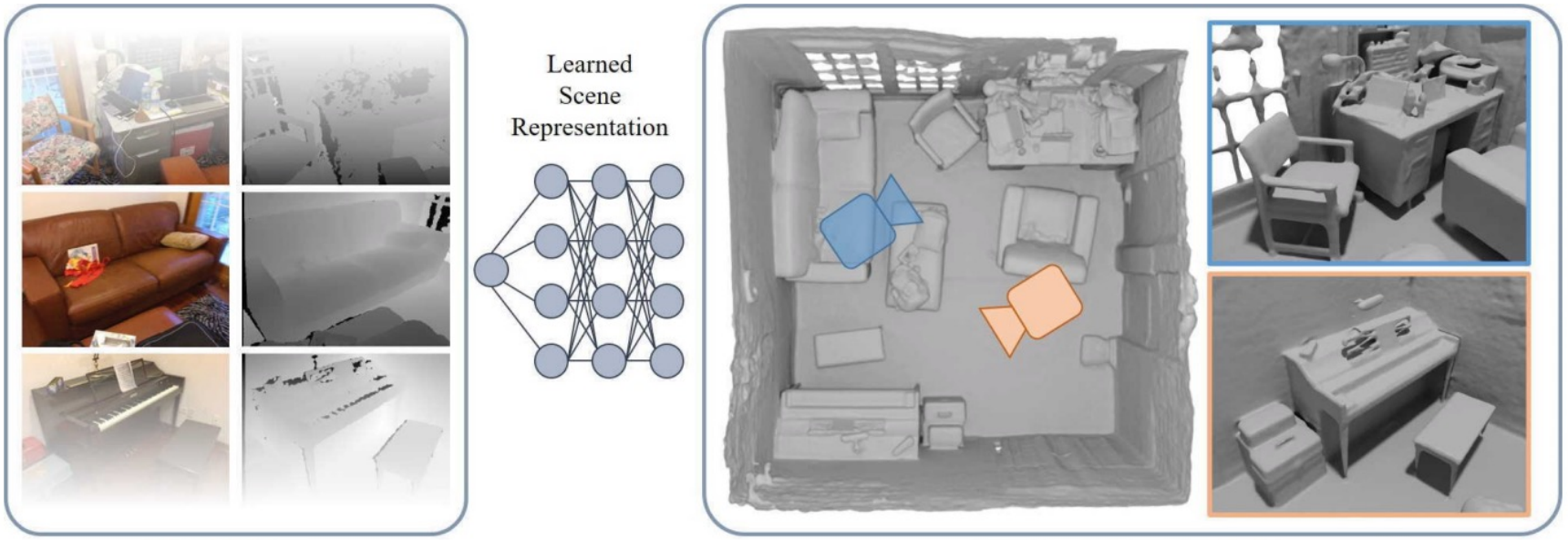
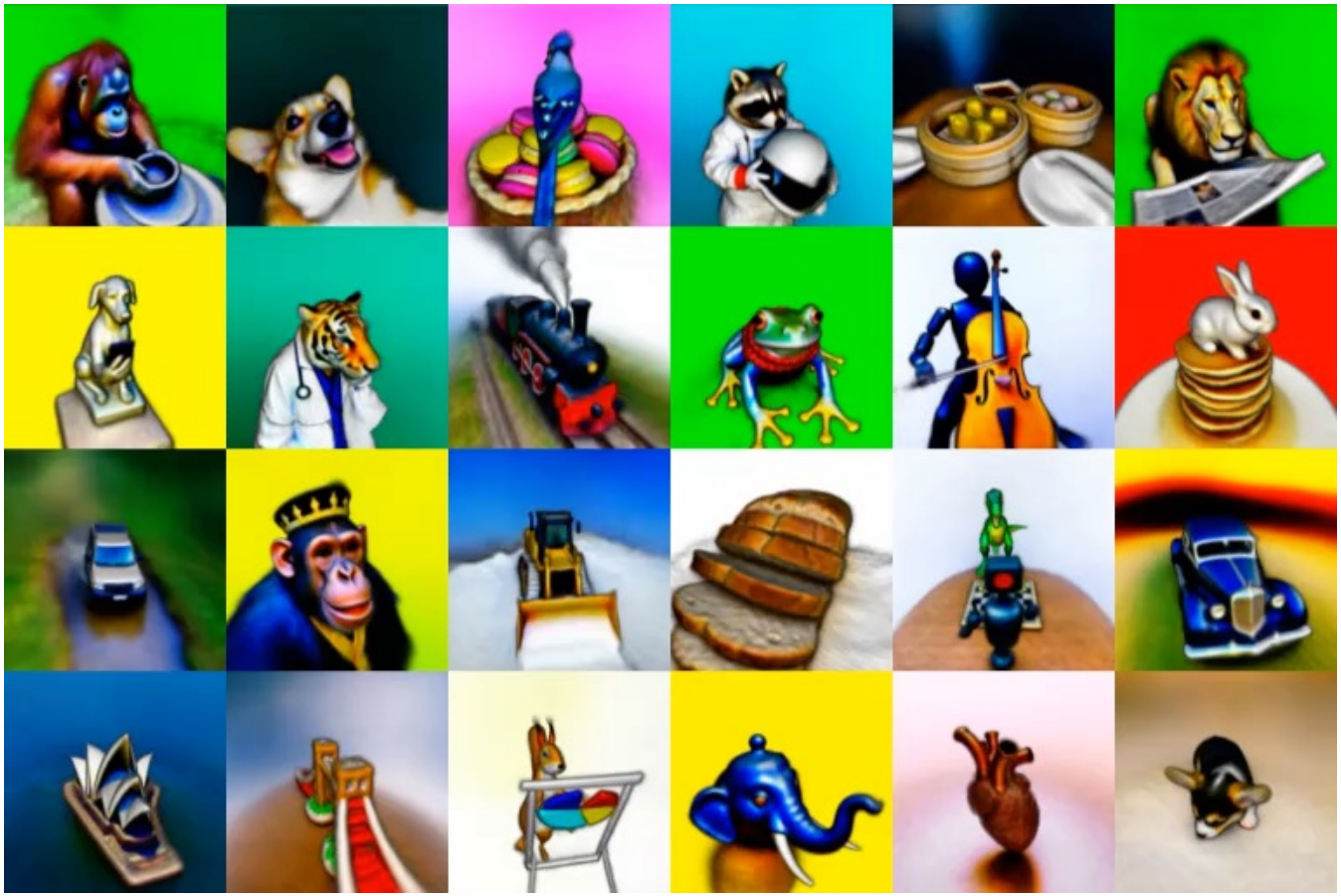


Figure 1. Our method obtains a high-quality 3D reconstruction from an RGB-D input sequence by training a multi-layer perceptron. The core idea is to reformulate the neural radiance field definition in NeRF [48], and replace it with a differentiable rendering formulation based on signed distance fields which is specifically tailored to geometry reconstruction.

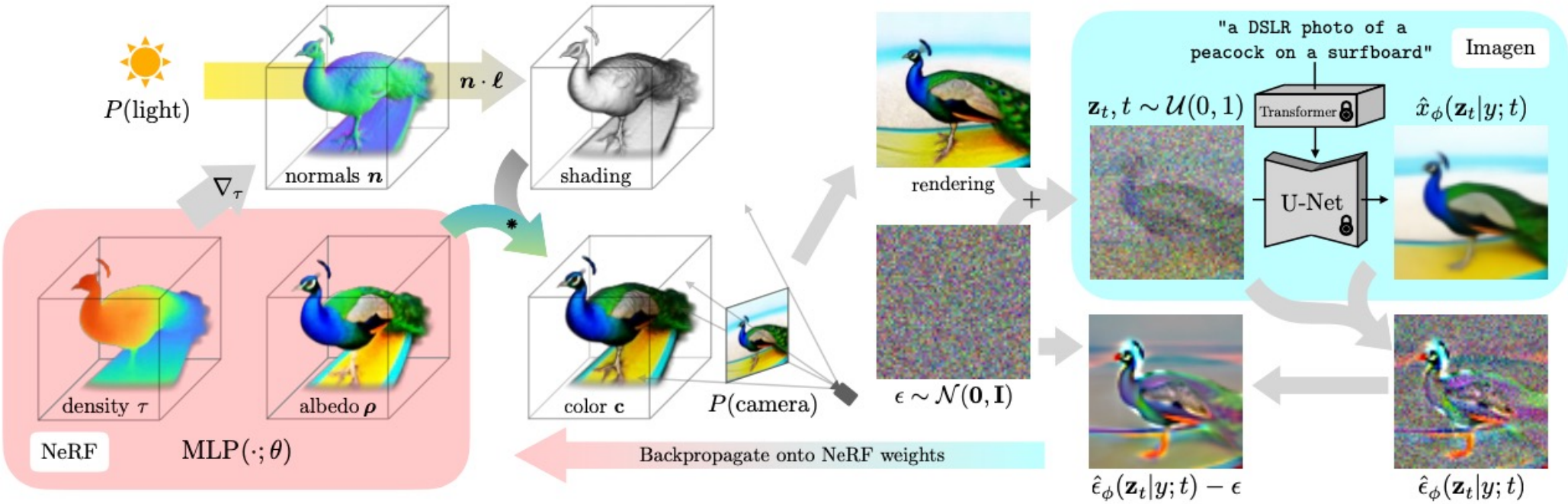
D. Azinovic et al. Neural RGB-D Surface Reconstruction. CVPR 2022

DreamFusion



B. Poole, A. Jain, J. Barron, B. Mildenhall. DreamFusion: Text-to-3D using 2D Diffusion. arXiv 2022

DreamFusion



B. Poole, A. Jain, J. Barron, B. Mildenhall. DreamFusion: Text-to-3D using 2D Diffusion. arXiv 2022