Animation

D.A. Forsyth
Animation

- **Persistence of vision:**
  - The visual system smooths in time. This means that images presented to the eye are perceived by the visual system for a short time after they are presented. In turn, this means that if images are shown at the right rate (about 20-30 Hz will do it), the next image replaces the last one without any perceived blank space between them.

- **Visual closure:**
  - A sequence of still images is seen as a motion sequence if they are shown quickly enough - i.e. smooth motion between positions is inferred.
Keyframing

From “It’s a magical world”, Watterson, 1996
Basic techniques

• **Keyframing:**
  • generate frames by drawings, interpolate between drawings

• **Stop motion:**
  • put model in position, photograph, move, photograph, etc.

• **Compositing:**
  • generate frames as mixtures of video sequences

• **Morphing:**
  • mix video sequences while modifying shapes

• **Procedural animation:**
  • use some form of procedural description to move object
Keyframing - issues

- Generating frames by hand is a huge burden -- 1hr of film is 3600x24 frames
- Skilled artists generate key frames, inbetweeners generate inbetween frames
- Changes are hideously expensive
- Natural interpolation problem -- interpolate various variables describing position, orientation, configuration of objects

Figure 10.4 Three keyframes. Three keyframes representing a ball on the ground, at its highest point, and back on the ground.

From “The computer in the visual arts”, Spalter, 1999
Linear interpolation

Figure 10.5 Inbetweening with linear interpolation. Linear interpolation creates inbetween frames at equal intervals along straight lines. The ball moves at a constant speed. Ticks indicate the locations of inbetween frames at regular time intervals (determined by the number of frames per second chosen by the user).

From “The computer in the visual arts”, Spalter, 1999
More complex interpolation

Figure 10.9  Inbetweening with nonlinear interpolation. Nonlinear interpolation can create equally spaced inbetween frames along curved paths. The ball still moves at a constant speed. (Note that the three keyframes used here and in Fig. 10.10 are the same as in Fig. 10.4.)
Modify the parameter, too

Figure 10.10 Inbetweening with nonlinear interpolation and easing. The ball changes speed as it approaches and leaves keyframes, so the dots indicating calculations made at equal time intervals are no longer equidistant along the path.

A use for parameter continuous interpolates here.
Notice that we don’t necessarily need a physical ball.

From “The computer in the visual arts”, Spalter, 1999
A variety of variables can be interpolated

From “The computer in the visual arts”, Spalter, 1999
 Grey-level

(iv)

Shear

(v)

Shape

(vi) From “The computer in the visual arts”, Spalter, 1999
Position and orientation:

note that the position travels along a motion path.

From “The computer in the visual arts”, Spalter, 1999
Various path specifications:

perhaps by interactive process;
  two issues:
  building the path
  where are the keyframes?

From “The computer in the visual arts”, Spalter, 1999
Interpolating orientation gives greater realism. Notice that the tangent to the motion path gives a great cue to the orientation of the object.

From “The computer in the visual arts”, Spalter, 1999
Stop motion

- Very important traditional animation technique
- Put model in position, photograph, move, photograph, etc. e.g. “Seven voyages of Sinbad”, “Clash of the titans”, etc.
  - Model could be
    - plastic
    - linkage
    - clay, etc.
- Model work is still very important e.g. “Men in Black”
- Computerizing model work is increasingly important
  - issue: where does configuration of computer model come from?
From “The computer Image”, Watt and Policarpo, 1998
Motion capture

- Instrument a person or something else, perhaps by attaching sensors
- Measure their motion
- Link variables that give their configuration to variables that give configuration of a computer model
Compositing

- Overlay one image/film on another
  - variety of types of overlay

Simple overlay - spaceship pixels replace background pixels

From “The computer in the visual arts”, Spalter, 1999
Compositing

Spaceship pixels replace background pixels if they are not white (white is “dropped out”)

From “The computer in the visual arts”, Spalter, 1999
Compositing

Spaceship pixels replace background pixels if they are darker

From “The computer in the visual arts”, Spalter, 1999
Compositing

Light areas are more transparent - blending

From “The computer in the visual arts”, Spalter, 1999
Compositing

- Note that human intervention might be required to remove odd pixels, if the background doesn’t have a distinctive colour.
- One can buy sets of images which have been segmented by hand.

From “The computer in the visual arts”, Spalter, 1999
Compositing

- Recall image relighting notes
  - we want to insert an object into a scene
  - we have
    - background scene  \( \text{image is: B} \)
    - model of background scene  \( \text{image is: Mn} \)
    - model of object in background scene  \( \text{image is: Mo} \)

- Composite by:
  - at model pixels
    - \( \text{B} + (\text{Mo} - \text{Mn}) \)
  - at object pixels
    - \( \text{Mo} \)
  - at background pixels
    - \( \text{B} \)
Compositing

Background model \( Mn \)

Mo-Mn in non-object, non-background pixels

Background image \( B \)

Background model, rendered with objects \( Mo \), superimposed on \( B \)

Figures from Debevec, Rendering Synthetic Objects into Real Scenes: Bridging Traditional and Image-based Graphics with Global Illumination and High Dynamic Range Photography 1998
Compositing

Figures from Debevec, Rendering Synthetic Objects into Real Scenes: Bridging Traditional and Image-based Graphics with Global Illumination and High Dynamic Range Photography 1998
More interesting compositing problems

Figure from Shadow matting and compositing, Chuang et al 2002
Morphing

- Simple blending doesn’t work terribly well for distinct shapes
- Idea: map the one shape to the other, while blending

From “The computer Image”,
Watt and Policarpo, 1998
Morphing

From “On growth and Form”, D’Arcy Thompson
Morphing

• Another use for the deformation encoding shown earlier

• From “The computer Image”,
  • Watt and Policarpo, 1998
Morphing

From “The computer Image”,
Watt and Policarpo, 1998
Procedural Animation

• Key idea:
  • Algorithms yield motion
  • Inspirations:
    • insight
    • physics
    • simplified physics
  • Easily guessed algorithm gives good results
    • waves
    • terrain
    • l-systems (for plants)
    • finite state machines (for character control)

• And the winners are particles
  • because they’re easy to model
  • and they don’t interact, as we shall see
A single particle under gravity

- State:
  - position x, velocity v
  - gravitational acceleration is a
    - (all vectors)
- Motion is governed by two differential equations:
  \[
  \frac{dx}{dt} = v
  \]
  \[
  \frac{dv}{dt} = a
  \]
- subject to initial conditions
  - x(0)=x0; v(0)=v0
Particle in a potential field

- Imagine there is some potential energy
  - usually depends on position only
  - gravity can be represented like this (remember gravitational potential?)
  - write potential as:
    \[ \phi(x) \]

- Now:
  - the particle has mass \( m \)
  - experiences force:
    \[
    - \nabla \phi(x) = - \left( \begin{array}{c}
    \frac{\partial \phi}{\partial x} \\
    \frac{\partial \phi}{\partial y} \\
    \frac{\partial \phi}{\partial z}
    \end{array} \right)
    \]
Particle in a potential field

• We get equations:

\[
\begin{align*}
\frac{dx}{dt} &= \mathbf{v} \\
\frac{dv}{dt} &= -\nabla \phi(x) \quad m
\end{align*}
\]

• subject to the same i.c.’s
Particle in a potential field

- Assume
  - we know position, velocity at time: \( t \)
    \[ x_t, v_t \]
  - want position, velocity at time: \( t + \Delta t \)
    \[ x_{t+\Delta t}, v_{t+\Delta t} \]

- Have:
  \[
  x_{t+\Delta t} \approx x_t + \Delta t v_t \\
  v_{t+\Delta t} \approx v_t - \Delta t \frac{\nabla \phi(x_t)}{m}
  \]
Particle in a potential field

- Previous slide is forward Euler method
- Any other method for solving ODE’s applies
  - and there are lots of better methods
  - which you learned in numerical analysis
Procedural Dynamics - Particle systems

• There is a source of particles
  • move under gravity, sometimes collisions
  • control with potential fields
    • notice it is pretty straightforward to do time-varying potentials

• Example: fireworks
  • particles chosen with random colour, originating randomly within a
    region, fired out with random direction and lasting for a random period of
    time before they expire
    • or explode, generating another collection of particles, etc

• Example: water
  • very large stream of particles, large enough that one doesn’t see the gap

• Example: grass
  • fire particles up within a tapered cylinder, let them fall under gravity, keep
    a record of the particle’s trail.
Now replace particle centers with small blobs of colour in the image plane

http://www.arch.columbia.edu/manuals/Softimage/3d_learn/GUIDED/PARTICLES/p_first.htm
By John Tsiombikas from Wikipedia
Commercial particle systems (wondertouch)
Commercial particle systems (wondertouch explosions)
Commercial particle systems (wondertouch distortions)
Ballistic + Collision

- Objects move freely under gravity until they collide.
- For accurate physical models, order in which collisions occur is important.
Collision detection

- Particles are straightforward
  - -ish (geometry is easy)
  - issues: undetected collisions
    - strategies:
      - take fixed time steps, fixup collision
        - but we may not be able to tell a collision has occurred!
      - potential barrier
        - but this may force quite small time steps; stiffness
        - backward Euler helps, but only within limits
      - identify safe bounds within which to advance time, search
        - use priority queue
        - but this may force quite small time steps
Collision detection

- **Rigid objects**
  - (safe bounds strategy)
  - We decide that objects closer than some small distance have collided
  - **Problem:**
    - we have a geometric representation
    - which faces/vertices are closer than epsilon?
  - **Strategy:**
    - prune with spatial data structures
    - axis aligned bounding boxes, BSP trees, etc.
    - test results exhaustively
    - triangle test is easiest case
Collision detection

- Two non-intersecting triangles can be separated by a plane
  - assume they’re not coplanar
    - then can look at 6 choose 3 = 20 planes obtained by choosing 3 verts
  - extra work if they’re coplanar
    - separating plane is normal to triangle plane
  - appropriate choice of plane yields distance between triangles
- Improvement
  - Gilbert-Johnson-Keerthi algorithm, using support functions
  - open source version due to Stephen Cameron
    - http://www.comlab.ox.ac.uk/stephen.cameron/distances/
Collision: SOA

12,201 chairs;
218,568,714 triangles

Collisions - resolution

- Strategies:
  - potential field
  - explicit collision model
    - state_out=F(state_in, physical parameters)
    - typical physical parameters:
      - friction, coefficient of restitution
  - data driven
    - match inputs to data, read off outputs

- Collisions
  - produce randomness in motion
  - are a mechanism to control the motion
Control via collisions

- Collisions are an important source of randomness
  - particularly in the case of sharp edges, rotation -> dice
  - physical parameters typically vary over space
    - Idea: modify physical parameters at collisions to produce desired outcome
  - Issues:
    - extremely complex search
    - requires very fast simulation
    - Notice: each object can be advanced different timesteps

Making collisions more “cartoony”

- Good cartoon animators anticipate and follow through
  - eg a ball hesitates and stretches before it starts moving
  - squashes and overshoots when it finishes

Making collisions more “cartoony”

Making collisions more “cartoony”

- and you can apply this to characters, too...

Automatic anticipation

- Subtract a small amount of second derivative from motion
  - works well for lots of cases
  - Wang et al. 2006

http://vis.berkeley.edu/papers/animfilter/
Automated anticipation
Deforming the mesh

- Apply slightly time-shifted version of the filter to different points
- Leading edge starts before trailing edge
12 principles of cartoon animation

1. Squash and stretch
2. Anticipation
3. Staging
4. Straight Ahead Action and Pose to Pose
5. Follow Through and Overlapping Action
6. Slow In and Slow Out
7. Arcs
8. Secondary Action
9. Timing
10. Exaggeration
11. Solid Drawing
12. Appeal

Secondary motion
Secondary motion
Flocking - Boids

• We’d like things to move in schools
  • and not hit each other, objects
  • abstraction: particle with rocket with maximum force

• 3 goals
  • How to accelerate?
  • each goal gives an acceleration; weighted sum
  • accumulate in priority order until acceleration exceeds threshold,
  • then cut back last

Alignment  Separation  Cohesion
COURSE: 07
COURSE ORGANIZER: DEMETRI TERZOPoulos

"BOIDS DEMOS"
CRAIG REYNOLDS
SILICON STUDIOS, MS 3L-980
2011 NORTH SHORELINE BLVD.
MOUNTAIN VIEW, CA  94039-7311

http://www.red.com/cwr/boids.html
Procedural ideas

- Easily guessed algorithm gives good results
  - waves
  - terrain
  - l-systems (for plants)
  - finite state machines (for character control)
Procedural animation

- **Kinematics**
  - the configuration of a chain given its state variables
  - e.g. where is the end of the arm if angles are given?
- **Inverse kinematics**
  - the state variables that yield the configuration
  - e.g. what angles put the end of the arm here?

From “The computer Image”, Watt and Policarpo, 1998
Inverse Kinematics

From “The computer Image”, Watt and Policarpo, 1998
Inverse Kinematics

When 3D Models Meet
the embarrassing social consequences of lacking inverse kinematics

From “The computer in the visual arts”, Spalter, 1999
Inverse kinematics

- Endpoint position and orientation is:
  \[ e(\theta) \]

- Central Question: how do I modify the configuration variables to move the endpoint in a particular direction?

\[
\delta e = \begin{pmatrix}
\frac{\partial e_1}{\partial \theta_1} & \ldots & \frac{\partial e_1}{\partial \theta_k} \\
\ldots & \ldots & \ldots \\
\frac{\partial e_6}{\partial \theta_1} & \ldots & \frac{\partial e_6}{\partial \theta_k}
\end{pmatrix}
\delta \theta = J \delta \theta
Inverse kinematics

- \( J \) is the Jacobian
  - If \( \text{rank}(J) < 6 \), then
    - some movements aren’t possible
    - or more than one movement results in the same effect
  - If \( k > 6 \) then the chain is redundant
    - more than one set of variables will lead to the same configuration

\[
\begin{bmatrix}
\frac{\partial e_1}{\partial \theta_1} & \cdots & \frac{\partial e_1}{\partial \theta_k} \\
\frac{\partial e_6}{\partial \theta_1} & \cdots & \frac{\partial e_6}{\partial \theta_k}
\end{bmatrix}
\delta e = \begin{bmatrix}
\delta \theta_1 \\
\delta \theta_2 \\
\vdots \\
\delta \theta_k
\end{bmatrix} \quad \delta \theta = J \delta \theta
\]
Procedural animation

• Generate animations using procedural approach
  • e.g. “Slice and dice” existing animations to produce a more complex animation
  • e.g. use forward kinematics and a hierarchical model (doors swinging in our original hierarchical model)
  • e.g. construct a set of forces, etc. and allow objects to move under their effects.
    • particle models
    • waves
    • collision and ballistic models
    • spring mass models
    • control - flocking, etc.
Procedural waves

- Sum weighted sinusoids
  - weights change by frequency
  - weights go down as frequency goes up
Turbulence/Perlin noise

- Many natural textures look like noise or “smoothed” noise
  - (marble, flames, clouds, terrain, etc.)
- Issue:
  - obtain the right kind of smoothing
- Strategy:
  - construct noise functions at a variety of scales
    - do this by drawing samples from a random number generator at different spacings
  - form a weighted sum
Turbulence/Perlin noise

- Typically,
  - spacing is in octaves
    - number of samples at i’th level is $2^i$
  - weights
    - $w(i)=p^i$
    - $p$ is persistence
- 1D turbulence yields natural head motions
- 2D turbulence yields marble, natural textures, terrains
- 3D turbulence yields animations for clouds, fog, flames
### Frequency

<table>
<thead>
<tr>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
</tr>
<tr>
<td>2</td>
</tr>
<tr>
<td>4</td>
</tr>
<tr>
<td>8</td>
</tr>
<tr>
<td>16</td>
</tr>
<tr>
<td>32</td>
</tr>
</tbody>
</table>

### Persistence

**Persistence = 1/4**

- Amplitude: $\frac{1}{4}$
- Amplitude: $\frac{1}{16}$
- Amplitude: $\frac{1}{64}$
- Amplitude: $\frac{1}{256}$
- Amplitude: $\frac{1}{1024}$
- Result

**Persistence = 1/2**

- Amplitude: $\frac{1}{2}$
- Amplitude: $\frac{1}{4}$
- Amplitude: $\frac{1}{8}$
- Amplitude: $\frac{1}{16}$
- Amplitude: $\frac{1}{32}$
- Result

**Persistence = 1/root2**

- Amplitude: $\frac{1}{\sqrt{2}}$
- Amplitude: $\frac{1}{4\sqrt{2}}$
- Amplitude: $\frac{1}{8\sqrt{2}}$
- Amplitude: $\frac{1}{16\sqrt{2}}$
- Amplitude: $\frac{1}{32\sqrt{2}}$
- Result

**Persistence = 1**

- Amplitude: 1
- Amplitude: 1
- Amplitude: 1
- Amplitude: 1
- Amplitude: 1
- Result
Some noise functions are created in 2D.

Adding all these functions together produces a noisy pattern.
To create more interesting and complicated textures, you should try mixing several Perlin functions. This texture was created in two parts. Firstly a Perlin function with low persistence was used to define the shape of the blobs. The value of this function was used to select from two other functions, one of which defined the stripes, the other defined the blochiety pattern. A high value chose more of the former, a low value more of the later. The stripes were defined by multiplying the first Perlin Function by some number (about 20) then taking the cosine.

A marbled texture can be made by using a Perlin function as an offset to a cosine function.

\[
texture = \cos( x + \text{perlin}(x,y,z) )
\]

Very nice wood textures can be defined. The grain is defined with a low persistence function like this:

\[
g = \text{perlin}(x,y,z) * 20
grain = y - \text{int}(g)
\]

The very fine bumps you can see on the wood are high frequency noise that has been stretched in one dimension.

\[
bumps = \text{perlin}(x+50, y+50, z+20)
\text{if bumps < .5 then bumps = 0 else bumps = 1}
\]

References

Intel Developer Site article about using the new MMX technology to render Perlin Noise in real-time

Ken Perlin's Homepage: [http://www.ari.edu/perlin/](http://www.ari.edu/perlin/)
I assume the person responsible for Perlin Noise. He has an interesting page with lots of useful links to texturing and modeling
The following textures were made with 3D Perlin Noise

Standard 3 dimensional perlin noise. 4 octaves, persistence 0.25 and 0.5

Low persistence. You can create harsher edges to the perlin noise by applying a function to the output.

To create more interesting and complicated textures, you should try mixing several Perlin functions. This texture was created in two parts. Firstly a Perlin function with low persistence was used to define the shape of the blobs. The value of this function was used to select from two other functions, one of which defined the stripes, the other defined the blitcy pattern. A high value chose more of the former, a low value more of the latter. The stripes were defined by multiplying the first Perlin Function by some number (about 20) then taking the cosine.

A marbly texture can be made by using a Perlin function as an offset to a cosine function.

\[ \text{texture} = \text{cosine}( x + \text{perlin}(x,y,z) ) \]
Flame: Compute intensity of point based on distance from center in x. Scale it based on distance in y. Add turbulence. Use 3-D turbulence to animate. Here is an example of a flame with added turbulence.

Conclusions

- Lots of interesting effects can be gained by adding turbulence
- Need to play with degree and scale to get most realistic images
- Ties together a lot of topics in graphics (fractals, texture, color, curves)
Terrain, clouds generated using procedural textures and Perlin noise
http://www.planetside.co.uk/ -- tool is called Terragen
Terrain, clouds generated using procedural textures and Perlin noise
http://www.planetside.co.uk/ -- tool is called Terragen
Terrain, clouds generated using procedural textures and Perlin noise
http://www.planetside.co.uk/ -- tool is called Terragen
Procedural Animation: L-systems

- Formal grammar, originally due to Lindenmayer
  - {Variables, Constants, Initial state, Rules}
  - Plants by:
    - Constants are bits of geometry,
    - rules appropriately chosen

Figure from wikipedia entry
L-Systems

L-Systems

Plant development

productions

L-System plant growing

Flowers at side branches

\[ A \rightarrow I[F]A \]

Monopodial branching - raceme

Flowers at the apex

A → I[A]F

Sympodial branching - cyme
Finite state machines

- **FSM**
  - set of states
    - special start, end state
  - input vocabulary
  - transition function
    - state change on receiving

Slides after slides by Jarret Raim, LeHigh
Map to character

- AI modelled as a set of mental states
- State=desired behaviour mode
- Events trigger transition
- Input to the FSM continues as long as the game continues.
FSM Authoring

- **States**
  - E: enemy in sight
  - S: hear a sound
  - D: dead

- **Events**
  - E: see an enemy
  - S: hear a sound
  - D: die

- **Action performed**
  - On each transition
  - On each update in some states (e.g. attack)

Problem: Can’t go directly from attack to patrol. We’ll fix this later.
FSM Authoring

- Original FSM doesn’t
  - remember previous state
  - so attack doesn’t know if it was triggered from patrol or inspect (sound heard?)

- Could add a state
  - but this gets messy
Hierarchy

- Each state is an FSM
- Some events move within a level, some trigger a transition at higher levels
- When we enter a state, we need an initial state for that FSM
  - Default
  - Random
  - Depends on behaviour, etc.
- This is all just a (much bigger) FSM, but easier to author
Hierarchy

- Note: This is not a complete FSM
  - All links between top level states still exist
  - Need more states for wander
Non-determinism

- Randomness easy to add, makes behaviour richer
Programming issues

- Typically work in a scripting language
  - Game engine, environment deal with details
  - e.g. events by polling? register/dispatch?
- Debugging
  - hard in rich environments
  - hard with multiple interacting state machines