

# Image Based Rendering

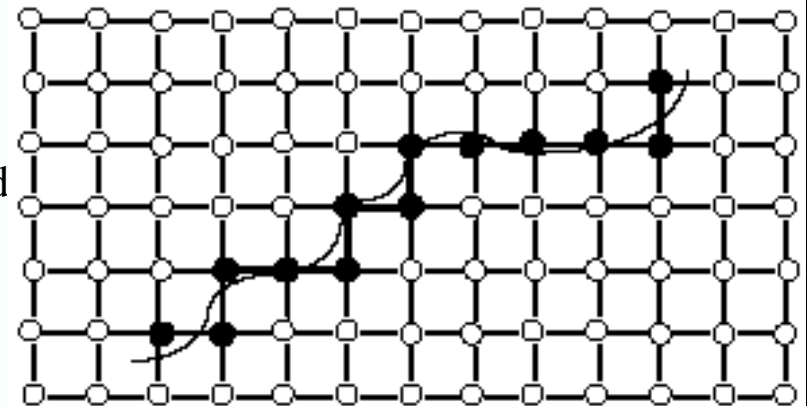
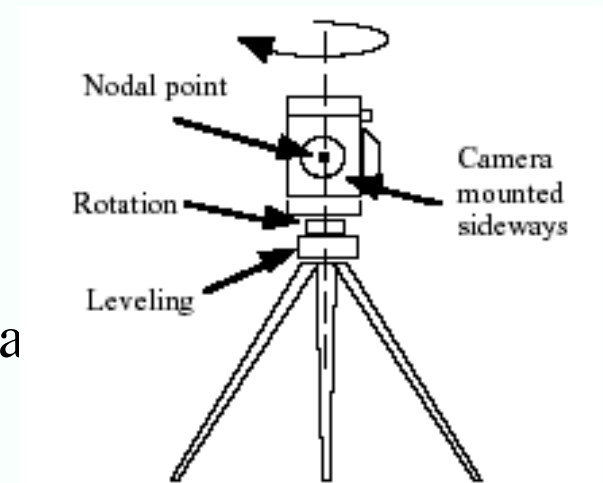
D.A. Forsyth, with slides from John Hart

# Topics

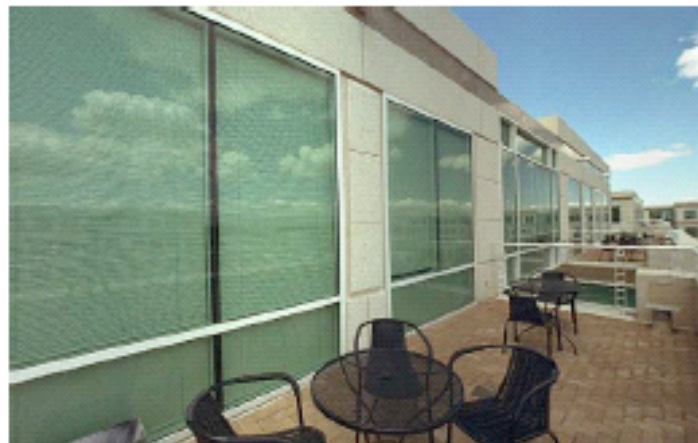
- **Mosaics**
  - translating cameras reveal extra information, break occlusion
- **Optical flow**
  - for very small movements of the camera
- **Explicit image based rendering**
  - multiple calibrated cameras yield a system of rays that models objects
- **Camera calibration**
  - postrender things into pictures
- **Stereopsis**
  - two cameras reveal a lot of geometry
- **Structure from motion**
  - more cameras yield even more geometry

# Implicit example: Quicktime VR

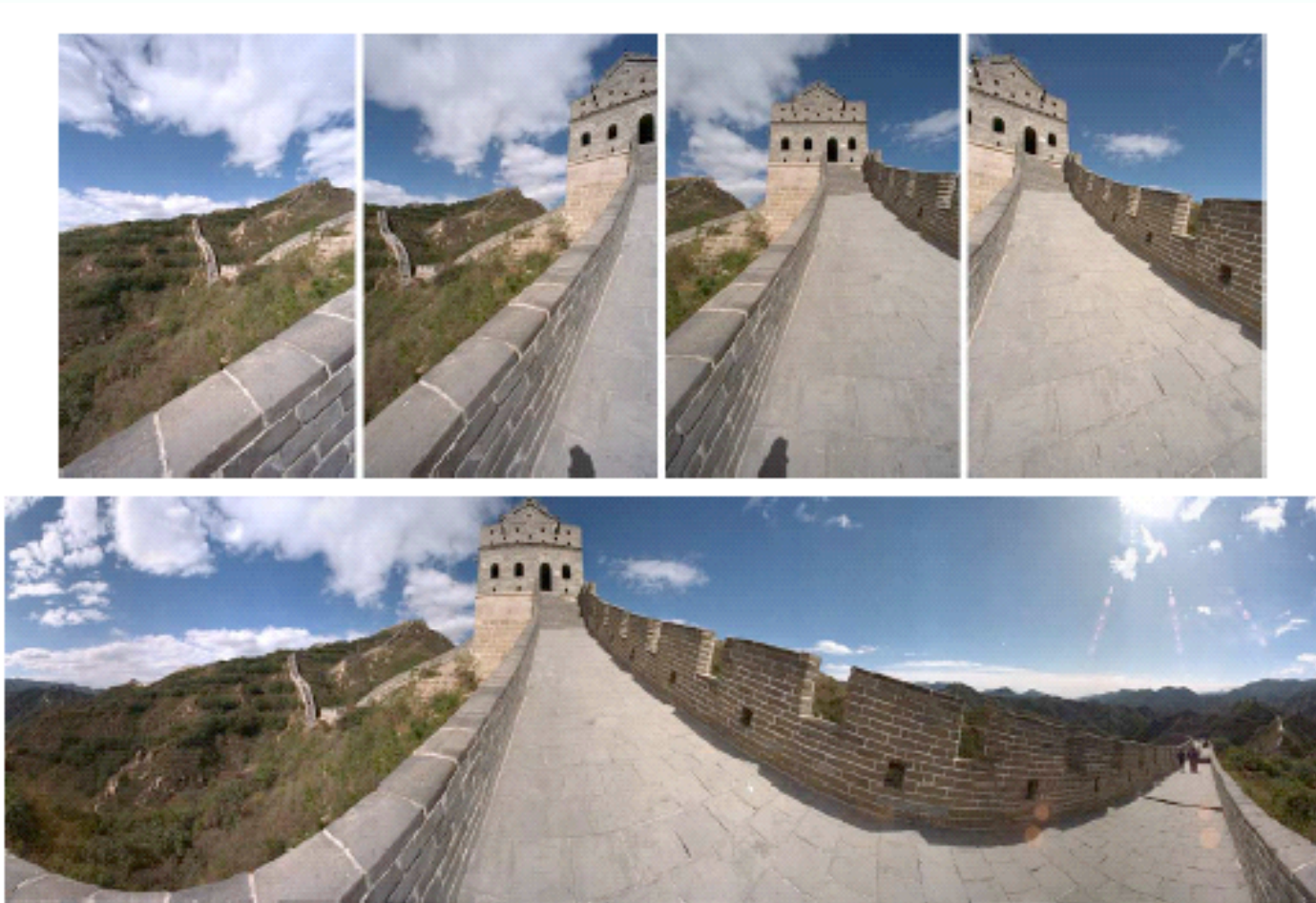
- Construct a mosaic that can provide va at various points
- Issues:
  - recovering the mosaics
    - specialised hardware
    - correlation based mosaicing
  - structuring the representation for fast rend



Figures from “QuickTime VR – An Image-Based Approach to Virtual Environment Navigation”, Shenchang Eric Chen, SIGGRAPH 95



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Figures from “QuickTime VR – An Image-Based Approach  
to

Matching points is important



M. Brown and D. Lowe, "Recognising Panoramas", ICCV 2003

# Matching points

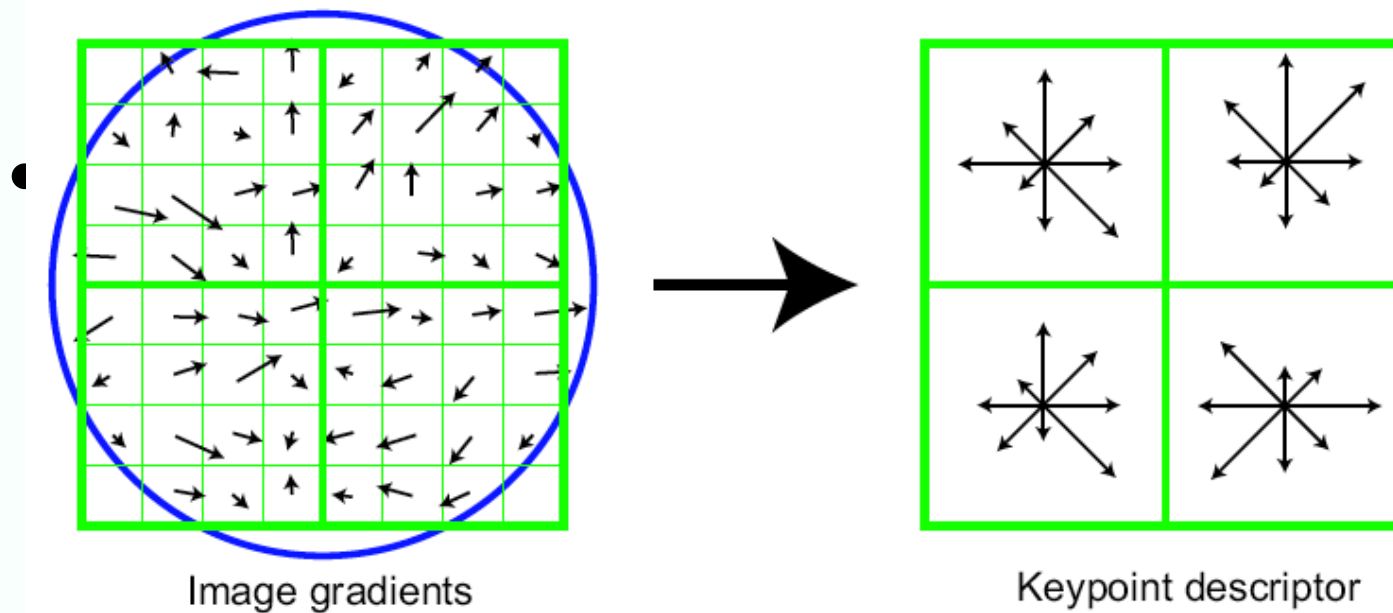
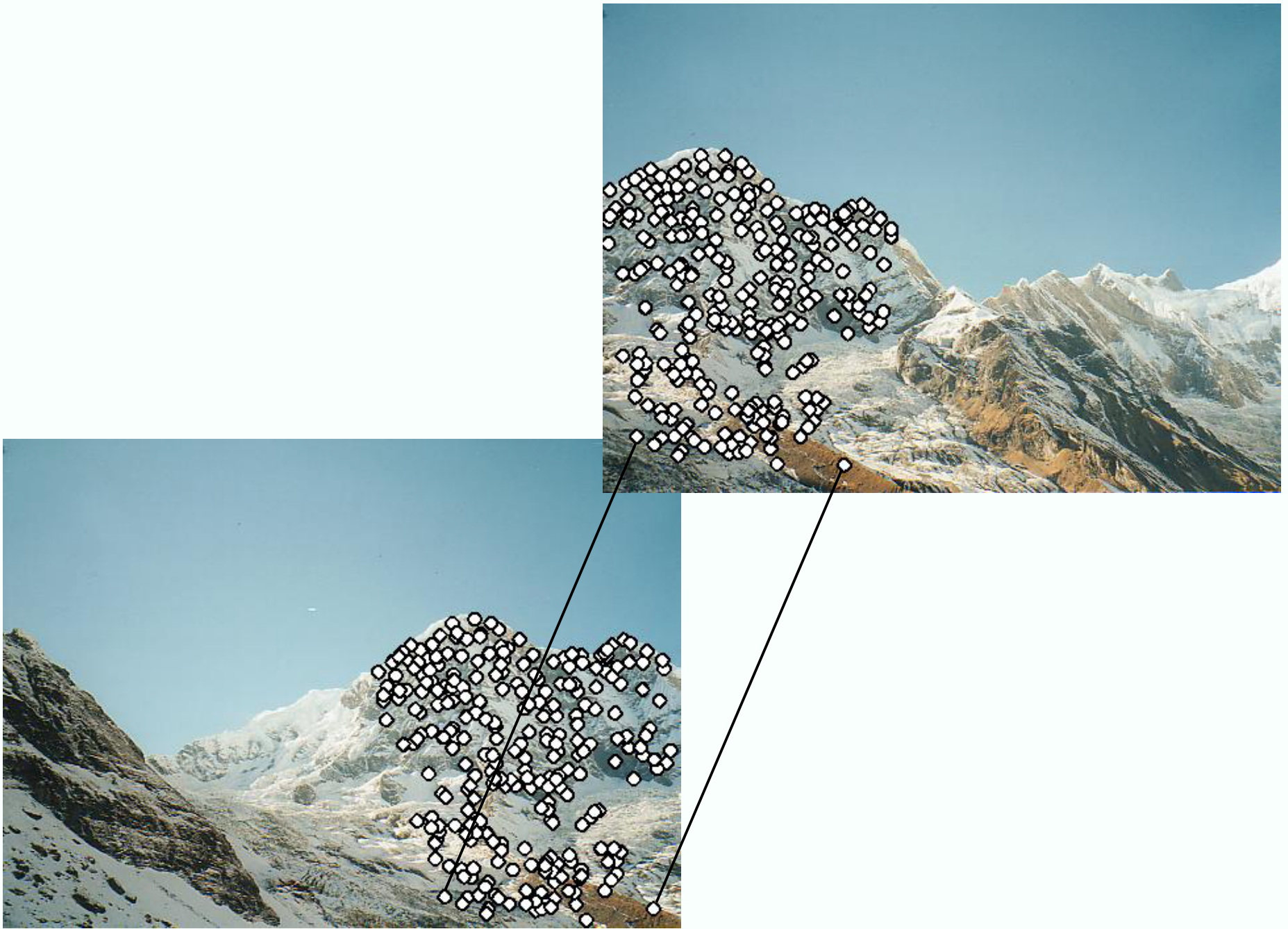


Fig 7 from:

Distinctive image features from scale-invariant keypoints

David G. Lowe, International Journal of Computer Vision, 60, 2 (2004), pp. 91-110.



M. Brown and D. Lowe, "Recognising Panoramas", ICCV 2003





Translation isn't enough to align the images - we need to use a homography



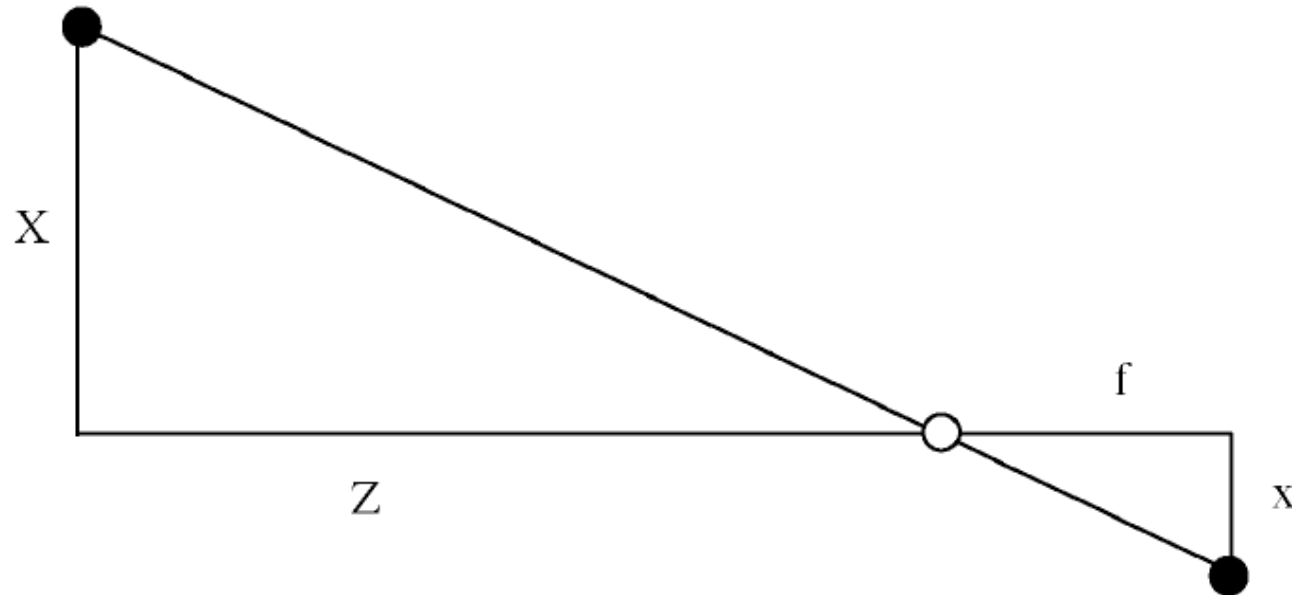
M. Brown and D. Lowe, "Recognising Panoramas", ICCV 2003

# Homographies

- Assume camera rotates about focal point
  - what happens to the image?
    - write camera as matrix, assume infinite image plane at  $z=-f$

# Projection in Coordinates

- From the drawing, we have  $X/Z = -x/f$
- Generally



# A perspective camera as a matrix

- Turn previous expression into HC's
  - HC's for 3D point are (X,Y,Z,T)
  - HC's for point in image are (U,V,W)

$$\begin{pmatrix} U \\ V \\ W \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & \frac{1}{f} & 0 \end{pmatrix} \begin{pmatrix} X \\ Y \\ Z \\ T \end{pmatrix}$$

*C*

# A general perspective camera - I

- Can place a perspective camera at the origin, then rotate and translate coordinate system
- In homogeneous coordinates, rotation, translation are:

$$\mathcal{E} = \begin{pmatrix} \mathcal{R} & \mathbf{t} \\ \mathbf{0} & 1 \end{pmatrix}$$

- So rotated, translated camera is:

$$\mathcal{C}\mathcal{E}$$

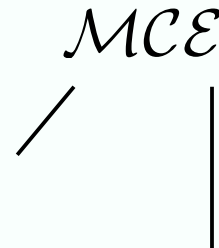
# A general perspective camera - II

- In the camera plane, there can be a change of coordinates
  - choice of origin
    - there is a “natural” origin --- the camera center
      - where the perpendicular passing through the focal point hits the image plane
  - rotation
  - pixels may not be square
  - scale

- Camera becomes

Intrinsics - typically come with the camera

Extrinsics - change when you move around



# What are the transforms?

$$\begin{pmatrix} U \\ V \\ W \end{pmatrix} = \begin{pmatrix} \text{Transform} \\ \text{representing} \\ \text{intrinsic parameters} \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & \frac{1}{f} & 0 \end{pmatrix} \begin{pmatrix} \text{Transform} \\ \text{representing} \\ \text{extrinsic parameters} \end{pmatrix} \begin{pmatrix} X \\ Y \\ Z \\ T \end{pmatrix}$$

|

$$\begin{pmatrix} s & 0 & c_x \\ 0 & sa & c_y \\ 0 & 0 & s/f \end{pmatrix}$$

$c_x, c_y$  - location of camera center

$s$  - scale

$a$  - aspect ratio

$f$  - focal length

# Homographies

- Camera 1 is

$$\begin{pmatrix} s & 0 & c_x \\ 0 & sa & c_y \\ 0 & 0 & s/f \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}$$

- Camera 2 is

$$\begin{pmatrix} s & 0 & c_x \\ 0 & sa & c_y \\ 0 & 0 & s/f \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix} \begin{pmatrix} \mathcal{R} & \mathbf{t} \\ 0 & 1 \end{pmatrix}$$



# Homographies

- There isn't any translation, so 1  $\rightarrow$  2 is

$$\begin{pmatrix} s & 0 & c_x \\ 0 & sa & c_y \\ 0 & 0 & s/f \end{pmatrix} \mathcal{R} \begin{pmatrix} s & 0 & c_x \\ 0 & sa & c_y \\ 0 & 0 & s/f \end{pmatrix}^{-1}$$

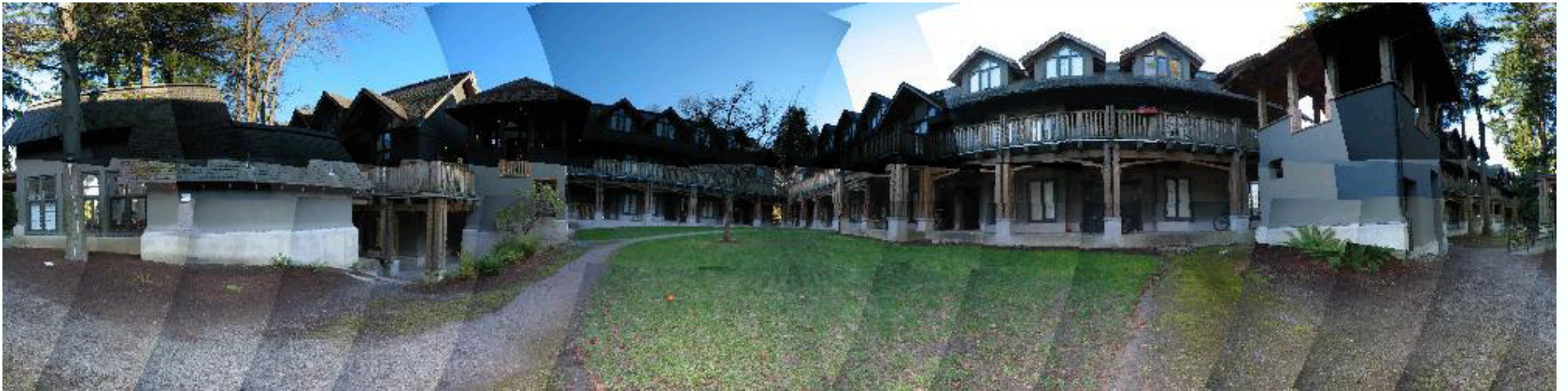
- How do we estimate?
  - linear least squares, followed by nonlinear least squares



M. Brown and D. Lowe, "Recognising Panoramas", ICCV 2003



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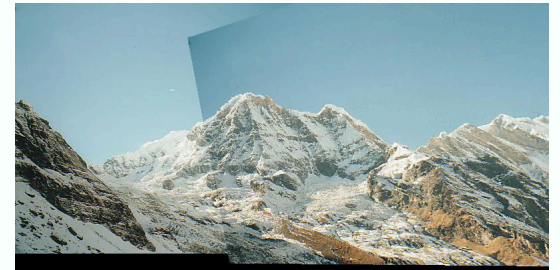
M. Brown and D. Lowe, "Recognising Panoramas", ICCV 2003

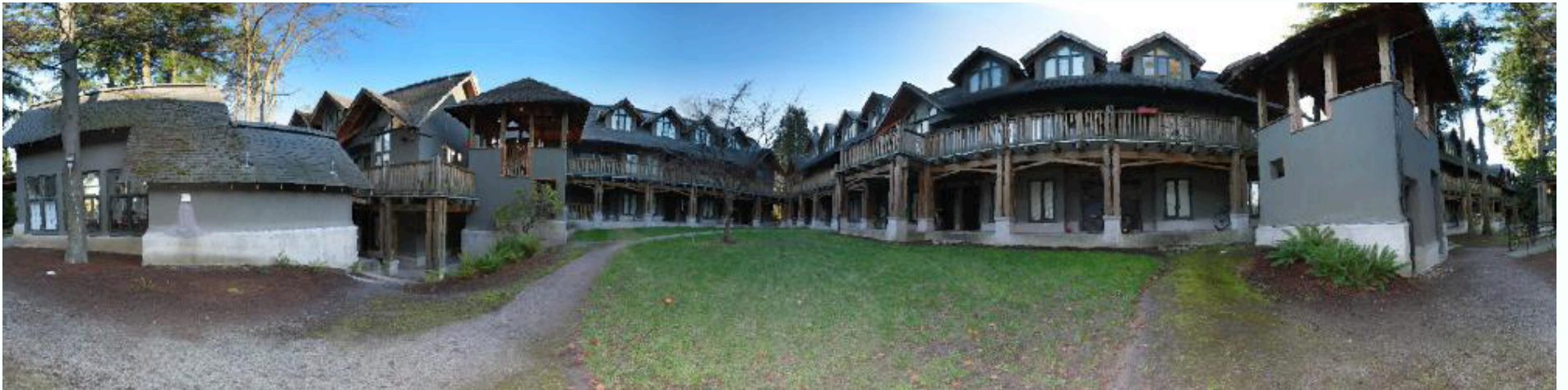
# Bundle adjustment

- Errors accumulate
  - so pairwise homographies will not join up to make a cylindrical mosaic
- Minimize all errors for all pairs of corresponding points
  - as a function of all parameters
  - start with pairwise estimates, use newton's method

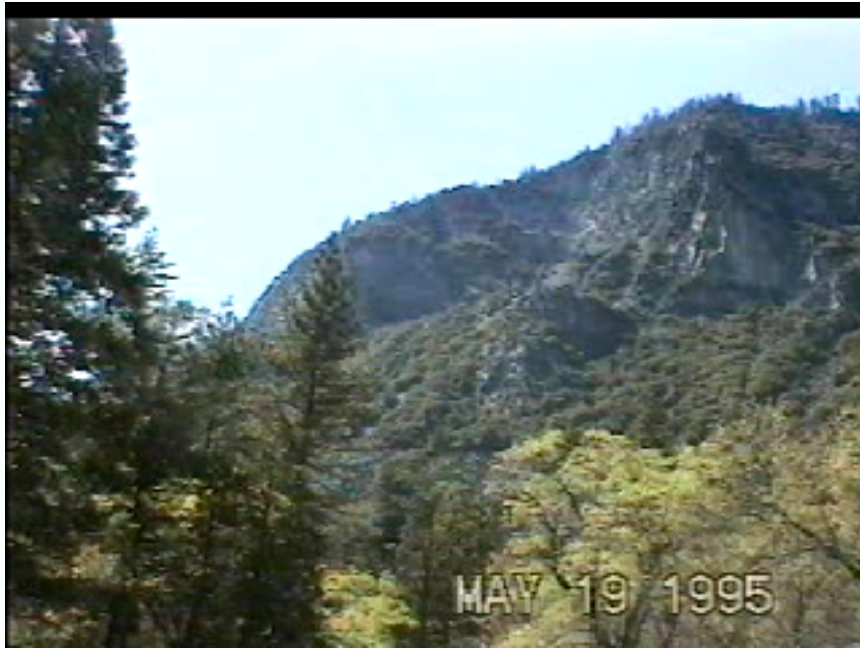
# Blending

- Corresponding pixels aren't always same color
  - aperture, sensitivity, etc., etc.
- Blend for consistency
  - pixels “far” from camera center are less reliable
  - Strategy:
    - weight with distance from camera center, then blend
      - fuzzes out small details
  - Strategy
    - separate bands
    - blend low spatial frequencies like this
    - high spatial frequencies from image with most weight

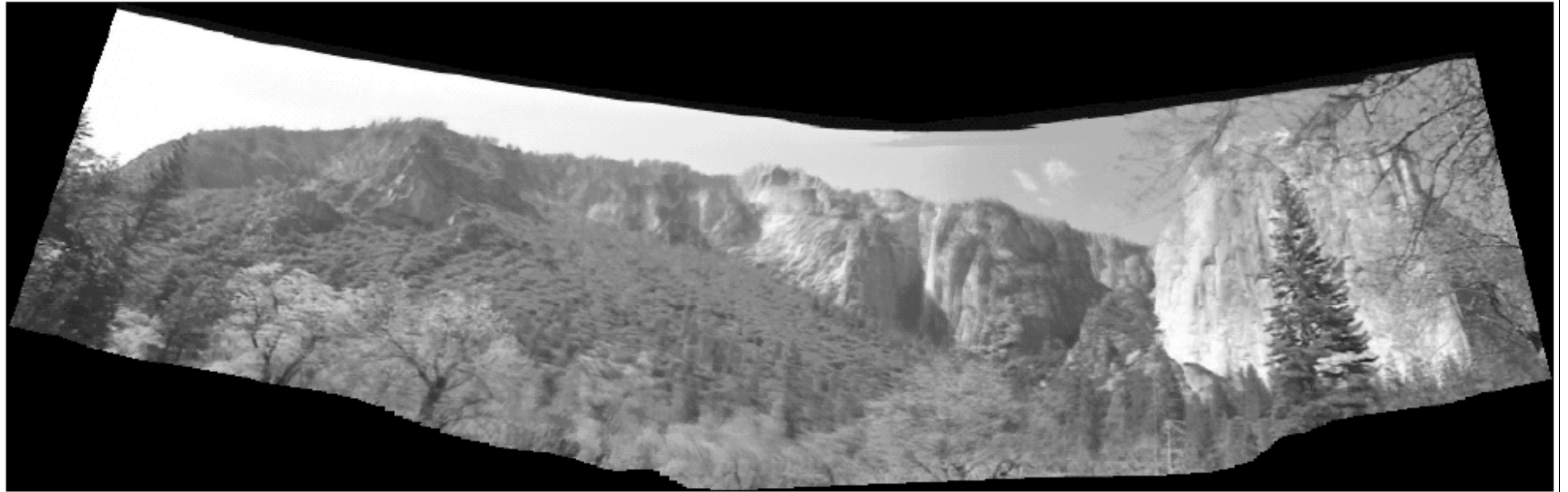


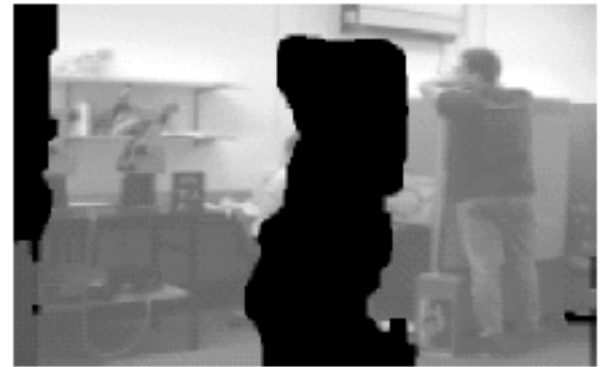
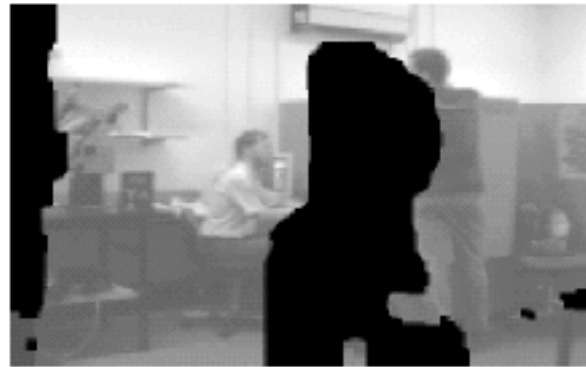


M. Brown and D. Lowe, "Recognising Panoramas", ICCV 2003



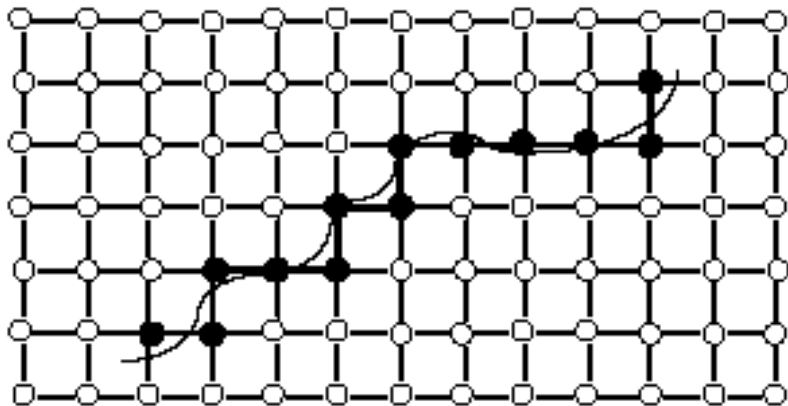


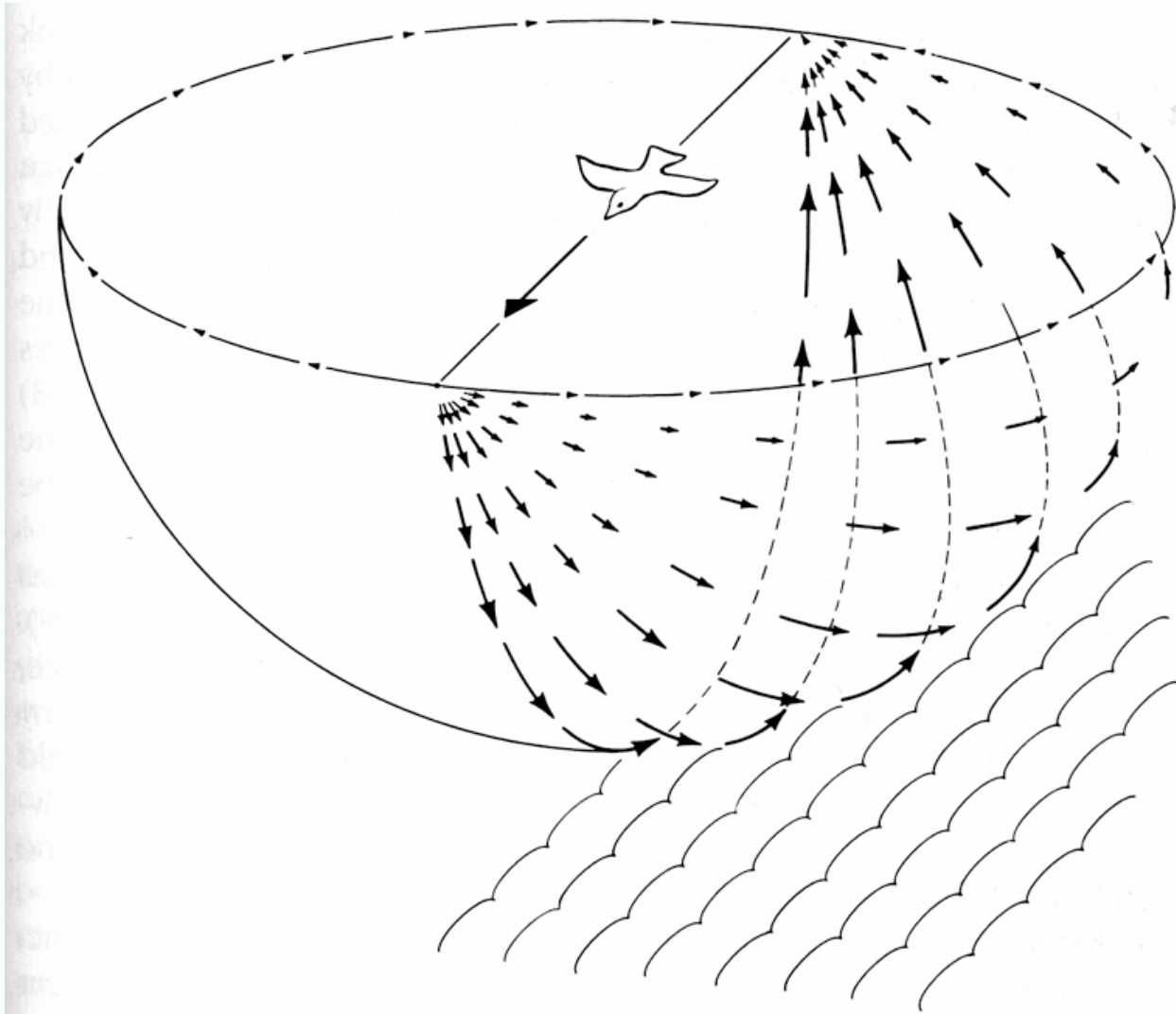




# Optical Flow

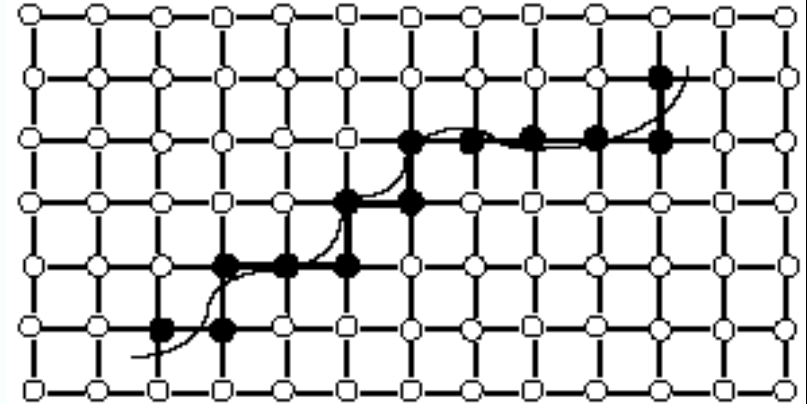
- Local motion “at a pixel”
  - Arrow joins pixel in this frame to corresponding pixel in next frame
    - hard to estimate accurately from images
      - but easy to predict for small movements of the head, known geom





*Figure 3-55.* Gibson's example of flow induced by motion. The arrows represent angular velocities, which are zero directly ahead and behind. (Reprinted from J. J. Gibson, *The Senses Considered as Perceptual Systems*, Houghton Mifflin, Boston, 1966, fig. 9.3. Copyright © 1966 Houghton Mifflin Company. Used by permission.)

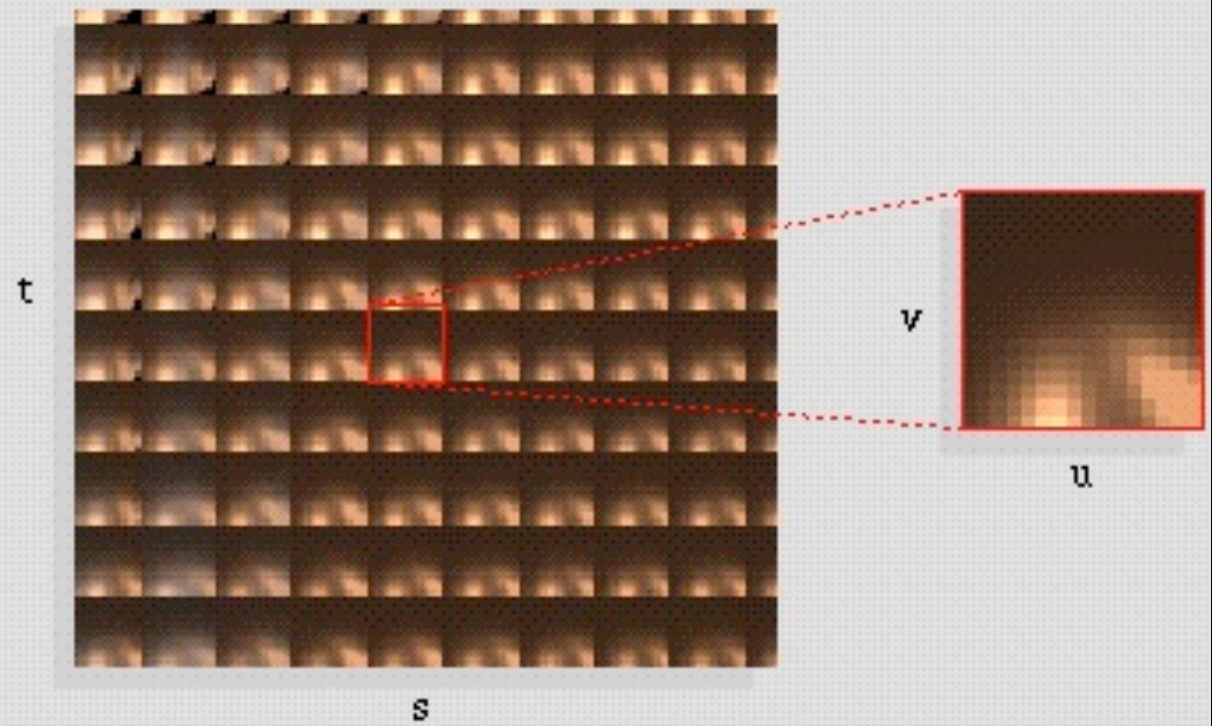
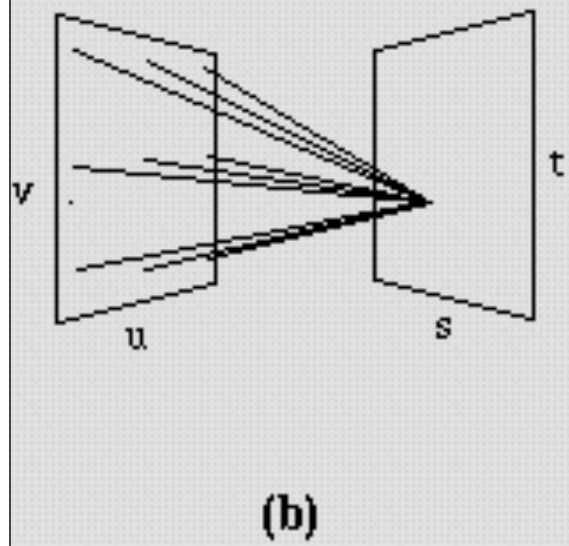
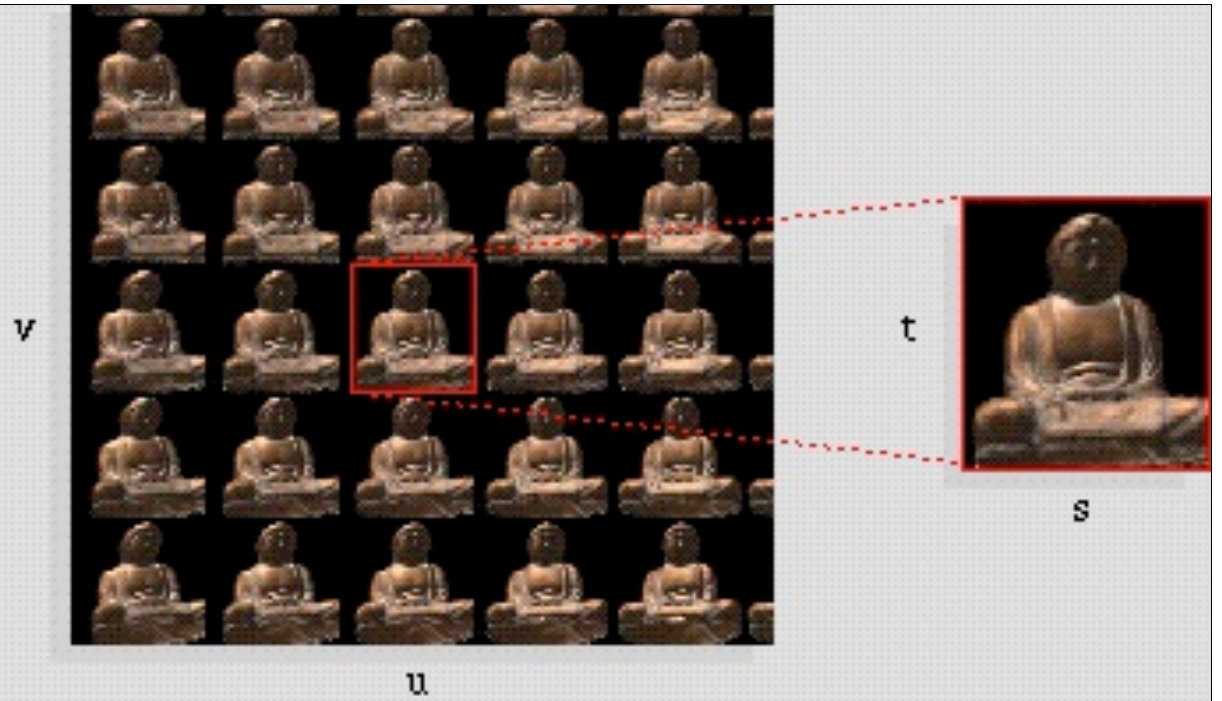
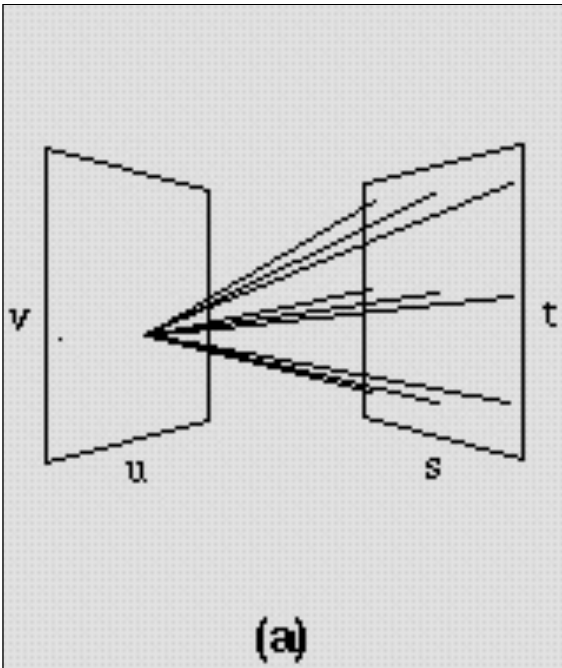
# Optical flow



- Compute flows produced by moving
  - with vision methods, using geometry constraints we haven't done yet
  - interpolate along flow to produce intermediate images

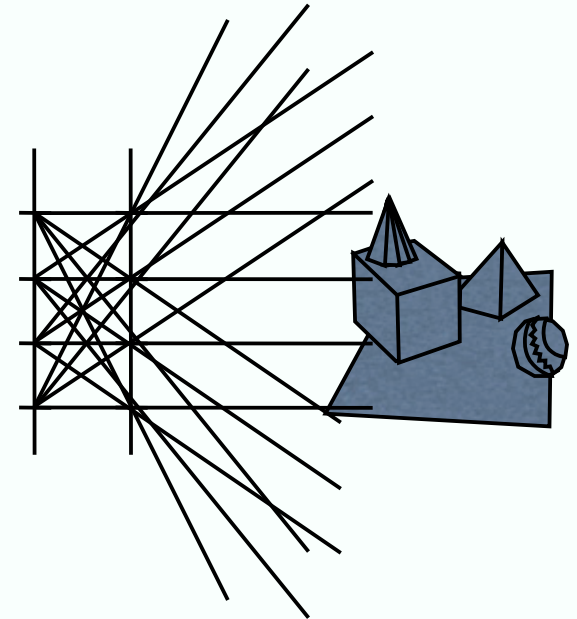
# Explicit image based rendering

- Put object “in a box”
- Evaluate every light ray through the box
  - four dimensional family
  - by taking lots of photographs
- Render
  - query this structure
  - using any ray tracing alg we know

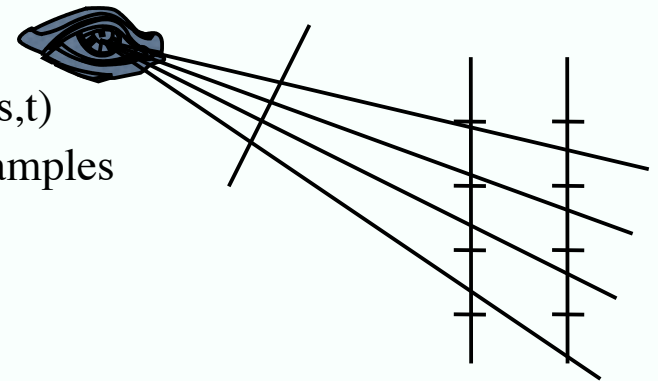


# Rendering and light fields

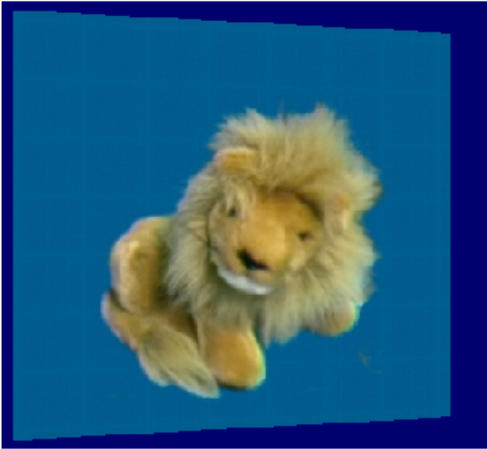
- Rendering into a light field
  - Cast rays between all pairs of points in panes
  - Store resulting radiance at  $(u,v,s,t)$

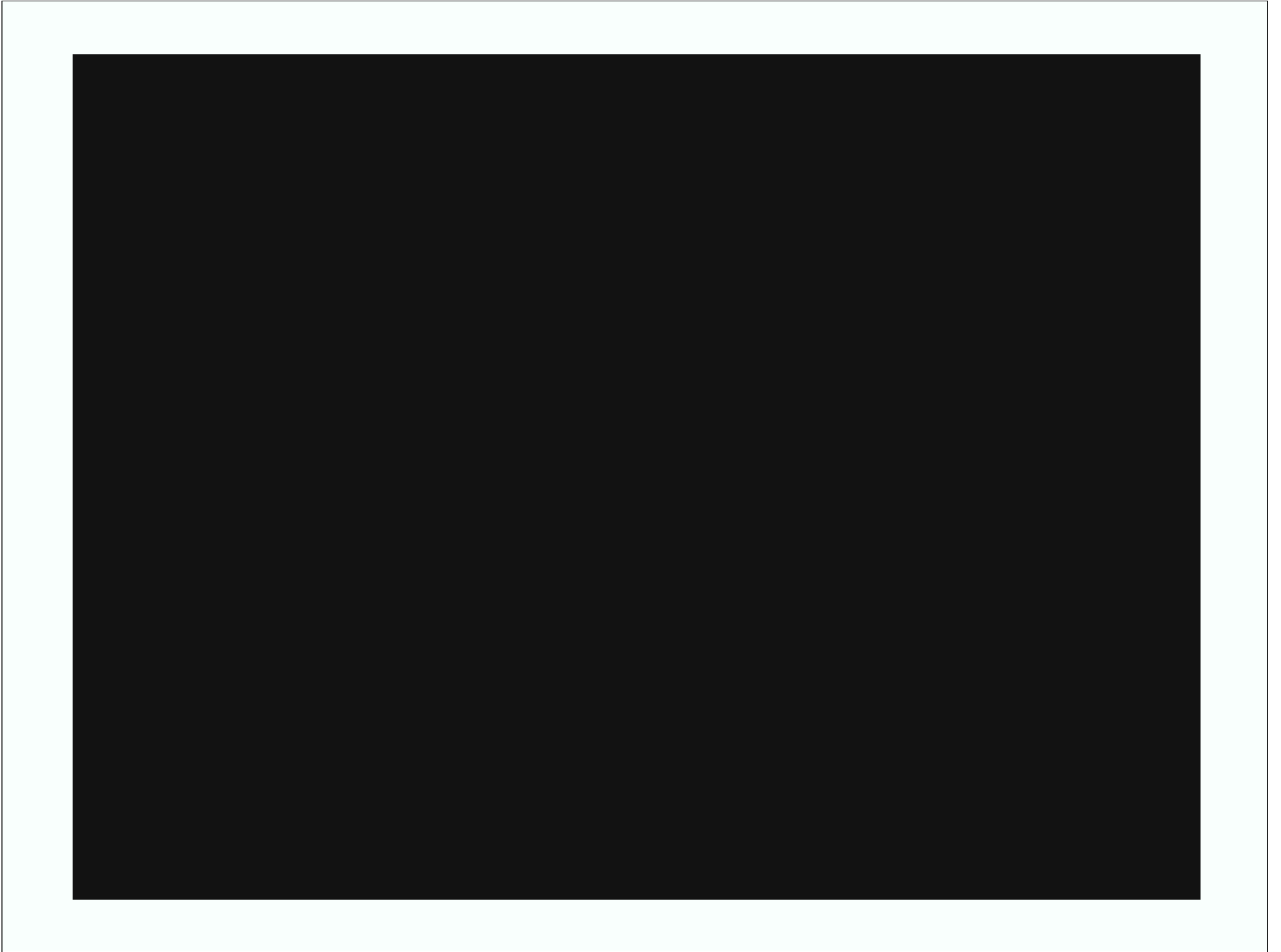


- Rendering from a light field
  - Cast rays through pixels into light field
  - Compute two ray-plane intersections to find  $(u,v,s,t)$
  - Interpolate  $u,v$  and  $s,t$  to find radiance between samples
  - Plot radiance in pixel



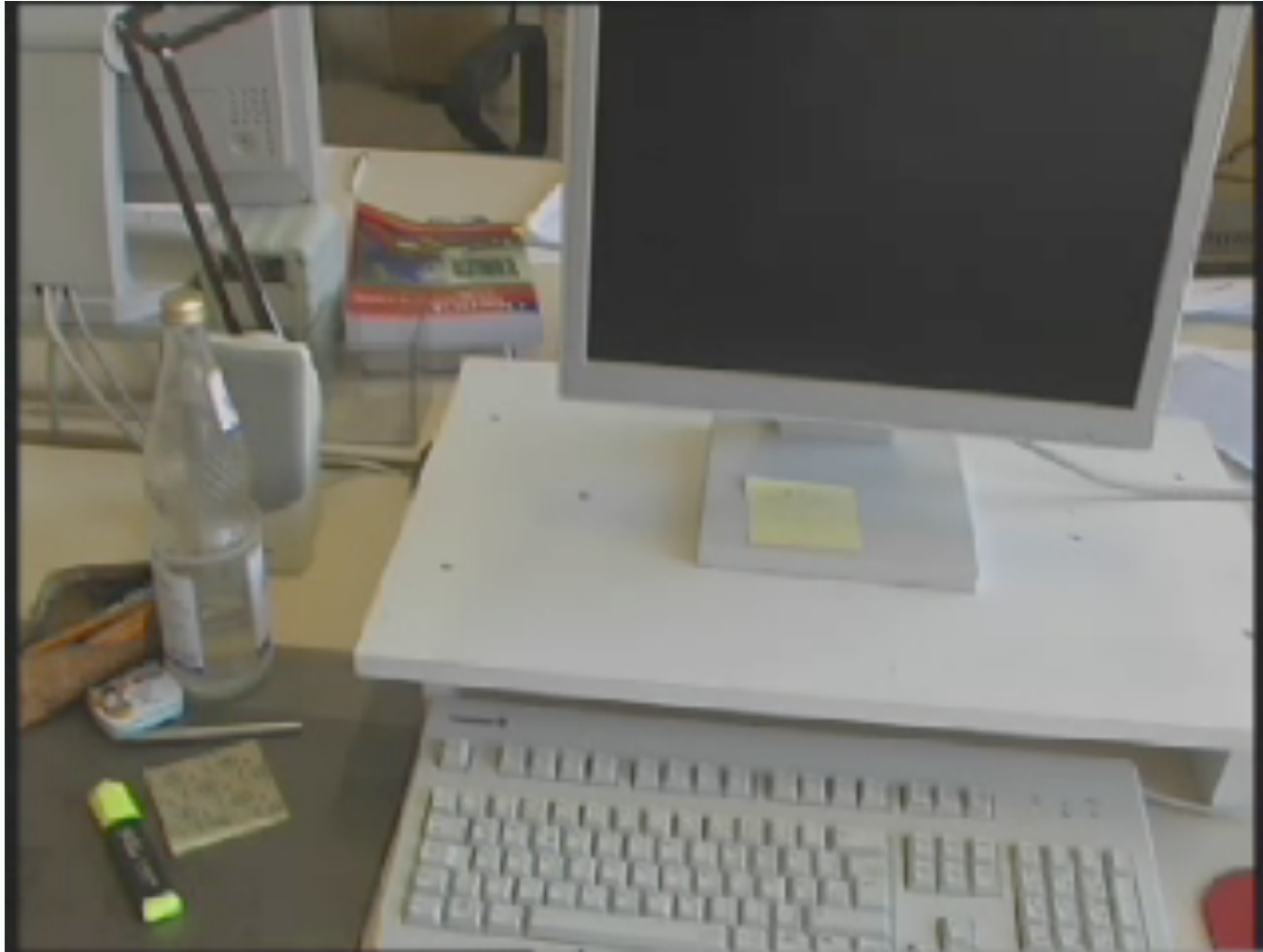






# Postrendering into images, video

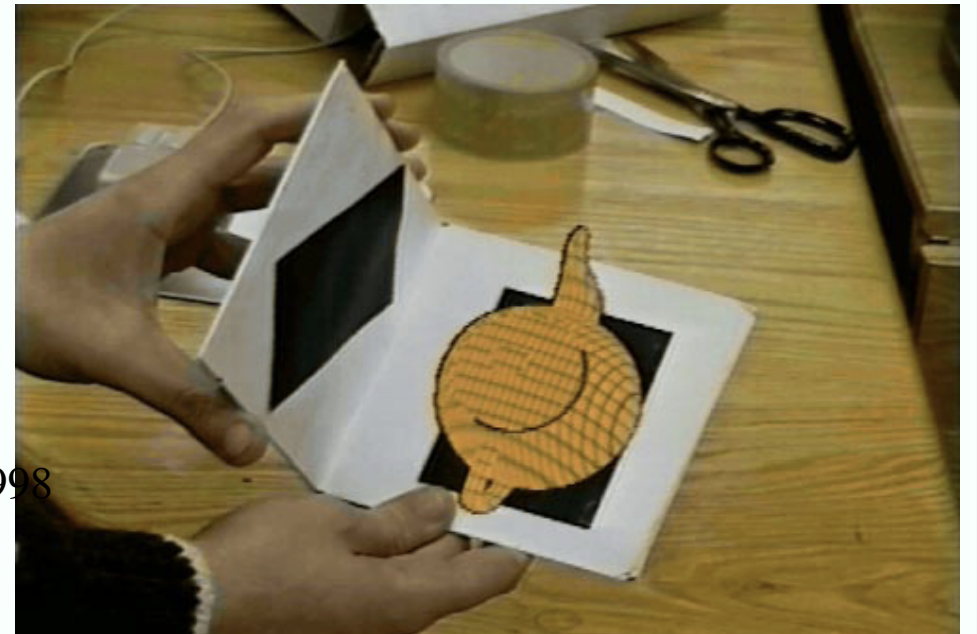
- Options
  - Insert a calibration object, calibrate camera, use this info to render
    - problem: calibration object in picture
  - (video) reconstruct world points, camera, render using camera
    - we'll discuss this shortly





# Camera calibration

- Two strategies:
  - Perspective cameras
    - calibration object has known points in 3D
    - find projections
    - compute camera using least squares
  - Scaled Orthography
    - projection is linear (no division, no H.C.'s)
    - world points as unique linear combination of calibration points
    - image projection is same linear combination of projected calibration points



Calibration-Free Augmented Reality  
Kiriakos N. Kutulakos and James R. Vallino, 1998