

$$\underline{x}' A \underline{x} + \underline{b}' \underline{x} + c = 0$$

↑ symmetric

root finding on

$$t^2 (\underline{v}' A \underline{v}) + t (2 \underline{f}' A \underline{v} + \underline{b}' \underline{v}) + (\underline{f}' A \underline{f} + \underline{b}' \underline{f} + c) = 0$$

again, straight forward.

More general algebraic surface:

$$p(x, y, z) = 0$$

↑ polynomial.

$Q(t) = 0$, by substitution

Problem 1: find smallest t , $t > 0$, st. $Q(t) = 0$
(primary ray)

Problem 2: is there a $0 < t < 1$ such that $Q(t) = 0$
(shadow cast).

Root finding techniques:

Exact (Sturm seqs, etc)

Numerical (Newton's method).

Coherence