

Notice that there is a second invariant

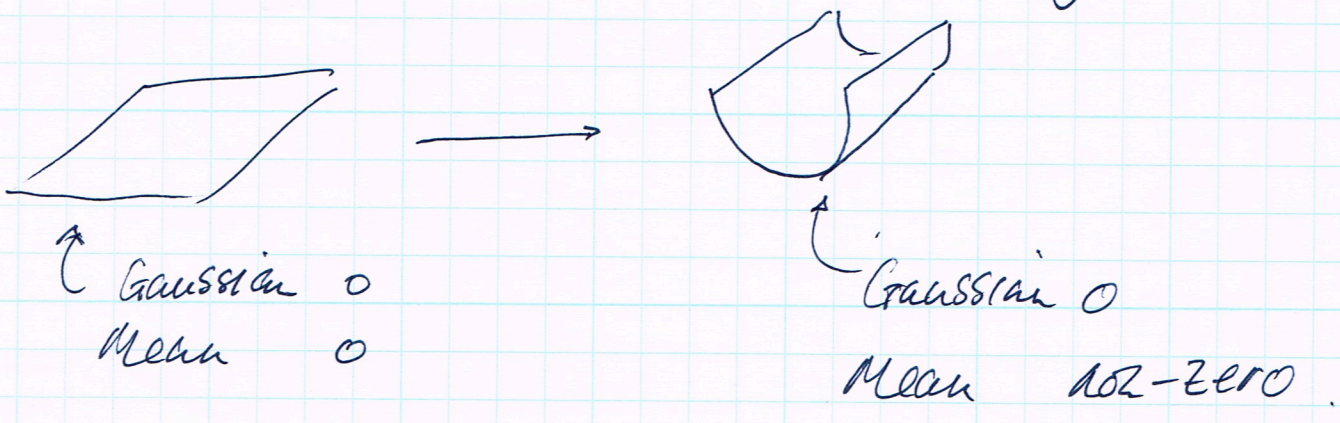
$$\text{Trace}(Q) = \text{Trace}(R^T Q R) = K_1 + K_2$$

$$\text{Mean curvature} = \frac{K_1 + K_2}{2}$$

AARGH!

Gaussian curvature has to do with area  
(demo w/ piece of paper)

Mean curvature with bending



Clearly, there are surfaces w/ non-zero G.C. and zero M.C.  
⇒ here G.C. is always -ve.

At this point, we need more powerful machinery - we don't want to constantly reparametrize.