

CSE-571 Probabilistic Robotics

Fast-SLAM Mapping

Particle Filters

- Represent belief by random **samples**
- Estimation of **non-Gaussian, nonlinear** processes

- Sampling Importance Resampling (SIR) principle
 - ▣ Draw the new generation of particles
 - ▣ Assign an importance weight to each particle
 - ▣ Resampling

- Typical application scenarios are tracking, localization, ...

Dependencies

- Is there a dependency between the dimensions of the state space?
- If so, can we use the dependency to solve the problem more efficiently?

- In the SLAM context
 - ▣ The map depends on the **poses** of the robot.
 - ▣ We know how to build a map **given** the position of the sensor is **known**.

Particle Filter Algorithm

1. Sample the particles from the proposal distribution

$$x_t^{[j]} \sim \pi(x_t | \dots)$$

2. Compute the importance weights

$$w_t^{[j]} = \frac{\text{target}(x_t^{[j]})}{\text{proposal}(x_t^{[j]})}$$

3. Resampling: Draw sample i with probability $w_t^{[i]}$ and repeat J times

Courtesy: C. Stachniss

Particle Representation

- A set of weighted samples

$$\mathcal{X} = \left\{ \langle x^{[i]}, w^{[i]} \rangle \right\}_{i=1, \dots, N}$$

- Think of a sample as one hypothesis about the state
- For feature-based SLAM:

$$x = \left(\underbrace{x_{1:t}}_{\text{poses}}, \underbrace{m_{1,x}, m_{1,y}, \dots, m_{M,x}, m_{M,y}}_{\text{landmarks}} \right)^T$$

Courtesy: C. Stachniss

Dimensionality Problem

Particle filters are effective in low dimensional spaces as the likely regions of the state space need to be covered with samples.

$$x = \left(x_{1:t}, m_{1,x}, m_{1,y}, \dots, m_{M,x}, m_{M,y} \right)^T$$

high-dimensional


Courtesy: C. Stachniss

Can We Exploit Dependencies Between
the Different Dimensions of the State
Space?

$$x_{1:t}, m_1, \dots, m_M$$

Courtesy: C. Stachniss

If We Know the Poses of the Robot,
Mapping is Easy!

$$\underbrace{x_{1:t}}_{\text{poses}}, \underbrace{m_1, \dots, m_M}_{\text{landmarks}}$$


Courtesy: C. Stachniss

Rao-Blackwellization for SLAM

- Factorization of the SLAM posterior

$$p(x_{0:t}, m_{1:M} \mid z_{1:t}, u_{1:t}) = p(x_{0:t} \mid z_{1:t}, u_{1:t}) \underbrace{p(m_{1:M} \mid x_{0:t}, z_{1:t})}$$

Landmarks are conditionally independent given the poses

First exploited in FastSLAM by Montemerlo et al., 2002

Courtesy: C. Stachniss

Rao-Blackwellization for SLAM

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$$p(x_{0:t}, m_{1:M} \mid z_{1:t}, u_{1:t}) = p(x_{0:t} \mid z_{1:t}, u_{1:t}) p(m_{1:M} \mid x_{0:t}, z_{1:t}) \\ p(x_{0:t} \mid z_{1:t}, u_{1:t}) \prod_{i=1}^M p(m_i \mid x_{0:t}, z_{1:t})$$

First exploited in FastSLAM by Montemerlo et al., 2002

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Rao-Blackwellization for SLAM

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2-dimensional EKF!

First exploited in FastSLAM by Montemerlo et al., 2002

Courtesy: C. Stachniss

Rao-Blackwellization for SLAM

- Factorization of the SLAM posterior

$$p(x_{0:t}, m_{1:M} \mid z_{1:t}, u_{1:t}) = p(x_{0:t} \mid z_{1:t}, u_{1:t}) p(m_{1:M} \mid x_{0:t}, z_{1:t}) \\ \underbrace{p(x_{0:t} \mid z_{1:t}, u_{1:t})}_{\text{particle filter similar to MCL}} \prod_{i=1}^M \underbrace{p(m_i \mid x_{0:t}, z_{1:t})}_{\text{2-dimensional EKF!}}$$

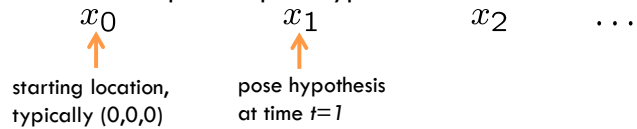
First exploited in FastSLAM by Montemerlo et al., 2002

Courtesy: C. Stachniss

Modeling the Robot's Path

□ Sample-based representation for $p(x_{0:t} | z_{1:t}, u_{1:t})$

□ Each sample is a path hypothesis



□ Past poses of a sample are not revised

□ No need to maintain past poses in the sample set

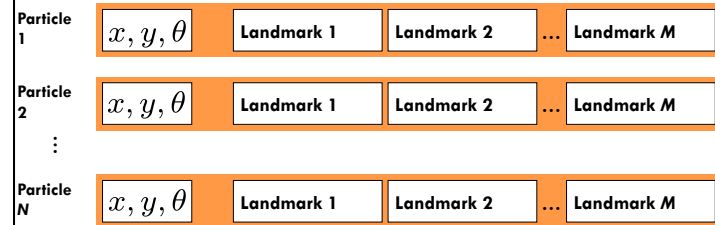
Courtesy: C. Stachniss

FastSLAM

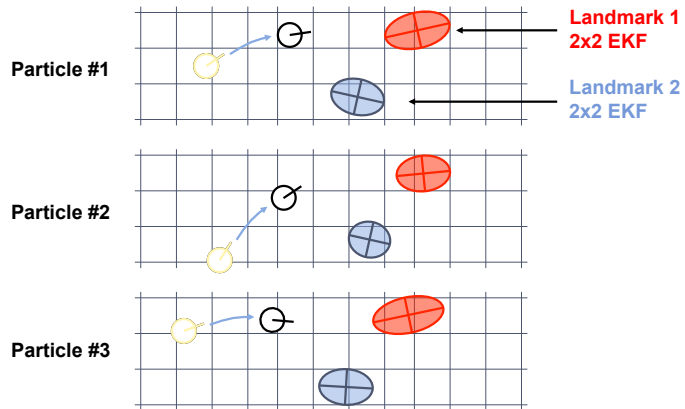
□ Proposed by Montemerlo et al. in 2002

□ Each landmark is represented by a 2x2 EKF

□ Each particle therefore has to maintain M individual EKFs

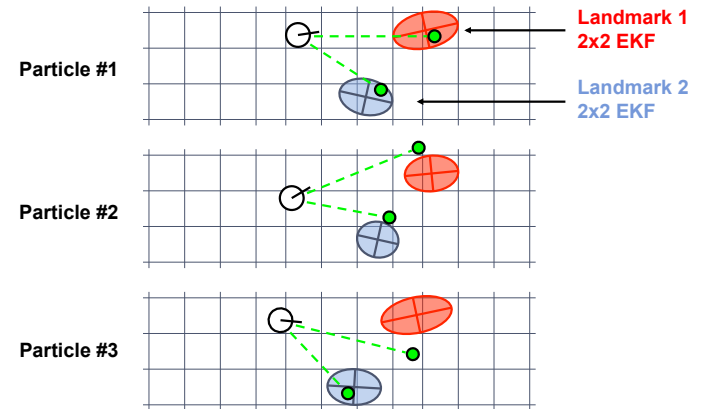


FastSLAM – Action Update

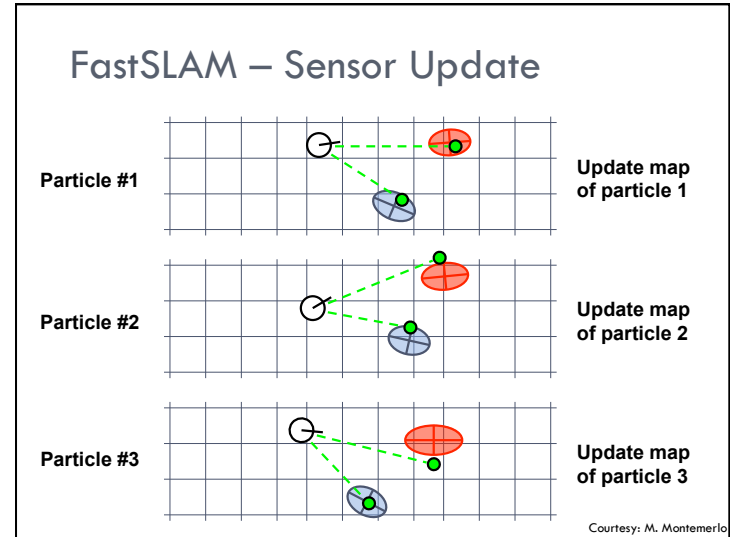
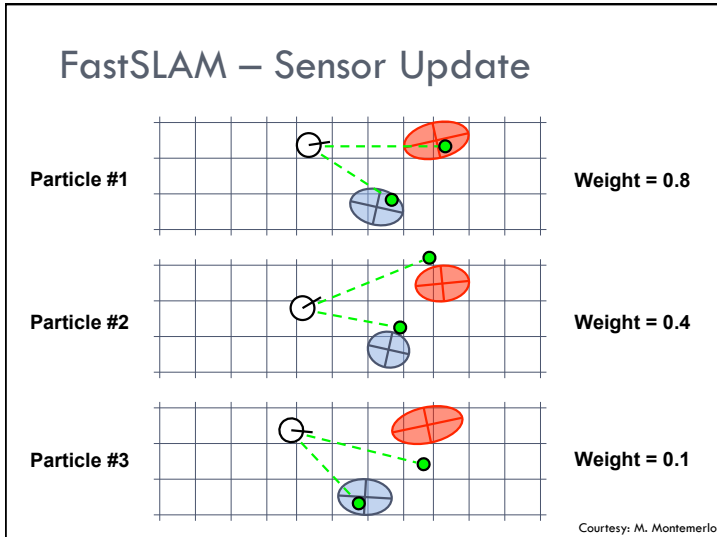


Courtesy: M. Montemerlo

FastSLAM – Sensor Update



Courtesy: M. Montemerlo



Key Steps of FastSLAM 1.0

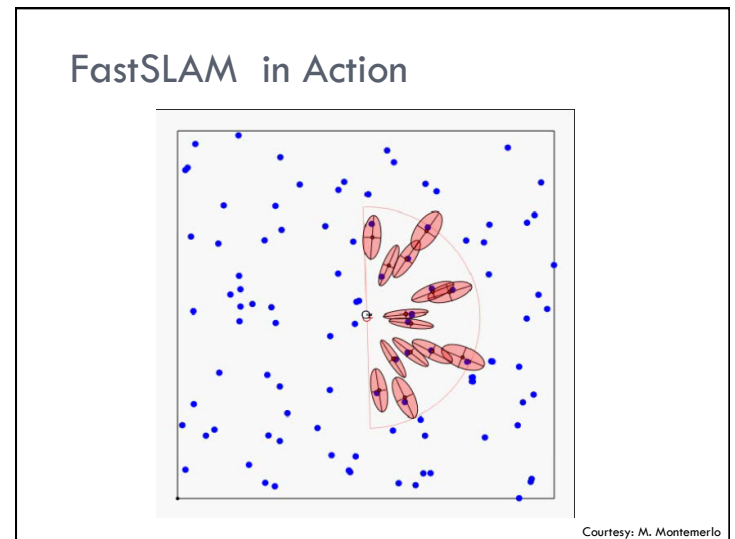
- Extend the path posterior by sampling a new pose for each sample

$$x_t^{[k]} \sim p(x_t | x_{t-1}^{[k]}, u_t)$$
- Compute particle weight

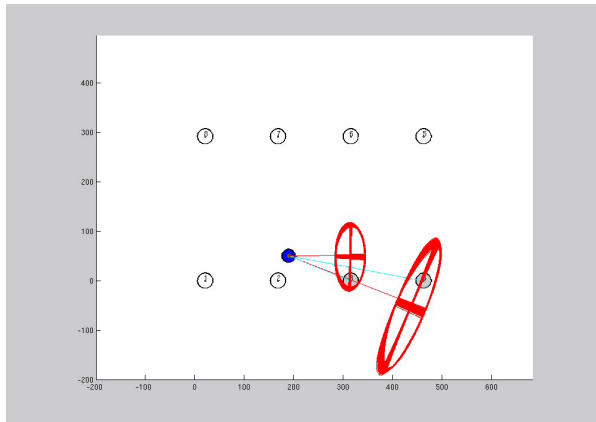
$$w^{[k]} = |2\pi Q|^{-\frac{1}{2}} \exp \left\{ -\frac{1}{2} (z_t - \hat{z}^{[k]})^T Q^{-1} (z_t - \hat{z}^{[k]}) \right\}$$

exp. observation ↓
↑ innovation covariance
- Update belief of observed landmarks (EKF update rule)
- Resample

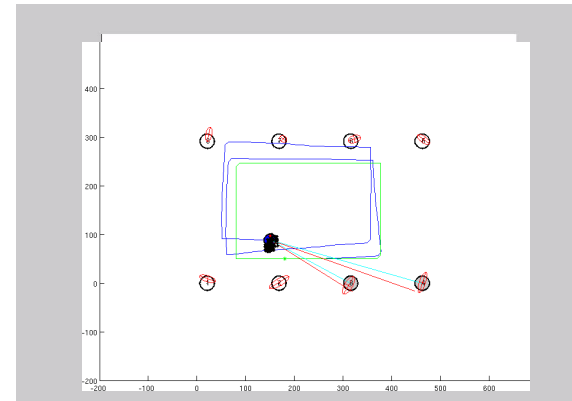
Courtesy: C. Stachniss



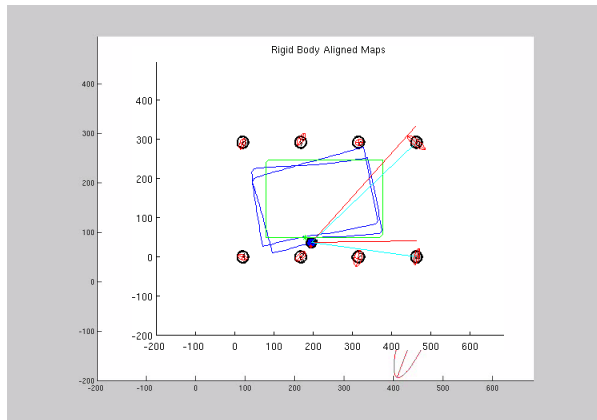
FastSLAM – Video – All Maps



FastSLAM – Video – “Best” particle in terms of **Mode** of the Posterior

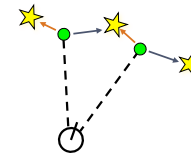


FastSLAM – Video – “Best” particle in terms of **Cum Log Prob**



Data Association Problem

- Which observation belongs to which landmark?

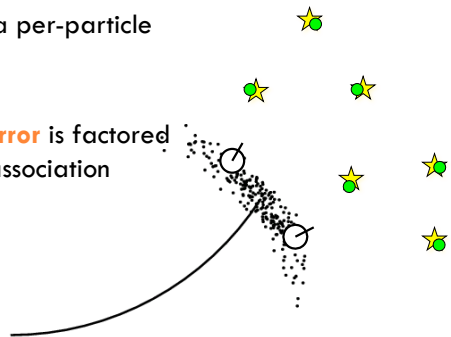


- More than one possible association
- **Potential data associations depend on the pose of the robot**

Courtesy: M. Montemerlo

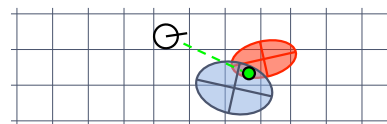
Particles Support for Multi-Hypotheses Data Association

- Decisions on a per-particle basis
- Robot pose **error** is factored out of data association decisions



Courtesy: M. Montemerlo

Per-Particle Data Association

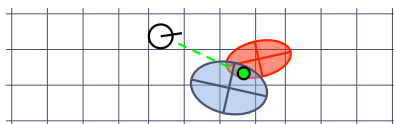


Was the observation generated by the **red** or by the **blue** landmark?

$$P(\text{observation} \mid \text{red}) = 0.3 \quad P(\text{observation} \mid \text{blue}) = 0.7$$

Courtesy: M. Montemerlo

Per-Particle Data Association



Was the observation generated by the **red** or by the **blue** landmark?

$$P(\text{observation} \mid \text{red}) = 0.3 \quad P(\text{observation} \mid \text{blue}) = 0.7$$

- Two options for per-particle data association
 - Pick the most probable match
 - Pick a random association weighted by the observation likelihoods
- If the probability for an assignment is too low, generate a new landmark

Courtesy: M. Montemerlo

Results – Victoria Park

- 4 km traverse
- < 2.5 m RMS position error
- 100 particles



Blue = GPS
Yellow = FastSLAM

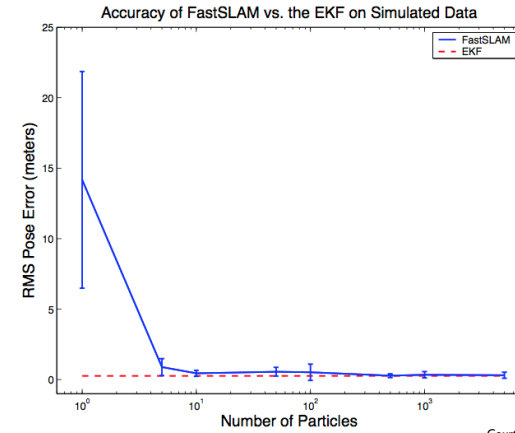
Courtesy: M. Montemerlo

Results – Victoria Park (Video)

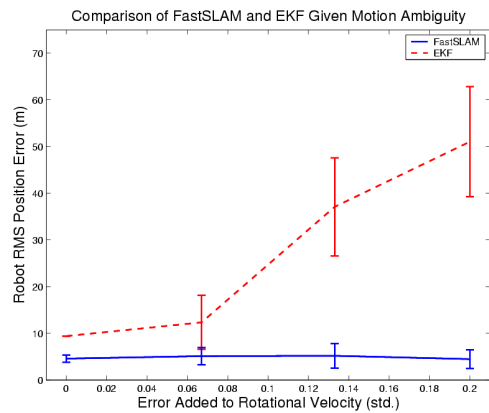


Courtesy: M. Montemerlo

Results (Sample Size)



Results (Motion Uncertainty)



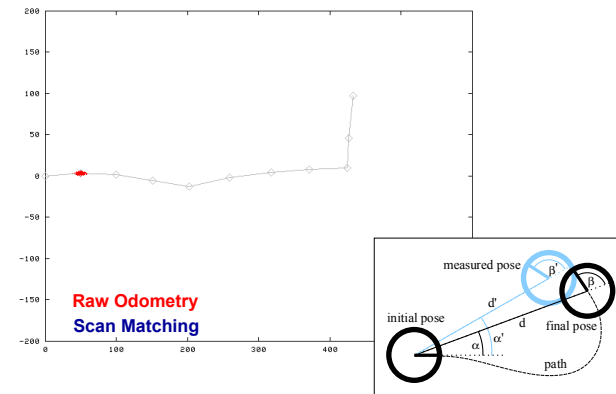
Techniques to Reduce the Number of Particles Needed

- Better proposals (put the particles in the right place in the prediction step).
- Avoid particle depletion (re-sample only when needed).

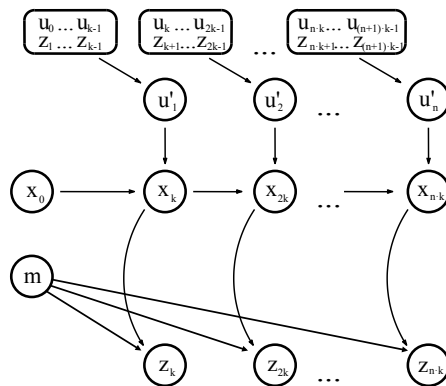
Generating better Proposals

- Use scan-matching to compute highly accurate odometry measurements from consecutive range scans.
- Use the improved odometry in the prediction step to get highly accurate proposal distributions.

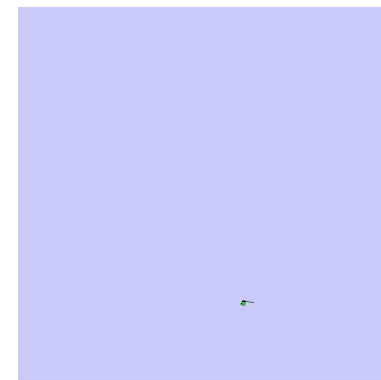
Motion Model for Scan Matching



Graphical Model for Mapping with Improved Odometry

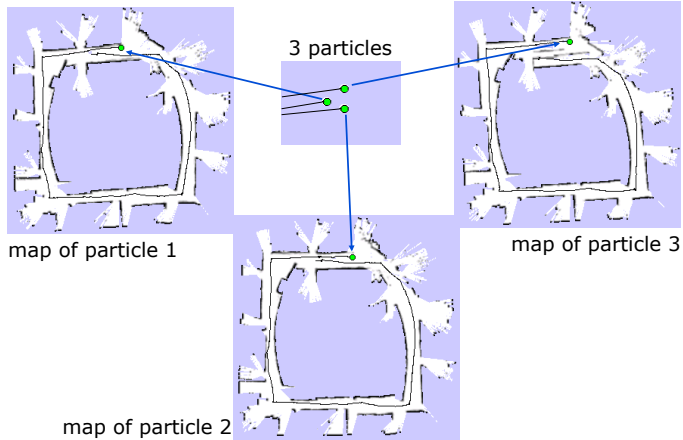


Rao-Blackwellized Mapping with Scan-Matching

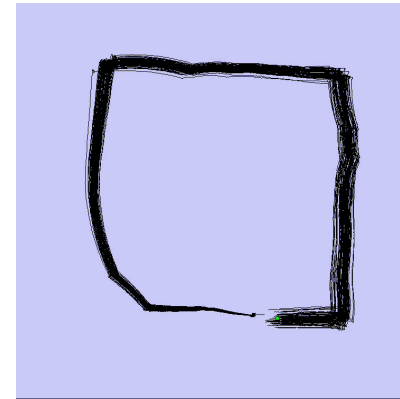


Map: Intel Research Lab Seattle

Loop Closure Example

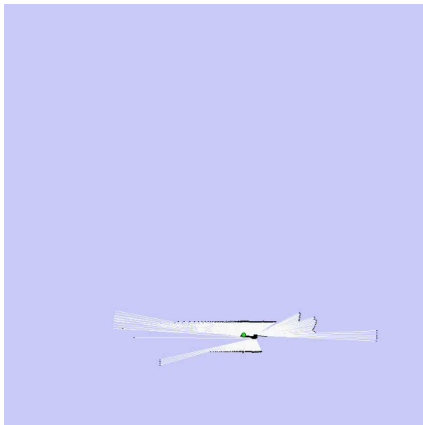


Rao-Blackwellized Mapping with Scan-Matching



Map: Intel Research Lab Seattle

Rao-Blackwellized Mapping with Scan-Matching



Map: Intel Research Lab Seattle

Example (Intel Lab)



- **15 particles**
- four times faster than real-time P4, 2.8GHz
- 5cm resolution during scan matching
- 1cm resolution in final map

Work by Grisetti et al.

Outdoor Campus Map



- **30 particles**
- 250x250m²
- 1.088 miles (odometry)
- 20cm resolution during scan matching
- 30cm resolution in final map

Work by Grisetti et al.

FastSLAM 1.0

- FastSLAM 1.0 uses the motion model as the proposal distribution

$$x_t^{[k]} \sim p(x_t | x_{t-1}^{[k]}, u_t)$$

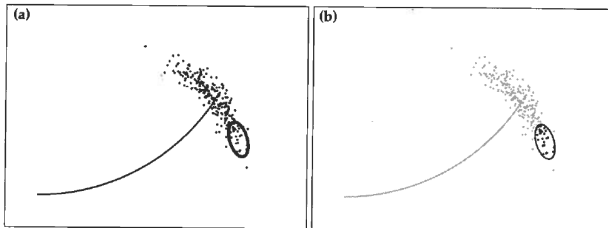
- **Is there a better distribution to sample from?**

[Montemerlo et al., 2002]

Courtesy: C. Stachniss

Weakness of FastSLAM 1.0

- Proposal Distribution
- Importance weighting



FastSLAM 1.0 to FastSLAM 2.0

- FastSLAM 1.0 uses the motion model as the proposal distribution

$$x_t^{[k]} \sim p(x_t | x_{t-1}^{[k]}, u_t)$$

- FastSLAM 2.0 **considers also the measurements during sampling**
- Especially useful if an accurate sensor is used (compared to the motion noise)

[Montemerlo et al., 2003]

Courtesy: C. Stachniss

FastSLAM 2.0 (Informally)

- FastSLAM 2.0 samples from

$$x_t^{[k]} \sim p(x_t | x_{1:t-1}^{[k]}, u_{1:t}, z_{1:t})$$

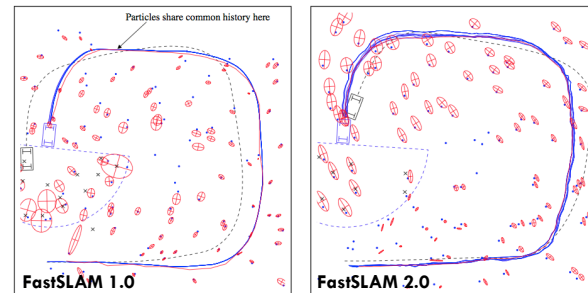
- Results in a more peaked proposal distribution
- Less particles are required
- More robust and accurate
- But more complex...

[Montemerlo et al., 2003]

Courtesy: C. Stachniss

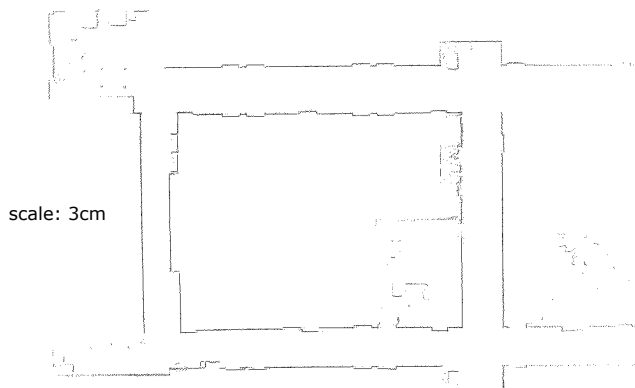
FastSLAM Problems

- How to determine the sample size?
- Particle deprivation, especially when closing (multiple) loops



Courtesy: M. Montemerlo

DP-SLAM: High-Res Fast-SLAM via History Sharing

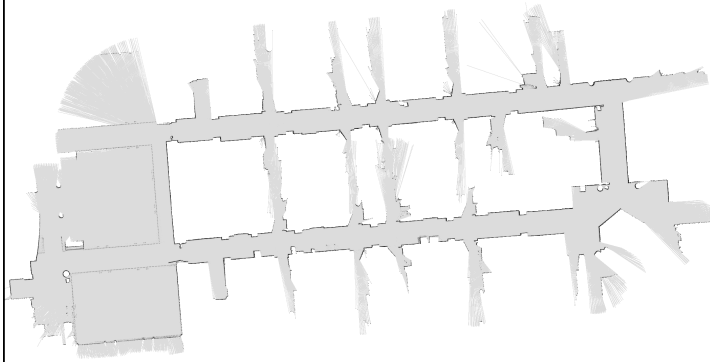


Run at real-time speed on 2.4GHz Pentium 4 at 10cm/s

Consistency

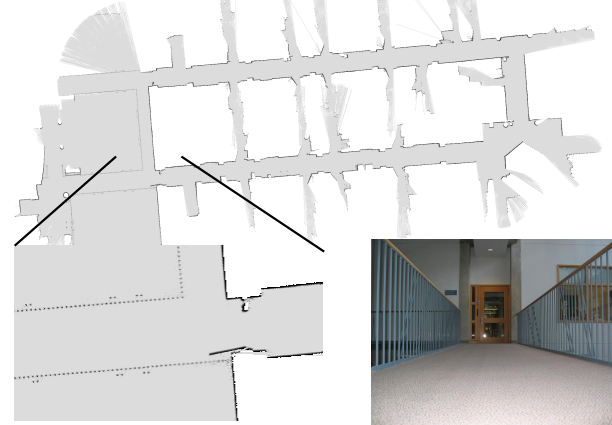


Results obtained with DP-SLAM 2.0 (offline)



Eliazar & Parr, 04

Close up



End courtesy of Eliazar & Parr

FastSLAM Summary

- Particle filter-based SLAM
- Rao-Blackwellization: model the robot's path by sampling and compute the landmarks given the poses
- Allow for per-particle data association
- FastSLAM 1.0 and 2.0 differ in the proposal distribution
- Complexity $\mathcal{O}(N \log M)$

Courtesy: C. Stachniss

Literature

FastSLAM

- Thrun et al.: "Probabilistic Robotics", Chapter 13.1-13.3 + 13.8 (see errata!)
- Montemerlo, Thrun, Kollar, Wegbreit: FastSLAM: A Factored Solution to the Simultaneous Localization and Mapping Problem, 2002
- Montemerlo and Thrun: Simultaneous Localization and Mapping with Unknown Data Association Using FastSLAM, 2003

Courtesy: C. Stachniss